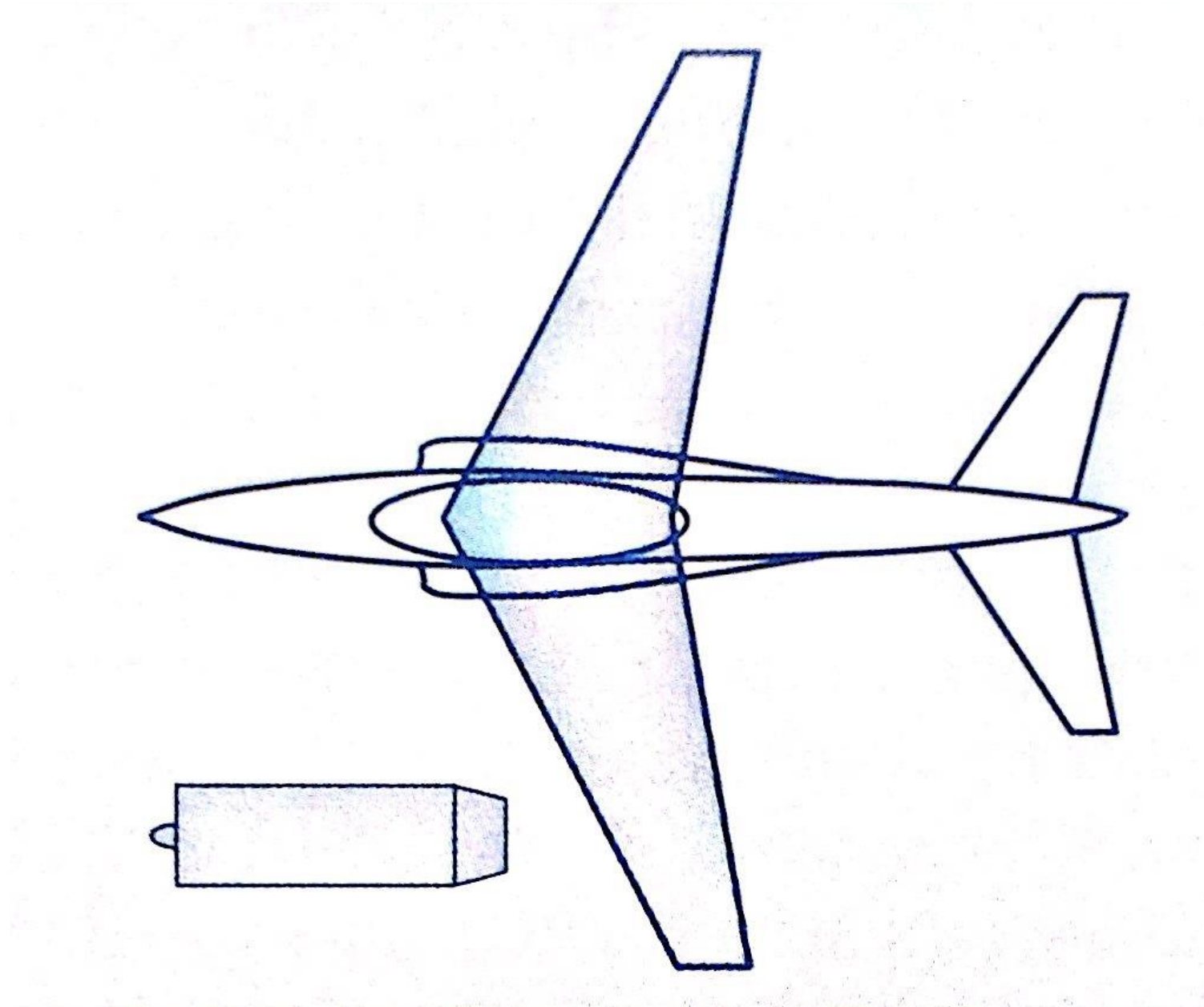


# ME4932 Aircraft Performance & Design

## T/ W and W/S (Chapter5)



# ME4932 Aircraft Performance & Design

## T/ W and W/S (Chapter5)

- T/W and W/S have the greatest effect on performance so we need to choose them well
- We look at the performance requirements
- Inappropriate to use purely historical data
- Cannot draw the A/C without wing or engine!




# ME4932 Aircraft Performance & Design

## T/ W and W/S (Chapter5)

- These values are normally listed at  $W_0$ , sea level, STP

Aircraft type	Typical installed $T/W$
Jet trainer	0.4
Jet fighter (dogfighter)	0.9
Jet fighter (other)	0.6
Military cargo/bomber	0.25
Jet transport (higher value for fewer engines)	0.25–0.4



Aircraft type	Typical $P/W$		Typical power loading (lb/hp)
	hp/lb	{Watt/g}	
Powered sailplane	0.04	{0.07}	25
Homebuilt	0.08	{0.13}	12
General aviation—single engine	0.07	{0.12}	14
General aviation—twin engine	0.17	{0.3}	6
Agricultural	0.09	{0.15}	11
Twin turboprop	0.20	{0.33}	5
Flying boat	0.10	{0.16}	10



# ME4932 Aircraft Performance & Design

## T/ W and W/S (Chapter5)

- These values are normally listed at  $W_0$ , sea level, STP

$T/W_0 = \alpha M_{\max}^C$	$a$	$C$
Jet trainer	0.488	0.728
Jet fighter (dogfighter)	0.648	0.594
Jet fighter (other)	0.514	0.141
Military cargo/bomber	0.244	0.341
Jet transport	0.267	0.363



# ME4932 Aircraft Performance & Design

## T/ W and W/S (Chapter5)

- These values are normally listed at  $W_0$ , sea level, STP

$P/W_0 = \alpha V_{\max}^3: \text{hp/lb}\{W/g\}$	$a$	$c$
Sailplane—powered	0.043 {0.071}	0
Homebuilt—metal/wood	0.005 {0.006}	0.57
Homebuilt—composite	0.004 {0.005}	0.57
General aviation—single engine	0.025 {0.036}	0.22
General aviation—twin engine	0.036 {0.048}	0.32
Agricultural aircraft	0.009 {0.010}	0.50
Twin turboprop	0.013 {0.016}	0.50
Flying boat	0.030 {0.043}	0.23

# ME4932 Aircraft Performance & Design

## T/ W and W/S (Chapter5)

Thrust Matching:

$$\left(\frac{T}{W}\right)_{\text{cruise}} = \frac{1}{(L/D)_{\text{cruise}}}$$

Climb rate requirement  
frequently sizes T/W!

$$\left(\frac{T}{W}\right)_{\text{climb}} = \frac{1}{(L/D)_{\text{climb}}} + \boxed{\frac{V_{\text{vertical}}}{V}}$$

From mission weight  
fractions

To convert to T/W<sub>0</sub> must do this:

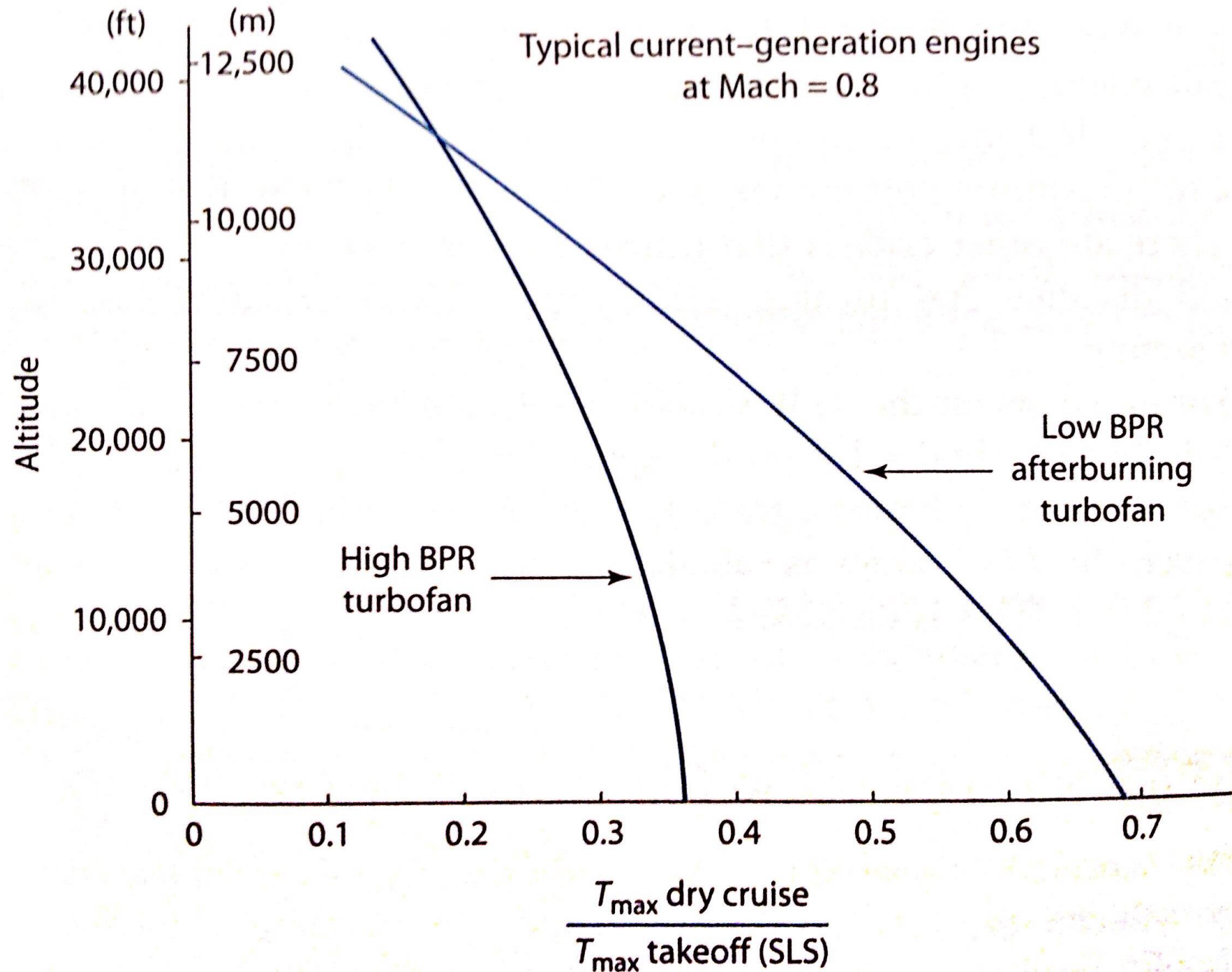
$$\left(\frac{T}{W}\right)_{\text{takeoff}} = \left(\frac{T}{W}\right)_{\text{cruise}} \left(\frac{W_{\text{cruise}}}{W_{\text{takeoff}}}\right) \left(\frac{T_{\text{takeoff}}}{T_{\text{cruise}}}\right)$$

From engine data



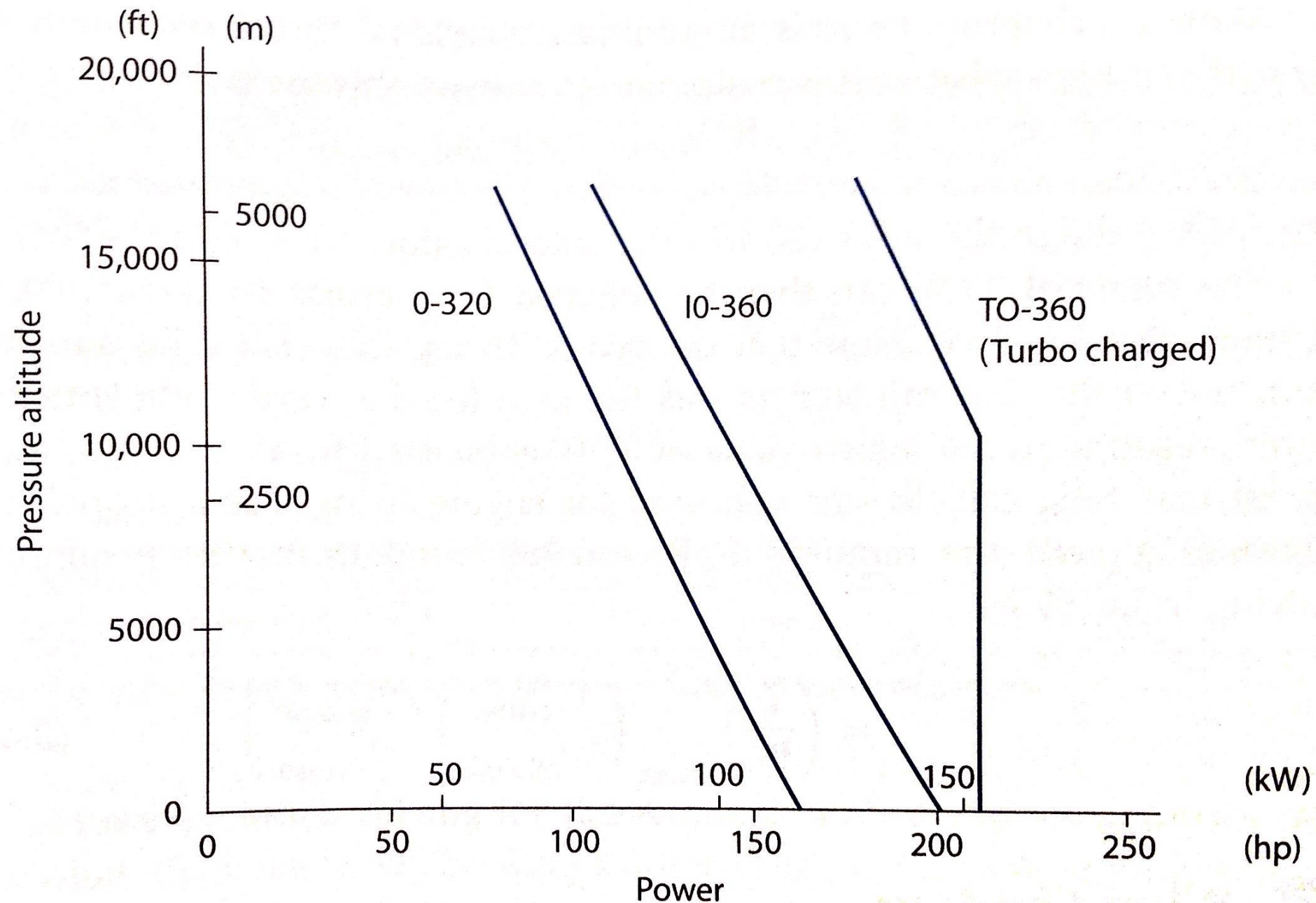
# ME4932 Aircraft Performance & Design

## T/ W and W/S (Chapter5)



# ME4932 Aircraft Performance & Design

## T/ W and W/S (Chapter5)





# ME4932 Aircraft Performance & Design

## T/ W and W/S (Chapter5)

- Mostly to get a "flavor" of what a typical W/S would be:

Typical Takeoff W/S		
Historical trends	lb/ft <sup>2</sup>	{kg/m <sup>2</sup> }
Sailplane	6	{30}
Homebuilt	11	{54}
General aviation—single engine	17	{83}
General aviation—twin engine	26	{127}
Twin turboprop	40	{195}
Jet trainer	50	{244}
Jet fighter	70	{342}
Jet transport/bomber	120	{586}

# ME4932 Aircraft Performance & Design

## T/ W and W/S (Chapter5)

- Stall speed requirement sets W/S:

$$W = L = q_{\text{stall}} S C_{L_{\text{max}}} = \frac{1}{2} \rho V_{\text{stall}}^2 S C_{L_{\text{max}}}$$
$$W/S = \frac{1}{2} \rho V_{\text{stall}}^2 C_{L_{\text{max}}}$$

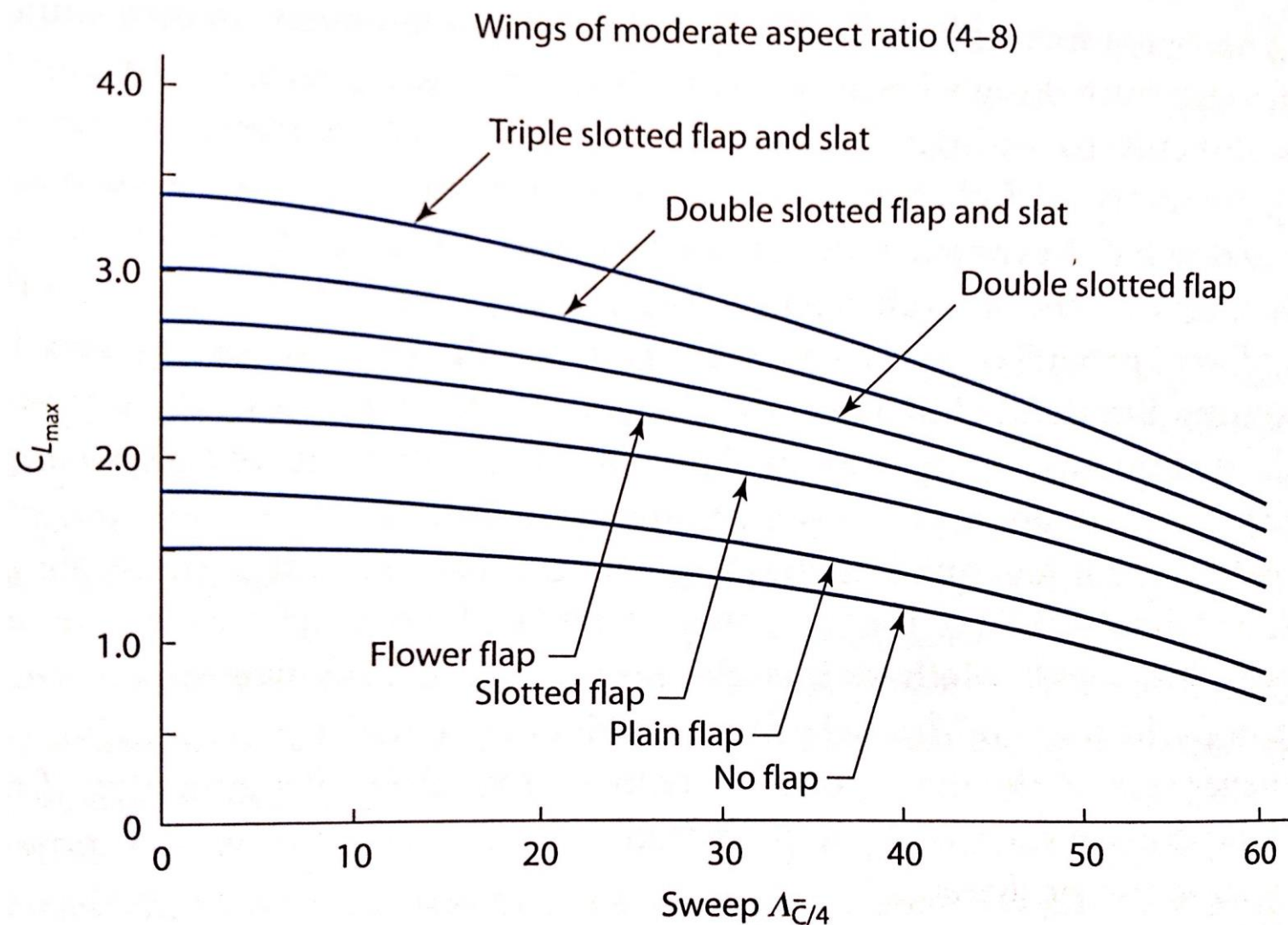
$$C_{L_{\text{max}}} = 0.9 C_{\ell_{\text{max}}} \cos \Lambda_{0.25c}$$

- If stall speed is a requirement, you can compute a W/S from it and from a section  $C_{l_{\text{max}}}$ . Then, you can compare this W/S with the one required by other requirements (like takeoff/landing) and decide what high-lift devices to use to change  $C_{l_{\text{max}}}$  to then change W/S to a more consistent or less penalizing one!



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## T/ W and W/S (Chapter5)



- HLD will allow you to have a larger W/S, that way avoiding penalties of a huge wing (wetted area and weight) that would hurt your design in other areas by not meeting a requirement (like max speed) or requiring a huge T/W and again Wo!

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## T/ W and W/S (Chapter5)

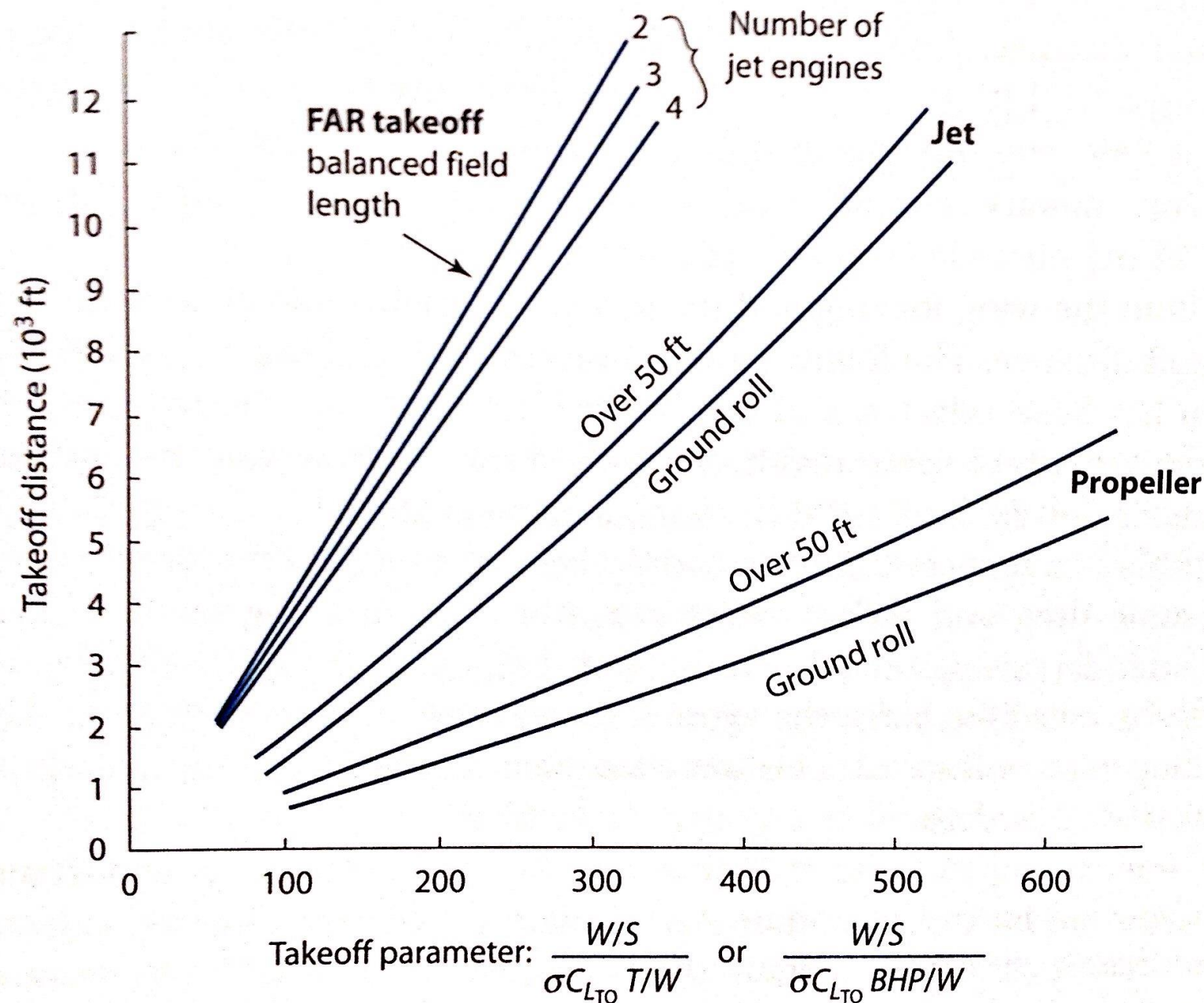
- Takeoff distance:
  - Ground roll
  - Total distance to clear an obstacle (35 or 50 ft.)
  - Balanced field length (distance required to clear the obstacle when an engine fails at decision speed)
  - Liftoff speed =  $1.1 V_{stall}$
  - Decision speed = speed at which the distance to stop after an engine fails equals the distance to continue and clear the obstacle
  - Takeoff distance requirements can set T/W and/or W/S
  - FAR,MIL regulations



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## T/ W and W/S (Chapter5)

- Takeoff distance requirements can set T/W and/or W/S:



$$(W/S) = (TOP)\sigma C_{L_{TO}}(hp/W)$$

$$(W/S) = (TOP)\sigma C_{L_{TO}}(T/W)$$

# ME4932 Aircraft Performance & Design

## T/ W and W/S (Chapter5)

- Catapult takeoff
  - Current steam catapults accelerate light aircraft more than heavier aircraft!
  - $V_{end}$  = catapult end speed
  - $V_{wod}$  = wind speed over deck
  - $V_{thrust}$  = extra velocity (3-10 kts) provided by engine
  - In the end, the velocity of the aircraft, as it leaves the catapult should be greater or equal to 1.1 stall

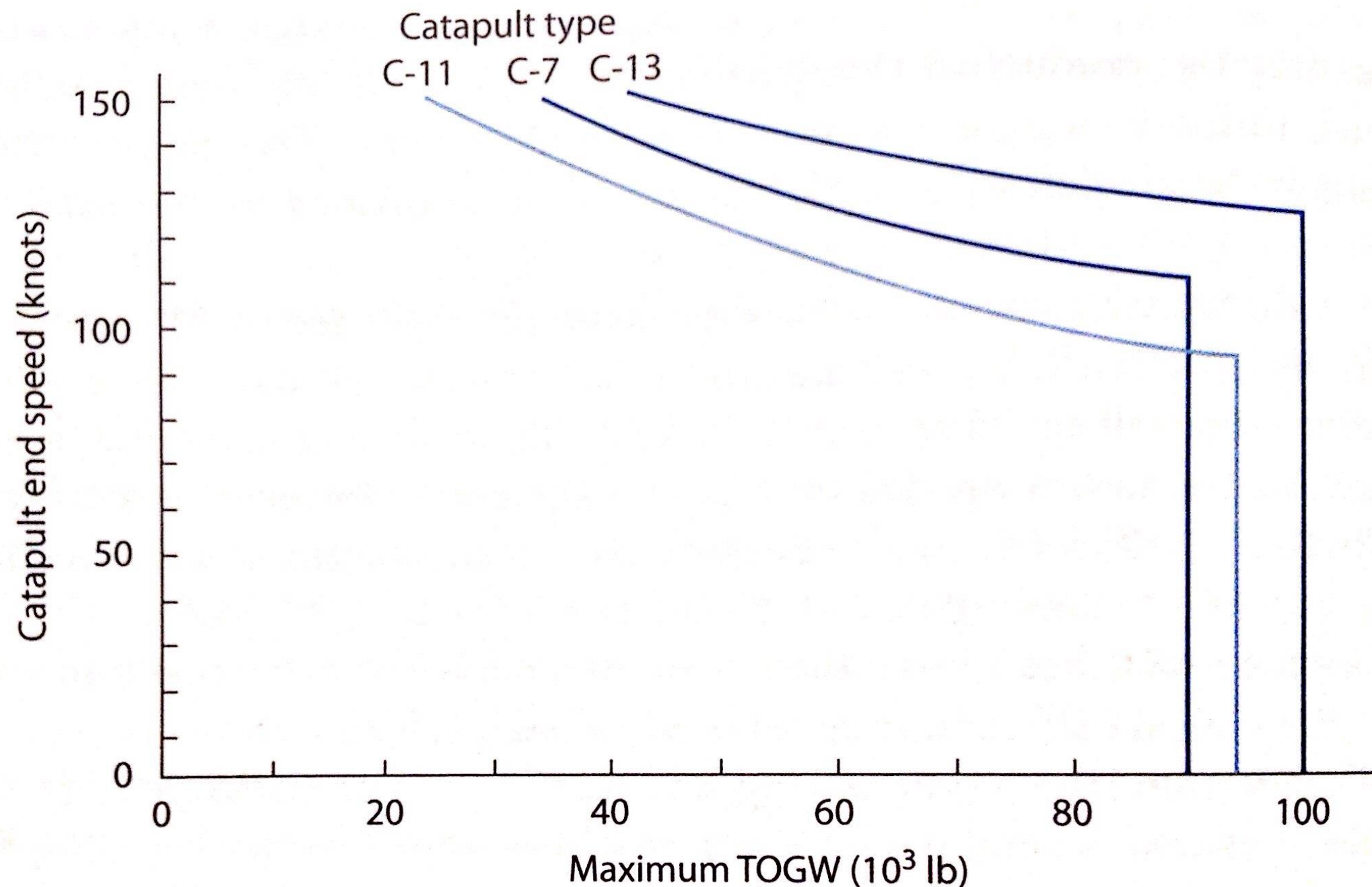
$$\left(\frac{W}{S}\right)_{takeoff} = \frac{1}{2} \rho (V_{end} + V_{wod} + \Delta V_{thrust})^2 \frac{(C_{L_{max}})_{takeoff}}{1.21}$$



# ME4932 Aircraft Performance & Design

## T/ W and W/S (Chapter5)

- Catapult takeoff:



# ME4932 Aircraft Performance & Design

## T/ W and W/S (Chapter5)

- Landing distance can set W/S:
  - Ground roll, or total distance from a 50 ft. obstacle?
  - Approach speed = 1.2  $V_{stall}$  for military (1.3 civil)

$$\begin{aligned} S_{\text{landing}} &= 80 \left( \frac{W}{S} \right) \left( \frac{1}{\sigma C_{L_{\max}}} \right) + S_a \quad \{\text{ft}\} \\ &= 5 \left( \frac{W}{S} \right) \left( \frac{1}{\sigma C_{L_{\max}}} \right) + S_a \quad \{\text{m}\} \end{aligned} \quad (5.11)$$

where

$\sigma$  = density ratio =  $\rho_{\text{landing}} / \rho_{\text{sea-level standard day}}$   
( $\sigma = 1.0$  for sea-level standard day;  $\sigma = 0.794$  for hot day at 5000 ft)

$S_a = 1000 \text{ ft } \{305 \text{ m}\}$  for airliner-type, 3-deg glideslope  
 $= 600 \text{ ft } \{183 \text{ m}\}$  for general-aviation-type power-off approach  
 $= 450 \text{ ft } \{137 \text{ m}\}$  for STOL, 7-deg glideslope



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## T/ W and W/S (Chapter5)

- Remember that if your W/S was calculated at a reduced weight (landing or other) you need to bring it to  $W_0$  level!
- For example if the landing requirement was at  $80\%W_0$ , and you came up with a W/S of 16, then at  $W_0$  this is a W/S of  $16/0.8 = 20$ ! Otherwise, you will end up with a wing that was unnecessarily large!
- In general, be careful to compare "apples to apples"....

# ME4932 Aircraft Performance & Design

## T/ W and W/S (Chapter5)

- W/S at cruise/loiter (what segment dominates the mission fuel requirement?):
  - Mostly calculated for reference, because the W/S that cruise and/or loiter conditions dictate is usually too low (large wing) to be able to do many other requirements.
  - For propeller aircraft, best cruise is at maximum L/D, where zero-lift drag and drag due-to-lift are equal in magnitude.
  - For jets, best cruise is at a lower L/D, where zero-lift drag is three times the magnitude of drag due-to-lift.
  - For loiter, jets prefer maximum L/D; propeller aircraft a lower L/D.

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## T/ W and W/S (Chapter5)

W/S at cruise/loiter (continued):

- Maximum prop range or jet loiter:  $W/S = q \sqrt{\pi A e C_{D_0}}$
- Maximum jet range:  $W/S = q \sqrt{\pi A e C_{D_0} / 3}$
- Maximum prop loiter:  $W/S = q \sqrt{3 \pi A e C_{D_0}}$

Assume:

- $C_{D_0} = 0.015$  jet, 0.02 (clean prop) to 0.03 (dirty prop , fixed gear)
- $e = 0.6$  to 0.8
- Altitude = limit h for turbocharged prop (S.L. if no turbo charger), 35,000 for jet
- Loiter speed = 150-200 kts. (jets), 80-120 kts. (props)



# ME4932 Aircraft Performance & Design

## T/ W and W/S (Chapter5)

- W/S for **instantaneous** turn rate requirements:
- 2 deg./sec. advantage is significant.
- Maximum instantaneous turn rate is set by CLmax and maximum load factor (remember CLmax is for the req'd flight conditions!):

$$\begin{array}{c} \dot{\psi} = \frac{g\sqrt{n^2 - 1}}{V} \\ n = \frac{qC_L}{W/S} \end{array} \quad \Rightarrow \quad n = \sqrt{\left(\frac{\dot{\psi}V}{g}\right)^2 + 1} \quad \Rightarrow \quad \frac{W}{S} = \frac{qC_{L_{\max}}}{n}$$

- W/S for turn rate requirements must be corrected back to Wo!

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## T/ W and W/S (Chapter5)

- W/S for **sustained** turn rate requirements:
- Maximum load factor at which velocity and altitude can be sustained. ( $T = D$ ,  $L = n \times W$ ).

$$n = (T/W)(L/D)$$

- Maximize T/W and L/D!

$$\frac{W}{S} = \frac{(T/W) \pm \sqrt{(T/W)^2 - (4n^2 C_{D_0} / \pi A e)}}{2n^2 / q \pi A e}$$

- Warning: the higher the load factor, the less appropriate the parabolic drag polar is (e may be too optimistic).

# ME4932 Aircraft Performance & Design

## T/ W and W/S (Chapter5)

- Climb and Glide requirement could set W/S if T/W is set low.
- Define G, climb gradient as the ratio of vertical and horizontal distance traveled:

$$G = (T - D)/W$$

$$\frac{W}{S} = \frac{[(T/W) - G] \pm \sqrt{[(T/W) - G]^2 - (4C_{D0}/\pi Ae)}}{2/q\pi Ae}$$

- If set  $T/W = 0$ , can obtain the W/S for a required power-off glide angle.
- The term inside the square root sign must be positive! No matter how clean your design is, T/W must be higher than the desired climb gradient! That's why a climb rate requirement frequently sets T/W instead of W/S!

$$\boxed{\frac{T}{W} \geq G + 2\sqrt{\frac{C_{D0}}{\pi Ae}}}$$



# ME4932 Aircraft Performance & Design

## T/ W and W/S (Chapter5)

- Ceiling requirement:
- At the absolute ceiling,  $P_s = R/C = 0$
- At the service ceiling ,  $P_s = R/C = 100 \text{ ft./min.}$
- Can use the previous formula, setting  $G = (\text{Required } P_s) / V$  if T/W known.
- Can use a design lift coefficient and  $W/S = qCL$
- Check with W/S for minimum power:  $W/S = q\sqrt{\pi AeC_{D_0}}$

# ME4932 Aircraft Performance & Design

## T/ W and W/S (Chapter5)

- Estimate T/W, P/W initially (better to use maximum speed and perhaps climb rate requirements)
- Calculate the lowest W/S (remember correction to  $W_0$  level)
- Remember that both **high** T/W and **low** W/S are expensive! Especially with W/S find alternatives (like HLD) to mitigate the effects on  $W_0$ . If necessary, relax a requirement!
- Re-check your final T/W and W/S and use for configuration layout!