



# Interferometry

MPAGS Astrophysical Techniques 2021

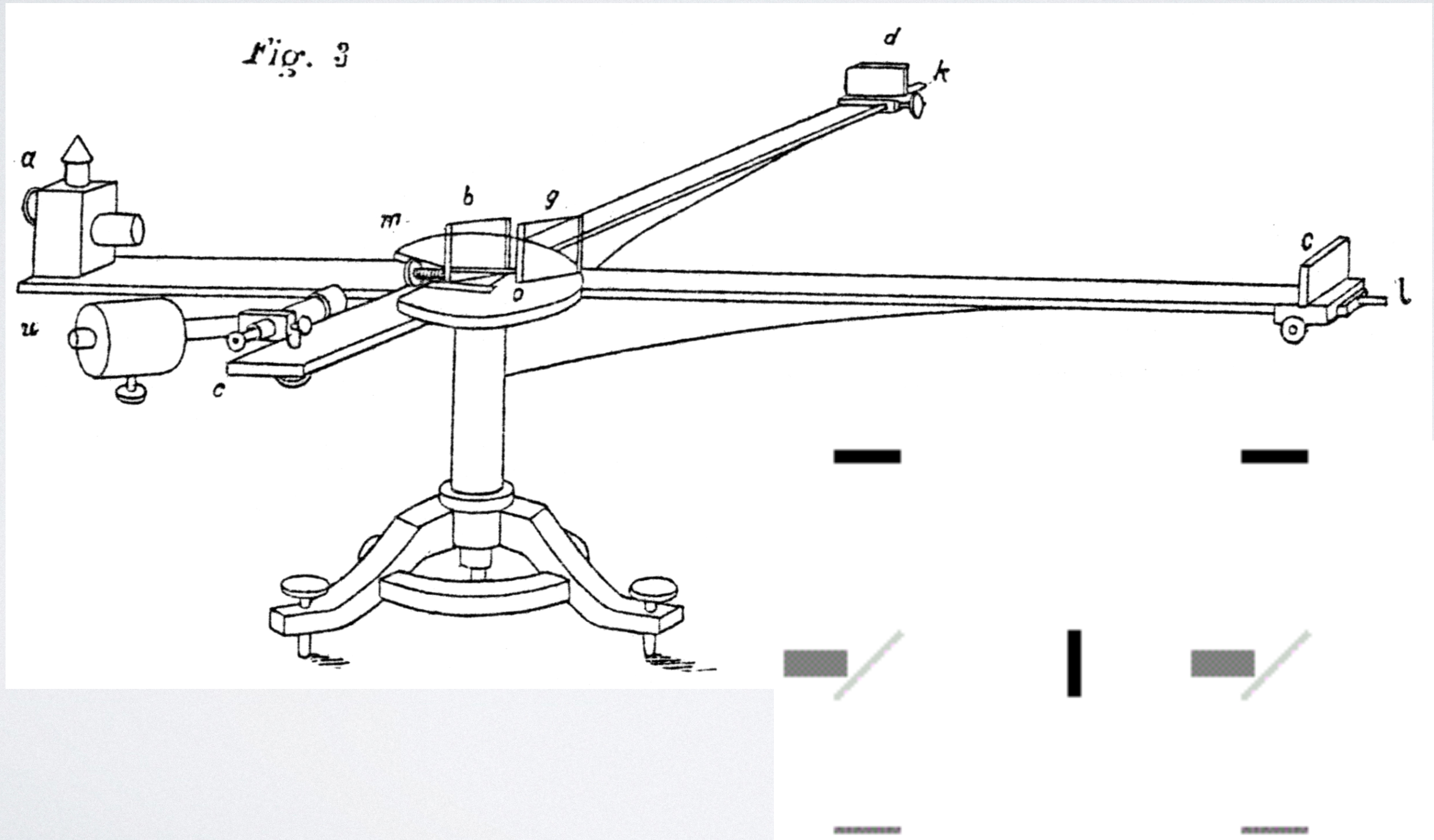
Grant Kennedy

(this session is being recorded)



# Early interferometers

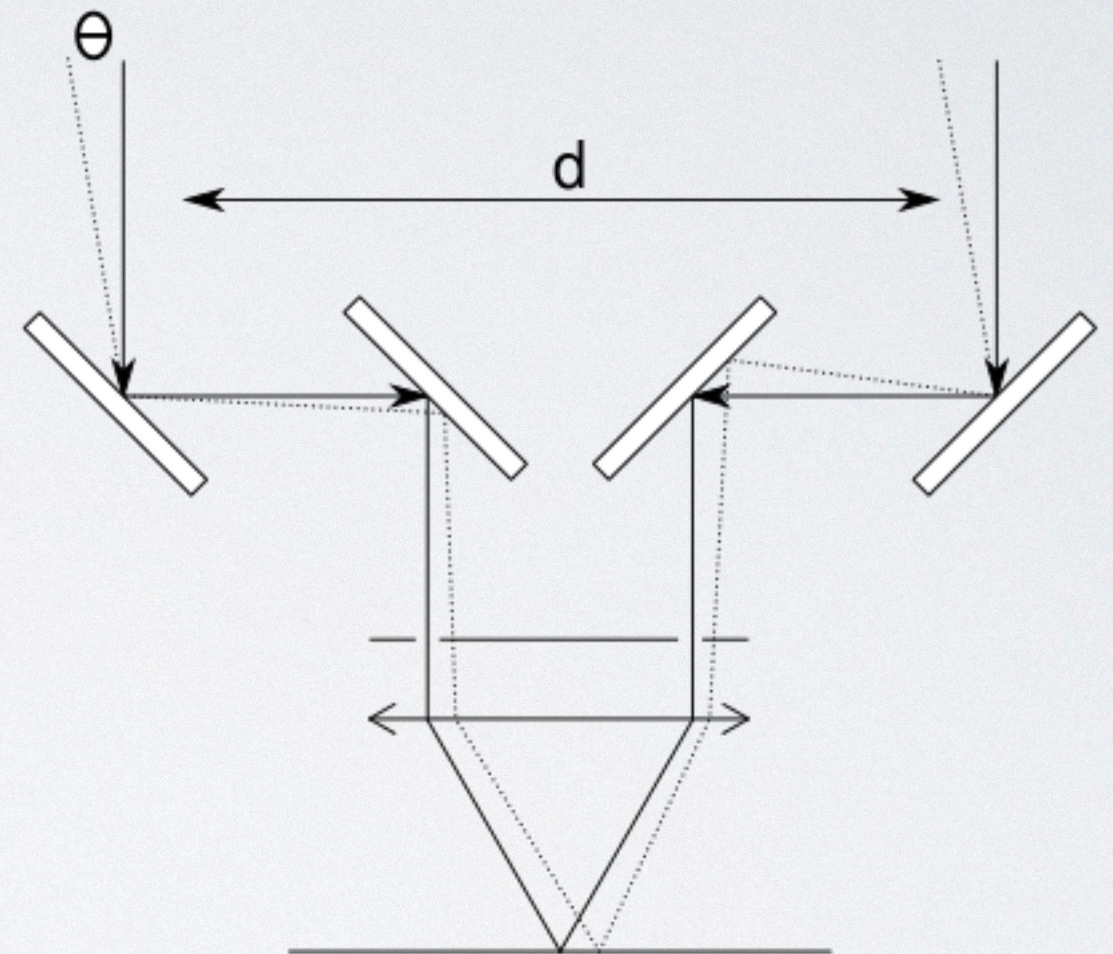
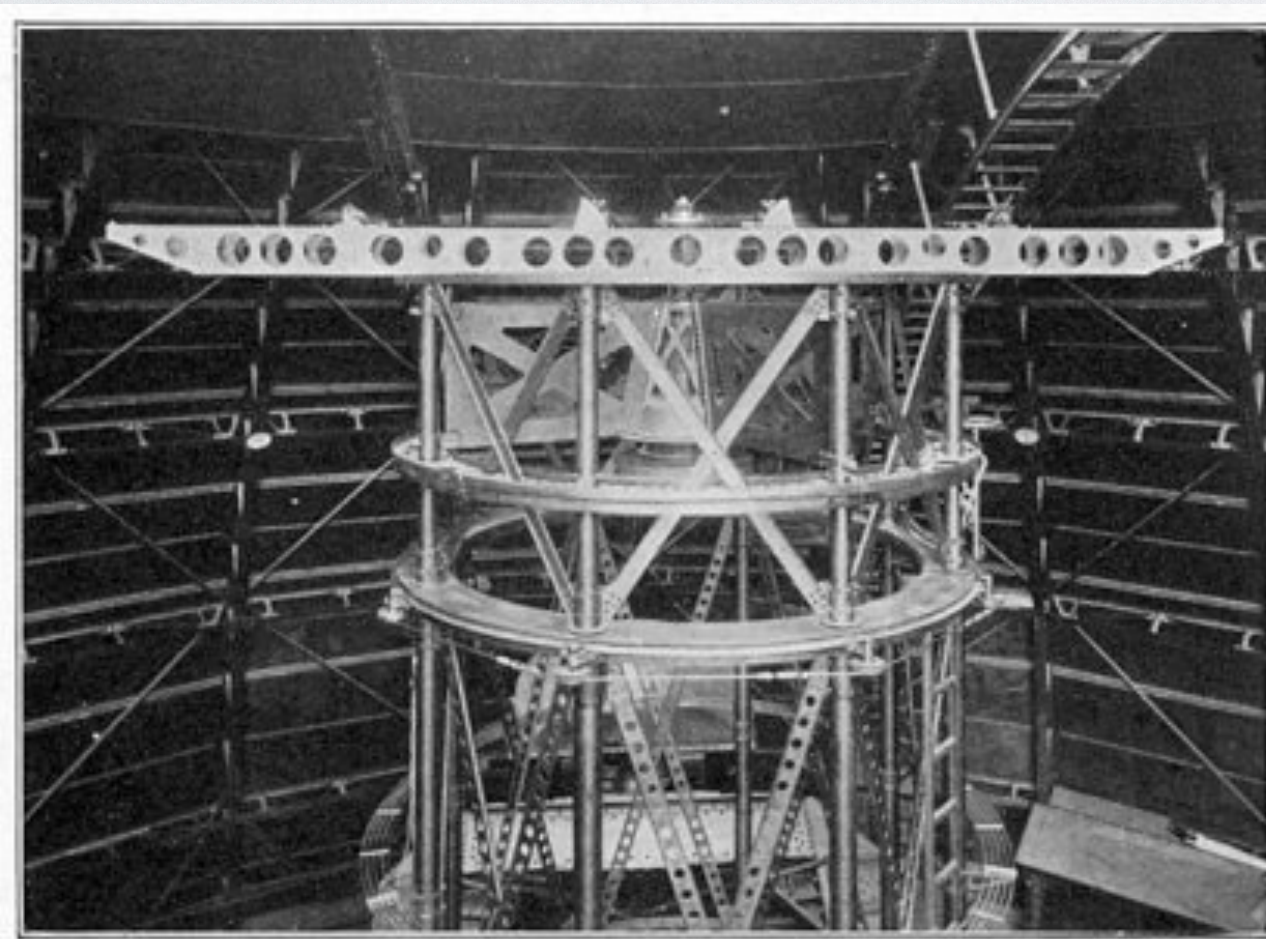
Michelson in 1881





# Early interferometers

Measurement of the diameter of Betelgeuse  
(by 'resolving out' the source - see later)

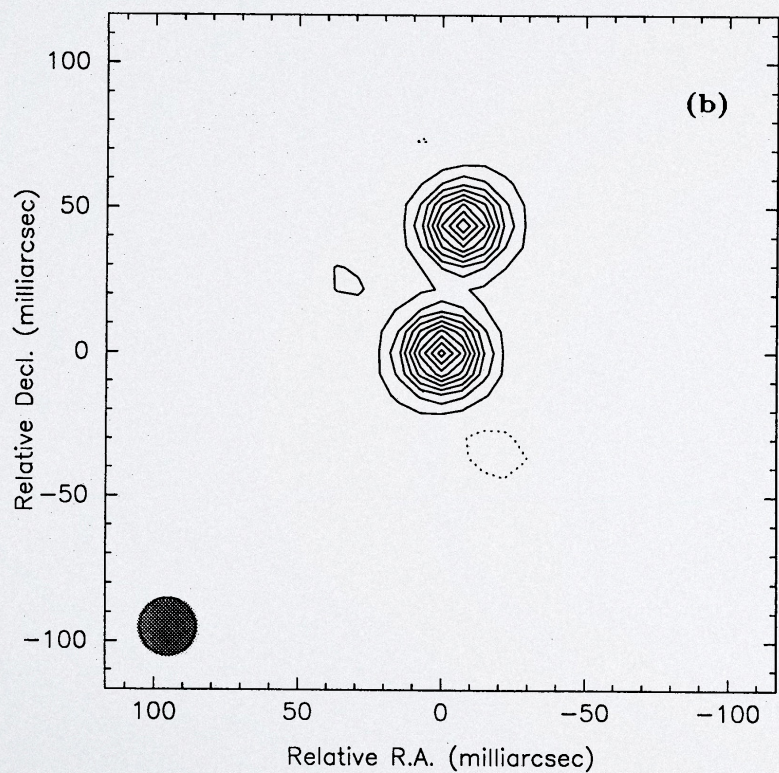
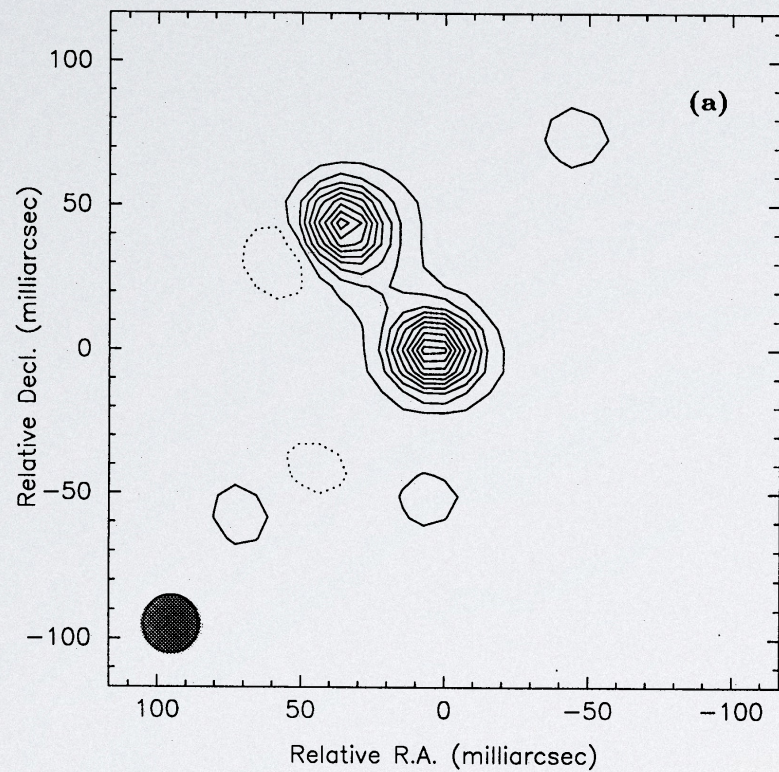




# Optical interferometry

Capella binary at two epochs

Cambridge!



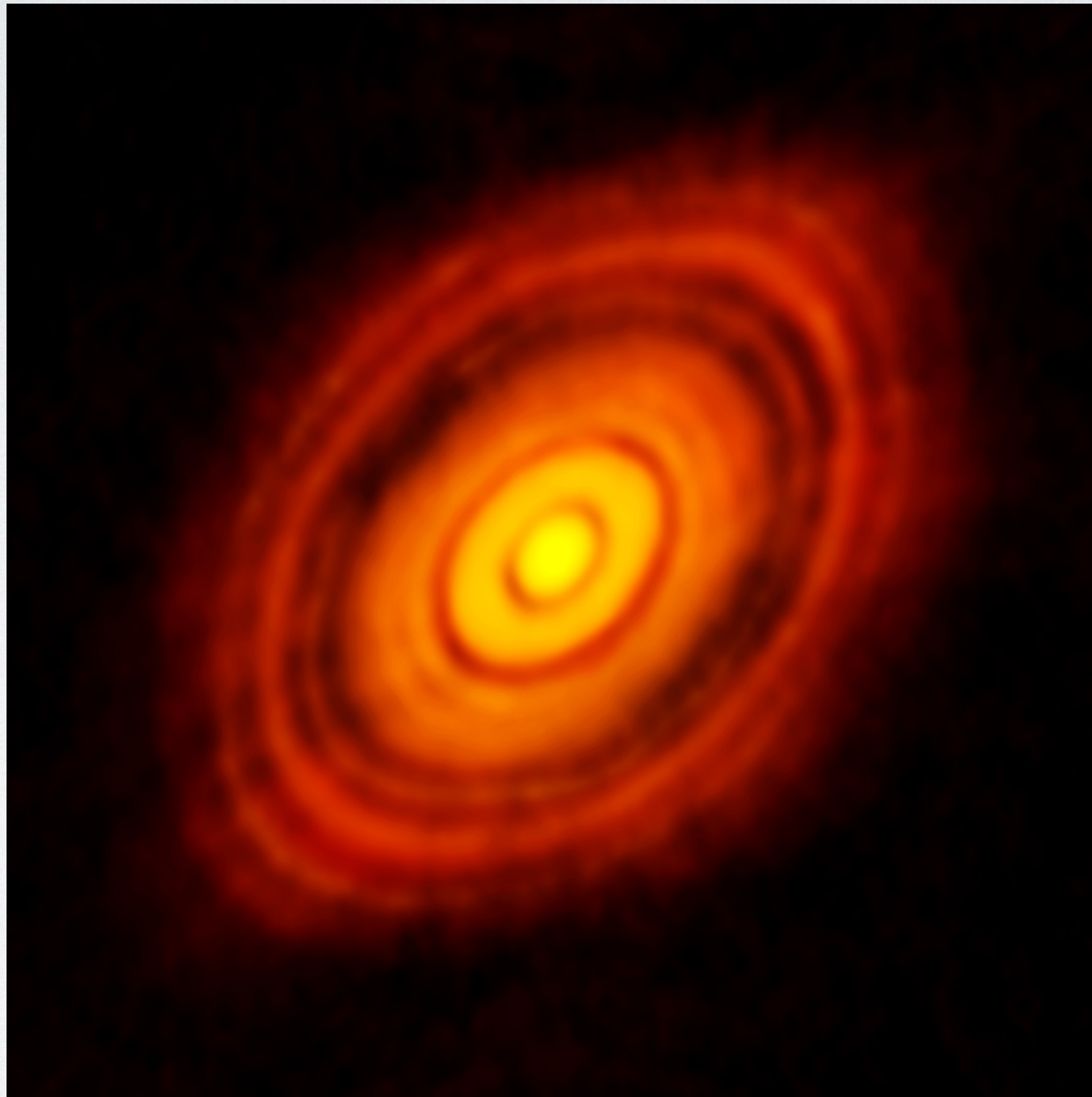


# Mid-IR interferometry



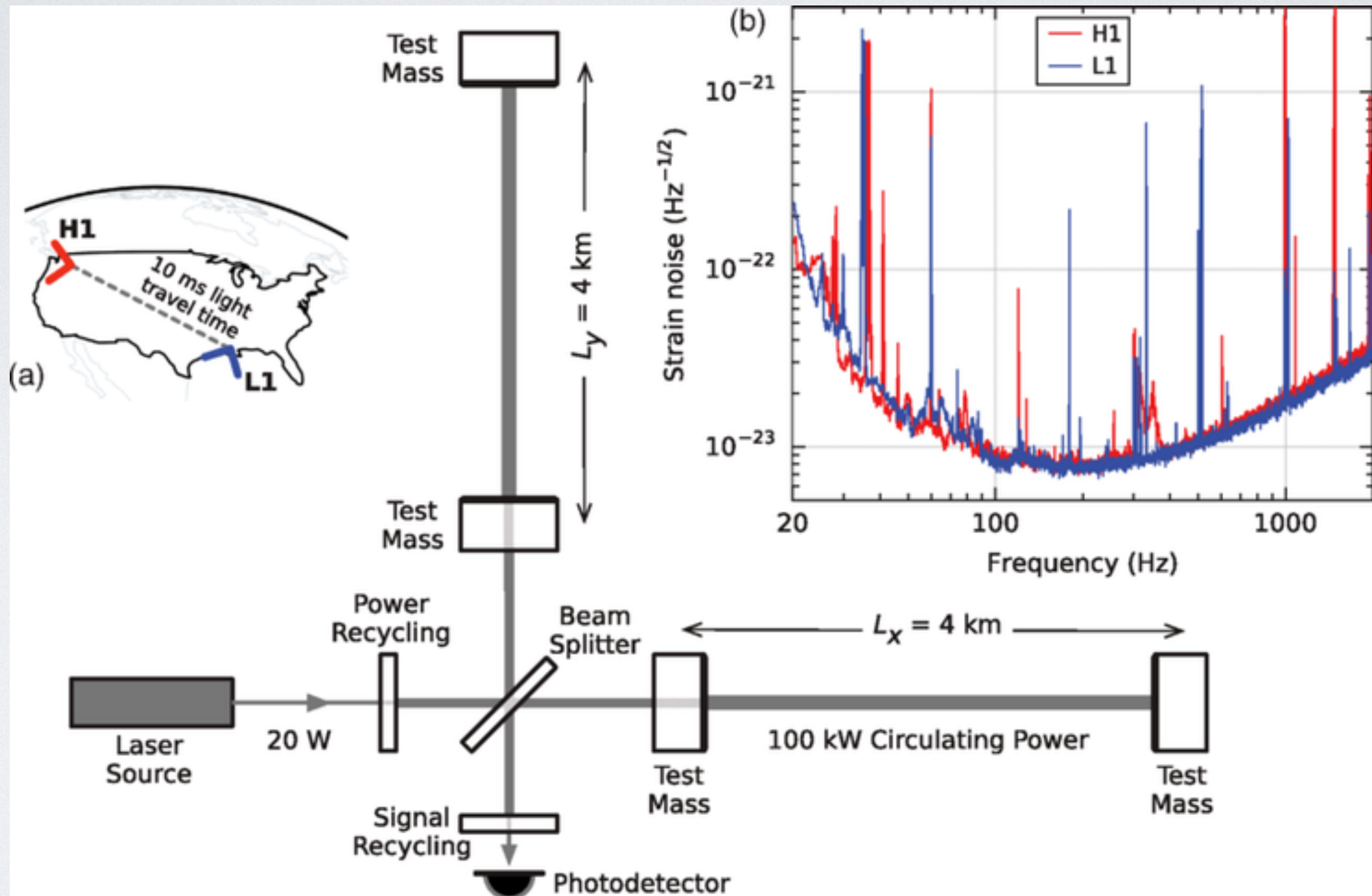


# Radio interferometry



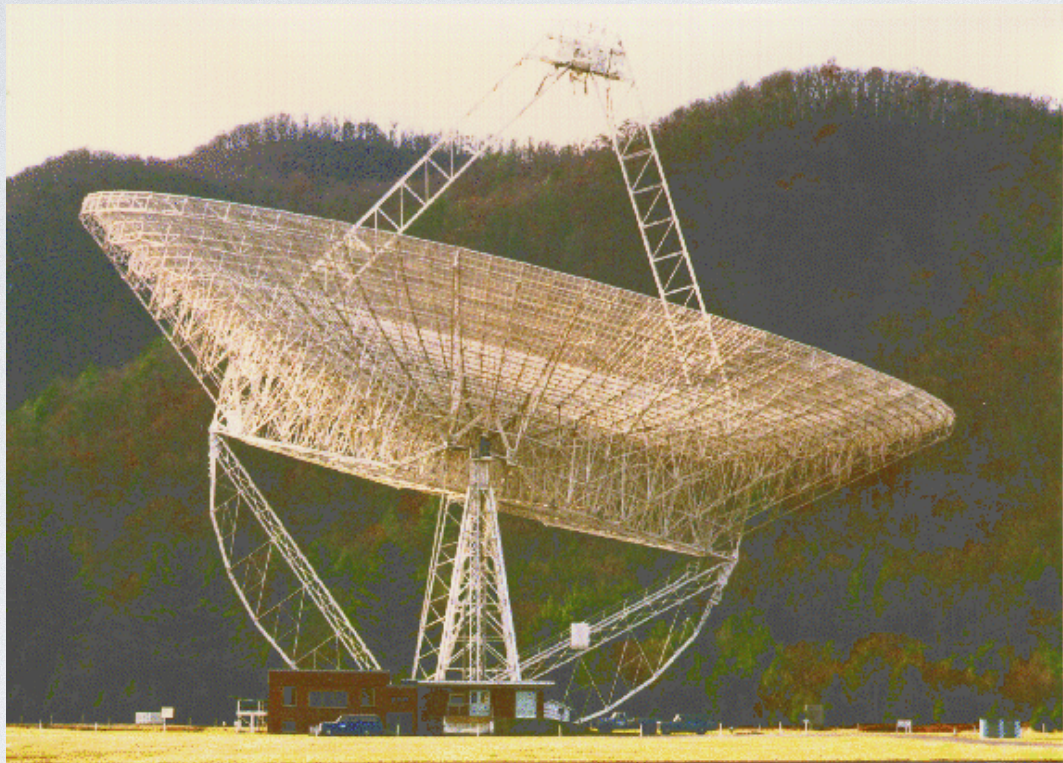


# Gravitational waves





# Why do interferometry?



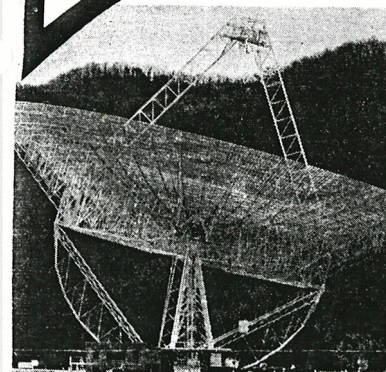
- Resolution  $1.22\lambda/D \rightarrow \lambda/(2b)$
- Dishes can only be so big



America's most powerful radio telescope **IS** ...

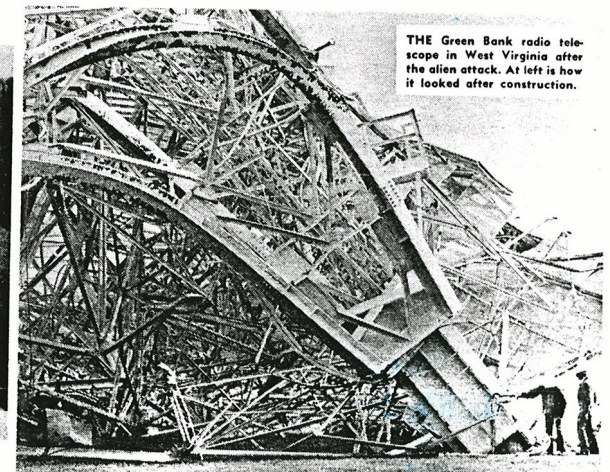
# ZAPPED!

... by hostile space aliens!



BEFORE ▲

▶ AFTER



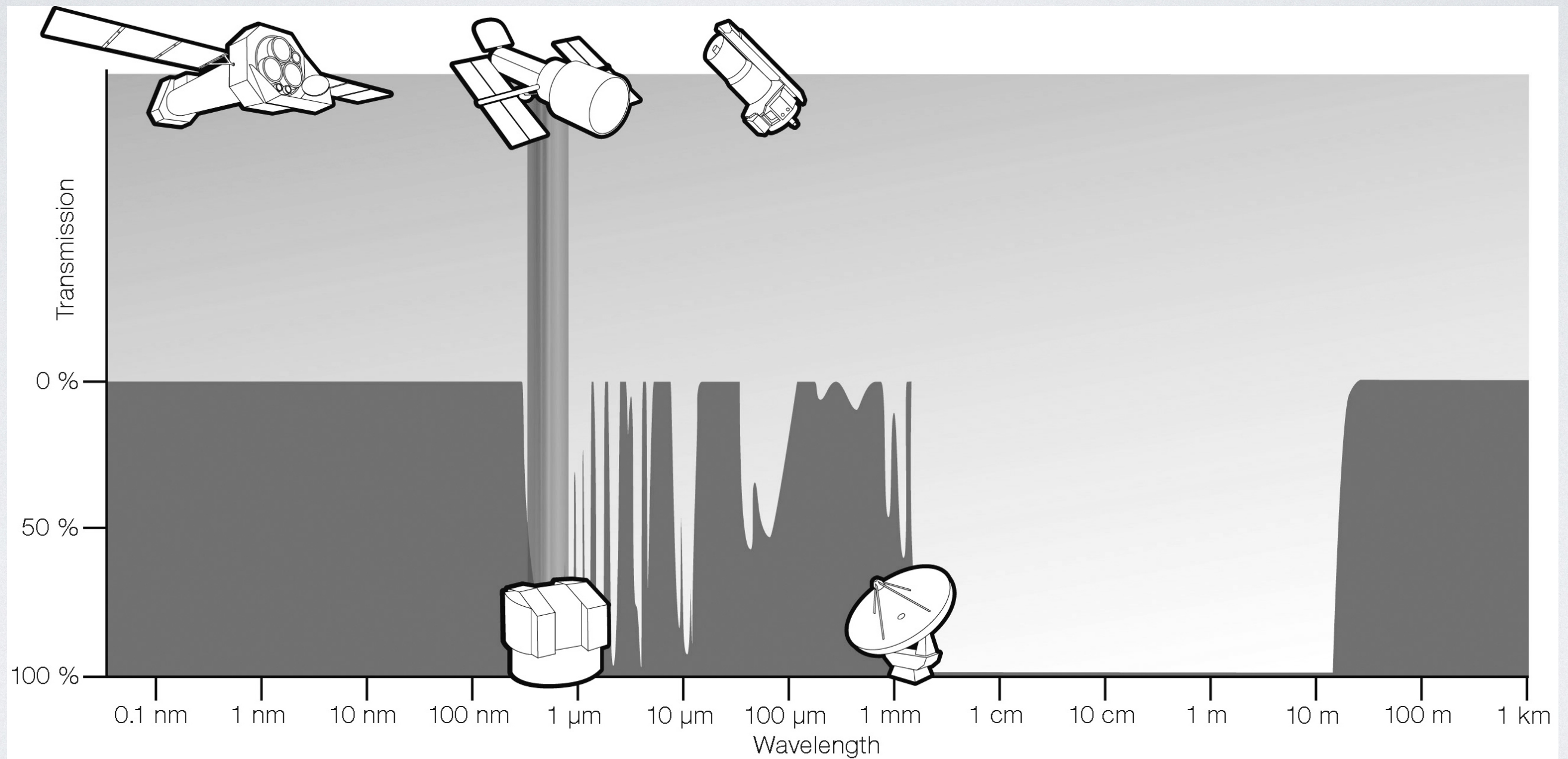
THE Green Bank radio telescope in West Virginia after the alien attack. At left is how it looked after construction.

Space aliens zapped the enormous radio telescope at Green Bank, W. Va., with a powerful laser to keep scientists from monitoring their activities in the northern hemisphere! That's the claim of Swiss astronomer Peter Voisard, who says the incident

shockwaves throughout the world's scientific community. But the handful of men who can talk about the Green Bank disaster with authority refused to describe the incident as anything more than "a mysterious zapping by extraterrestrials who wanted to mask their activity from mankind," Dr. Voisard said. "Any other explanation defies logic," he continued. "The steps are necessary to prove extraterrestrials topped the telescope at Green Bank," he said. "But let's wait until all the evidence is in. Then we can take whatever steps are necessary to



# Windows for astronomy





# Interferometry

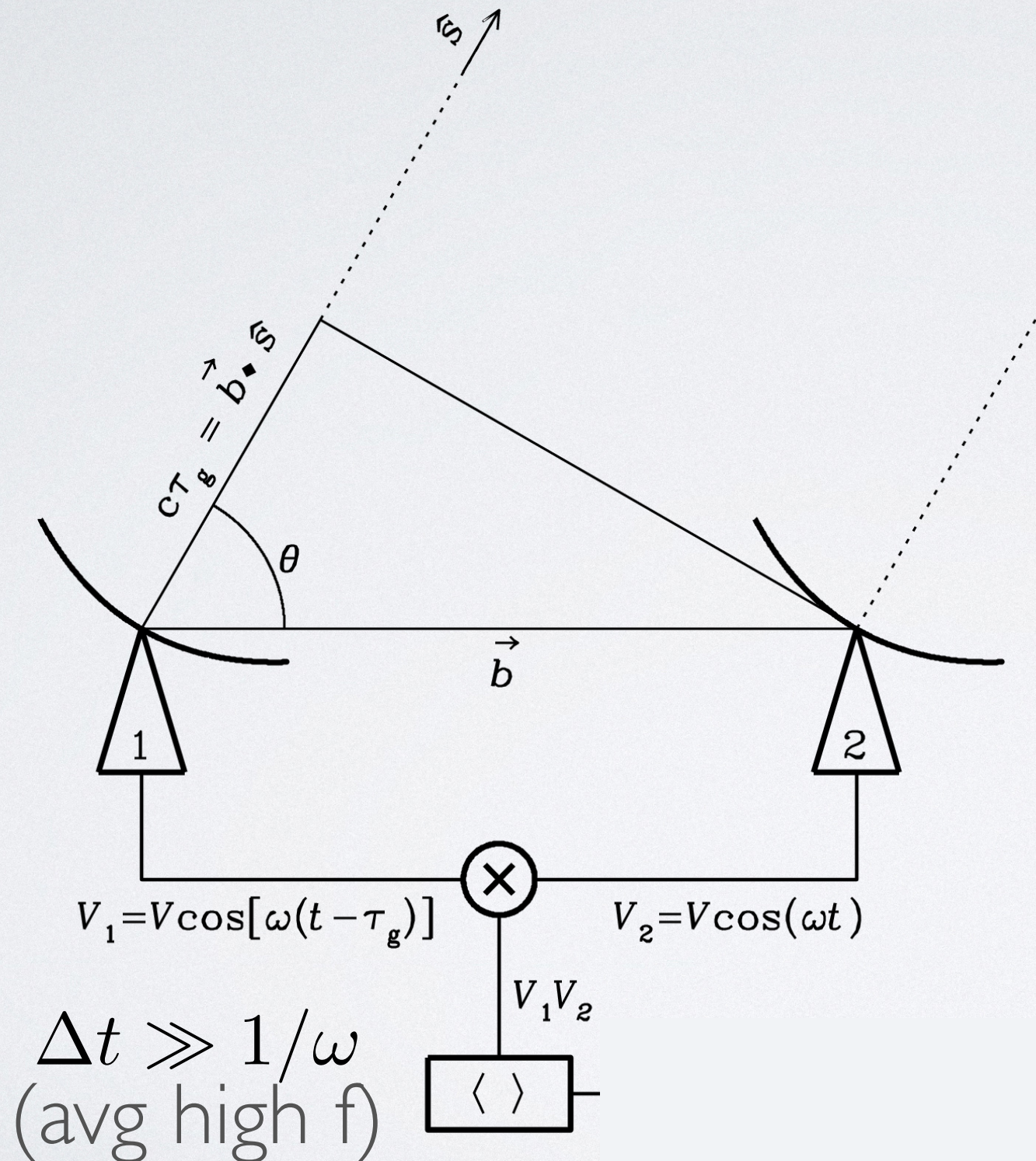
Jansky Very Large Array, New Mexico



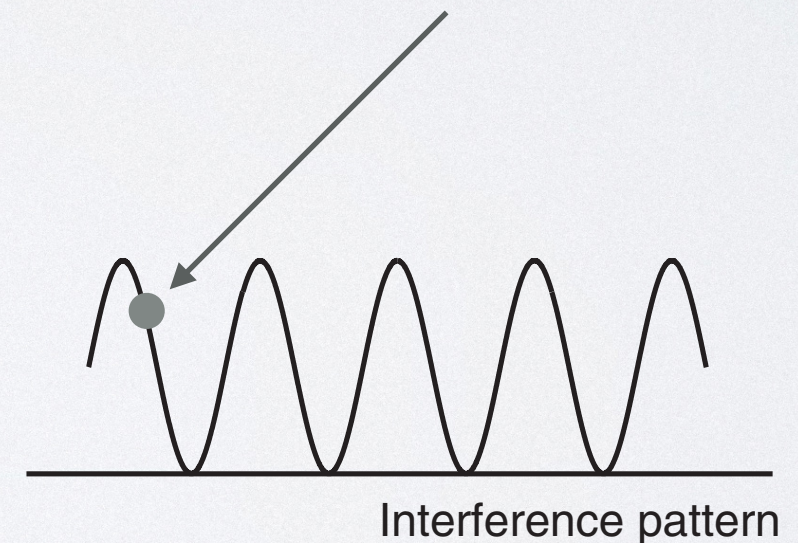


# Basic interferometer

response to a monochromatic source



$$\begin{aligned}
 R_C &= (V^2/2) \cos(\omega\tau_g) \\
 &= (V^2/2) \cos\left(2\pi \frac{\mathbf{b} \cdot \hat{\mathbf{s}}}{\lambda}\right) \\
 &\text{(i.e. a number)}
 \end{aligned}$$

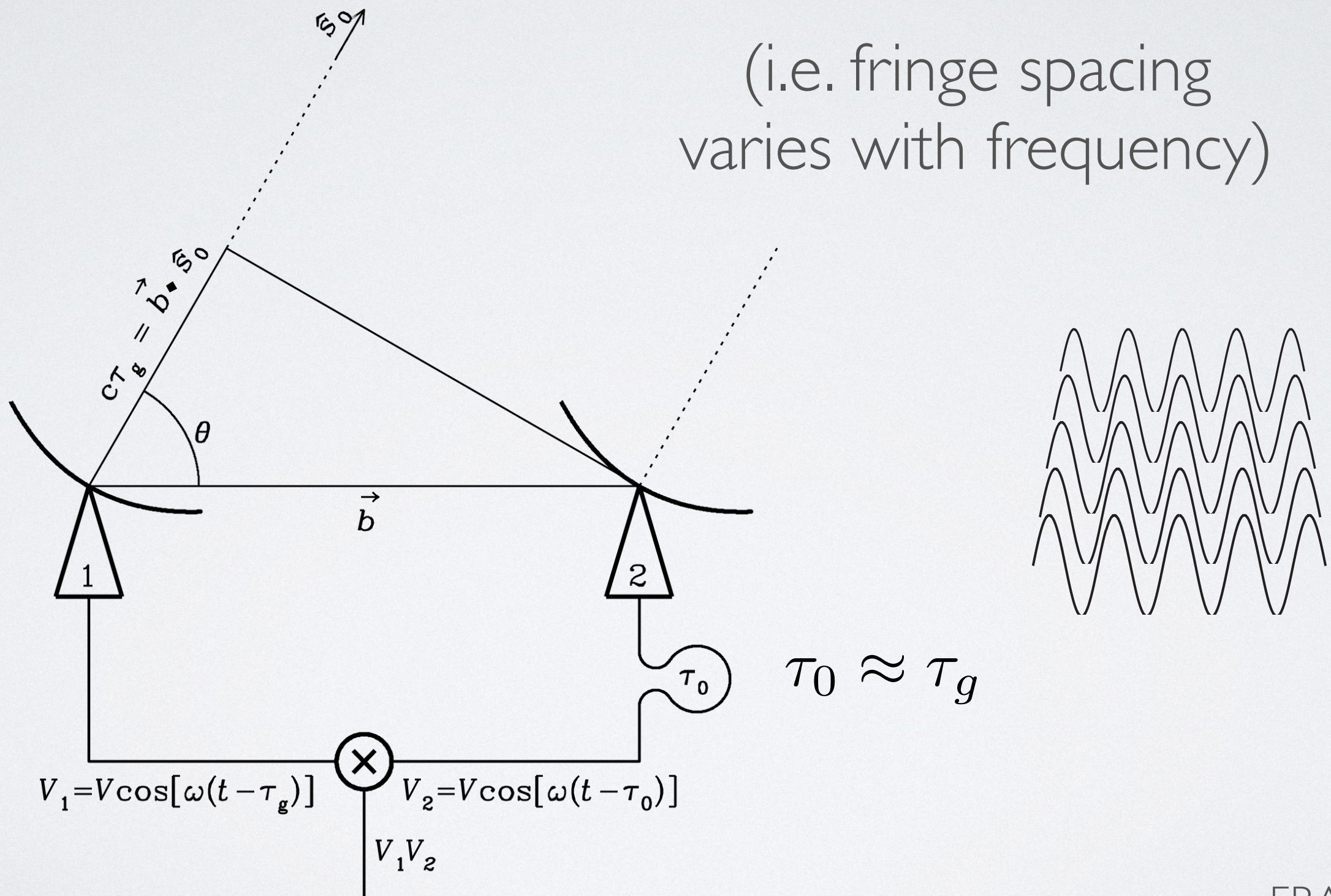




# Basic interferometer

finite bandwidth - add delay to "point" phase center

(i.e. fringe spacing varies with frequency)





# Astrometry

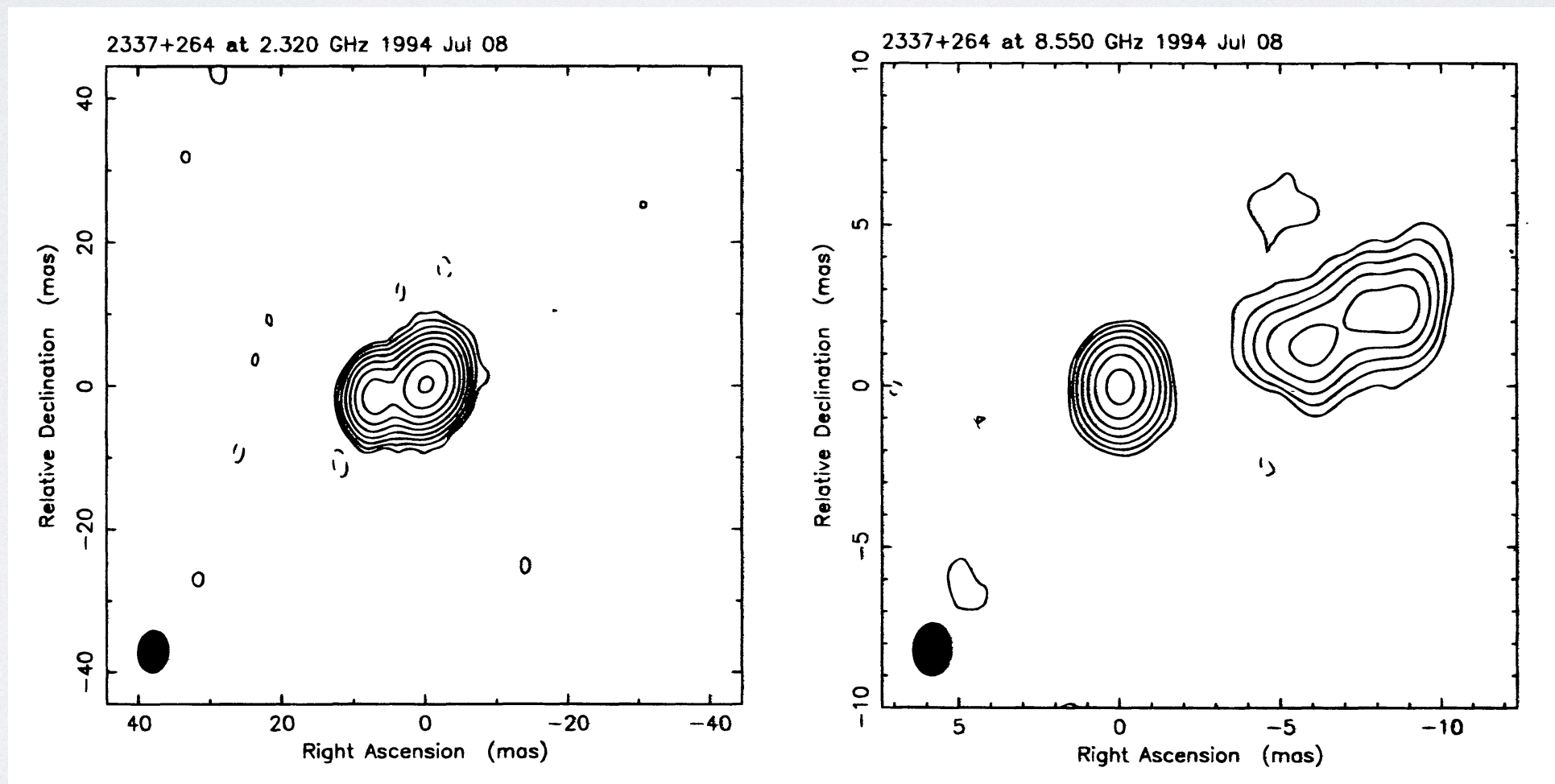
milli-arcsec precision - basis of ICRF

phase

$$\phi = 2\pi \frac{b \cos \theta}{\lambda}$$

$$d\phi/d\theta = 2\pi \frac{b \sin \theta}{\lambda}$$

$$b \sin \theta \gg \lambda$$

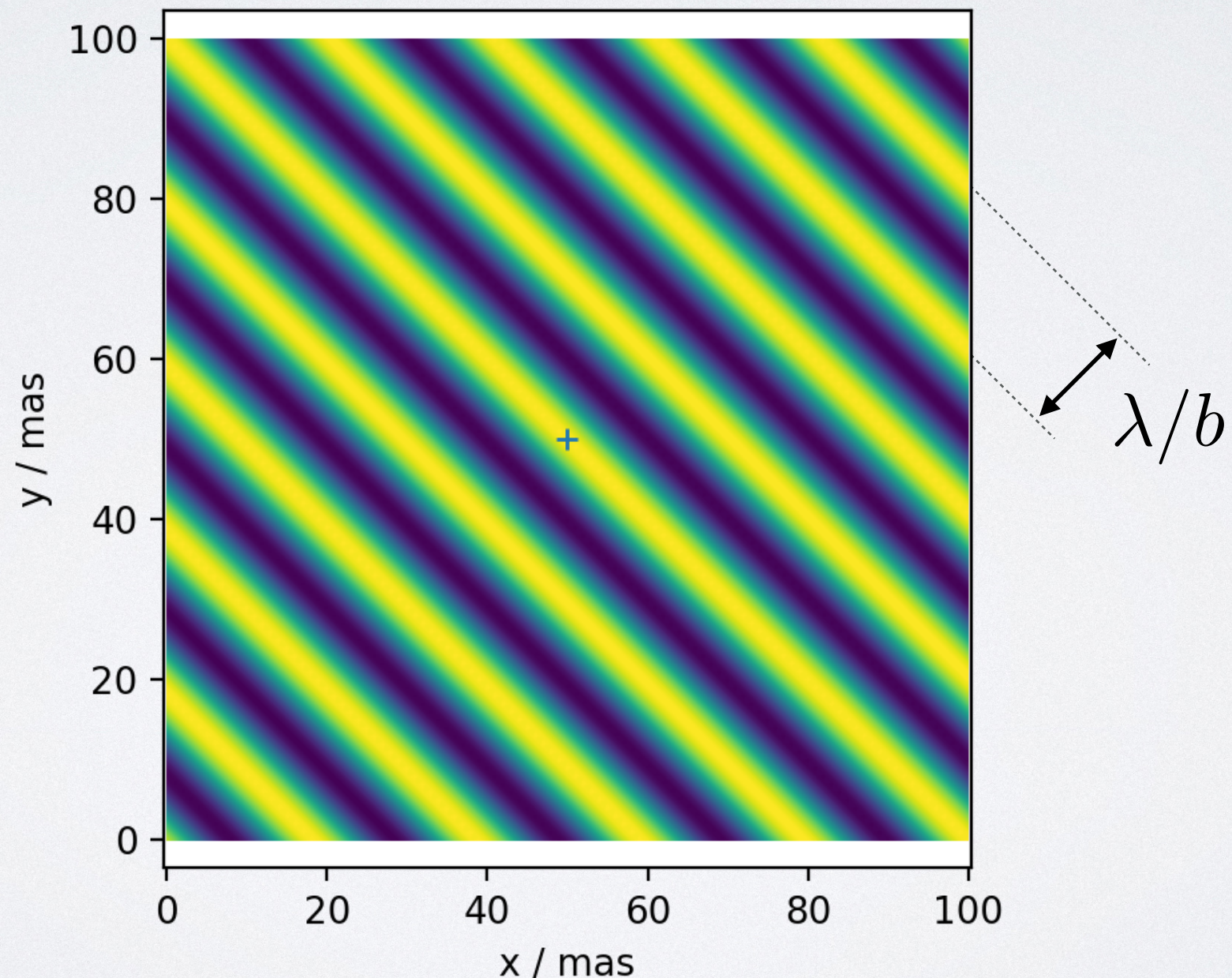




# Basic interferometer

signal = sum of (sky image x fringe pattern on sky)

$$R_C = \int I(\mathbf{s}) \cos(2\pi \mathbf{b} \cdot \hat{\mathbf{s}} / \lambda) d\Omega \quad (\text{i.e. a number})$$

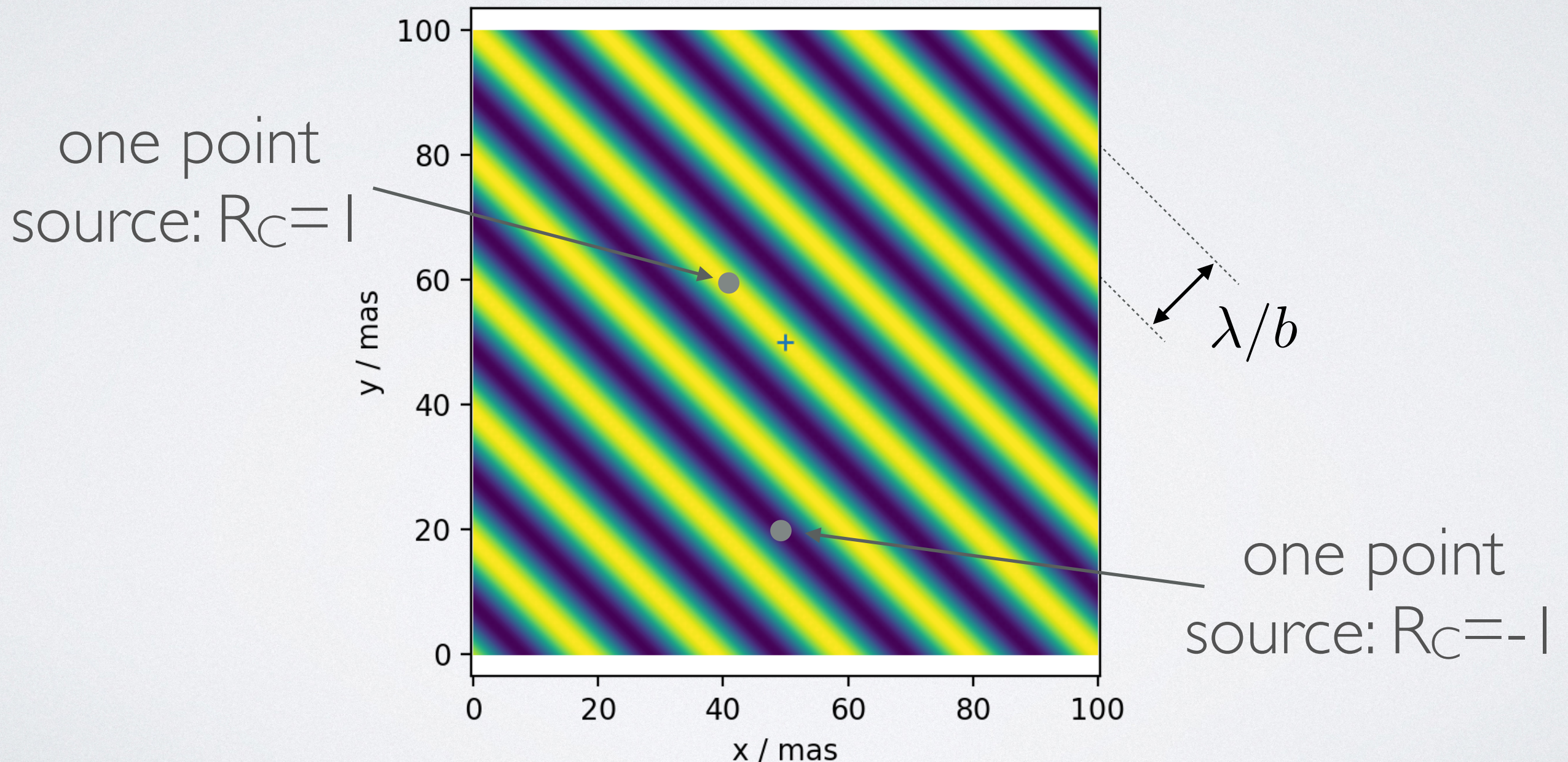




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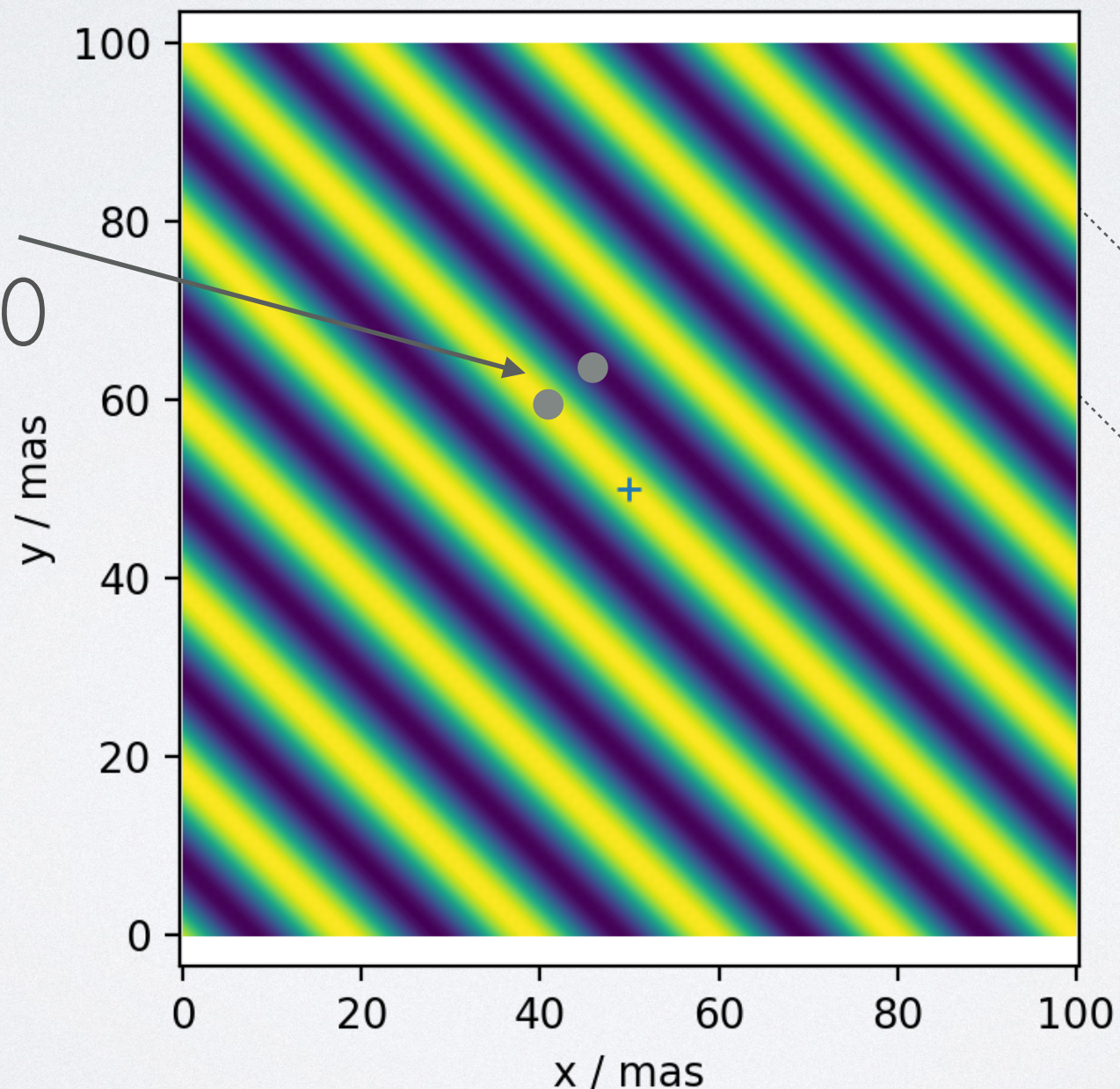


# Basic interferometer

signal = sum of (sky image x fringe pattern on sky)

$$R_C = \int I(\mathbf{s}) \cos(2\pi \mathbf{b} \cdot \hat{\mathbf{s}} / \lambda) d\Omega \quad (\text{i.e. a number})$$

two point sources:  $R_C = 0$



define “resolved”  
 $\Delta\theta = \lambda / (2b)$



# Basic interferometer

but odd component of a signal is invisible:  
second correlator with 90deg phase shift

$$R_S = \int I(\mathbf{s}) \sin(2\pi \mathbf{b} \cdot \hat{\mathbf{s}} / \lambda) d\Omega$$

now define complex visibility

$$V = R_C - iR_S = Ae^{-i\phi}$$

$$A = (R_C^2 + R_S^2)^{1/2}$$

visibility amplitude

$$\phi = \tan^{-1}(R_S/R_C)$$

visibility phase



# Basic interferometer

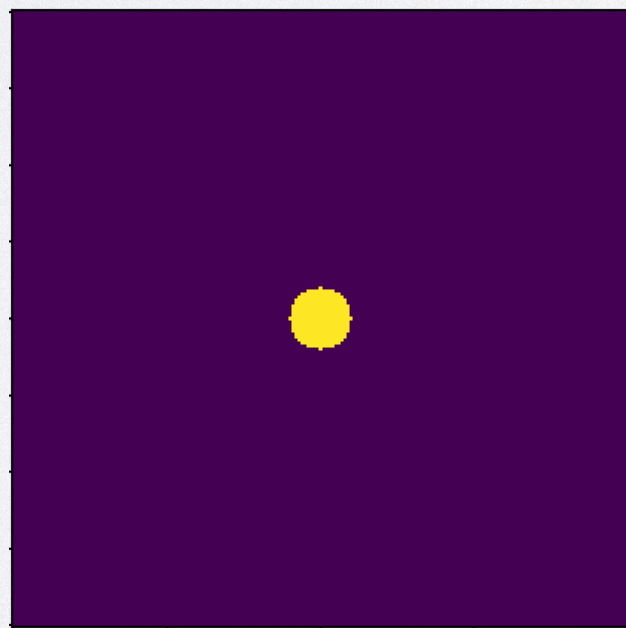
$$V = R_C - iR_S = Ae^{-i\phi}$$

$$V = \int I(\mathbf{s}) \exp(-i2\pi \mathbf{b} \cdot \hat{\mathbf{s}}/\lambda) d\Omega$$

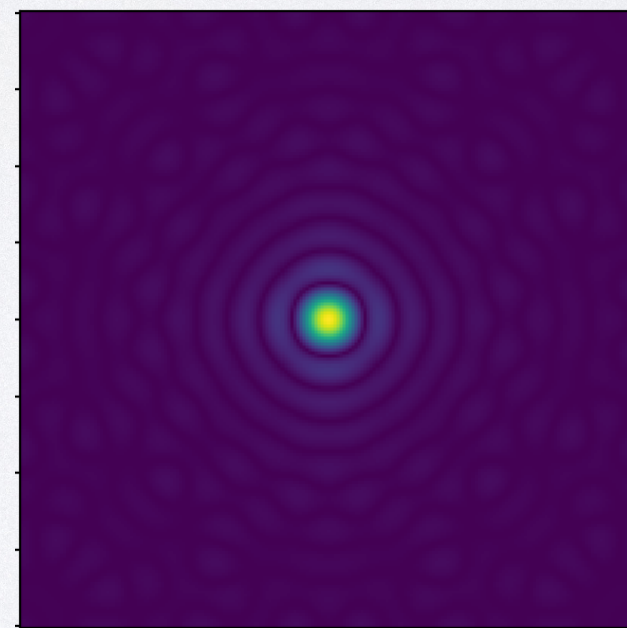
Van Cittert-Zernike theorem:

*Fourier transform of a far source is equal to its complex visibility*

image



'uv' plane  $u = b/\lambda$



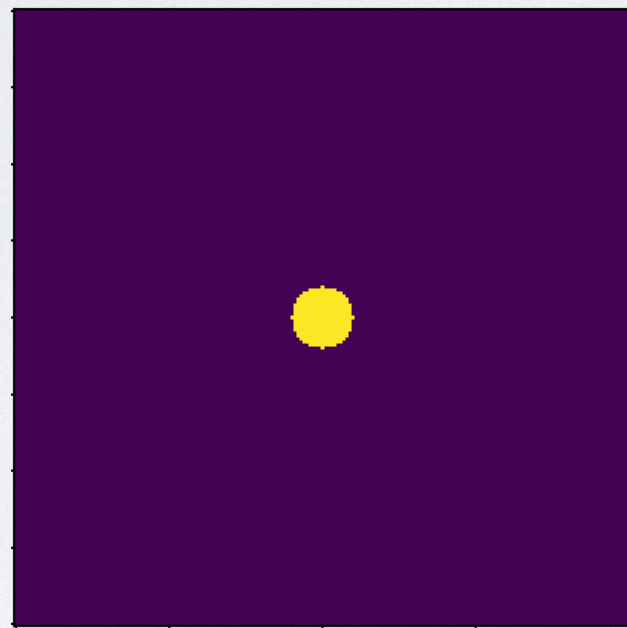
**i.e. sample  $V$  at a given  $u,v$  (which is set by baseline)**



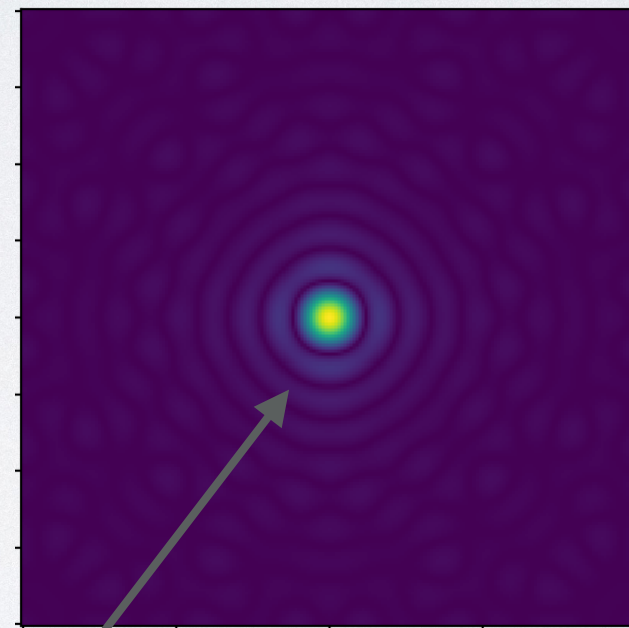
# Basic interferometer

i.e. sample  $V$  at a given  $u,v$  (which is set by baseline)

image



'uv' plane  $u = b/\lambda$

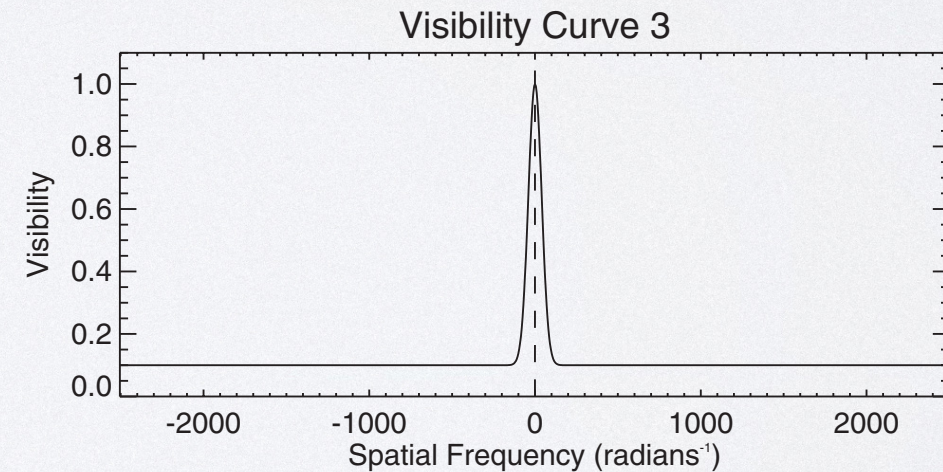
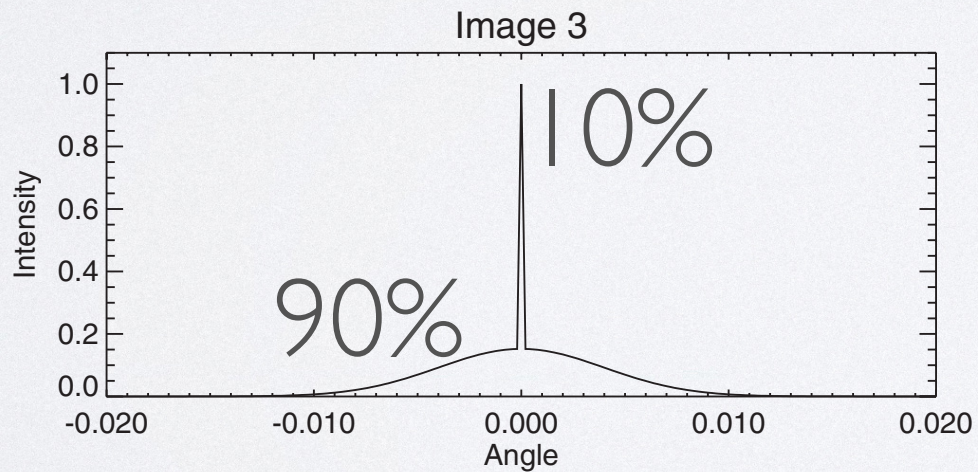
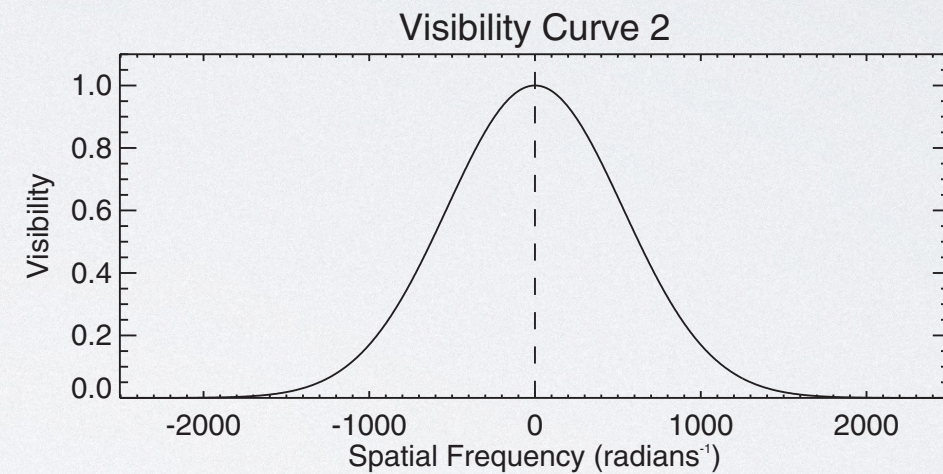
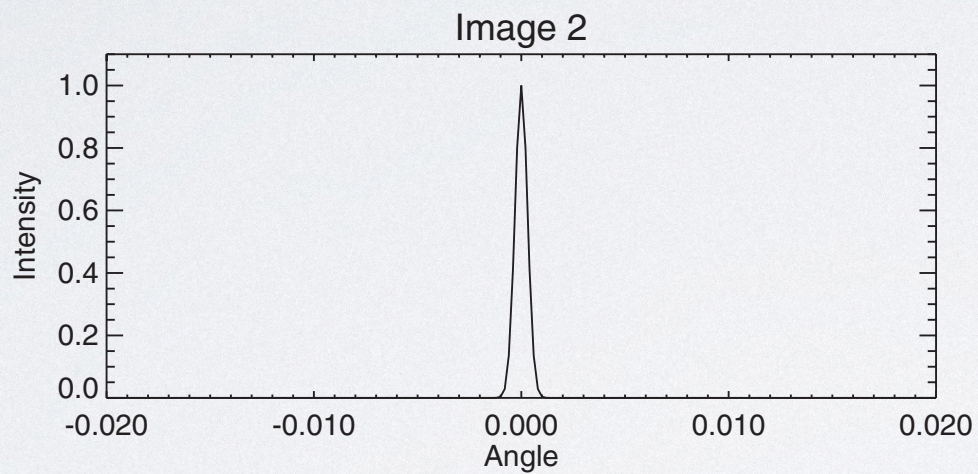
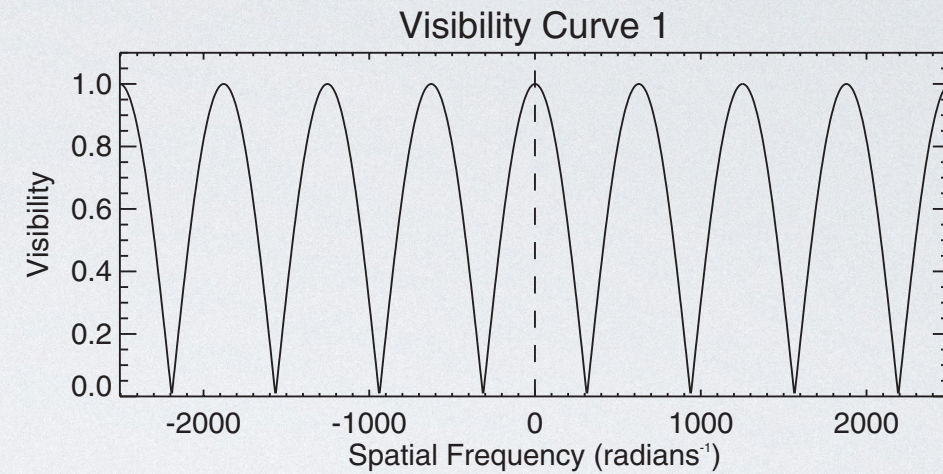
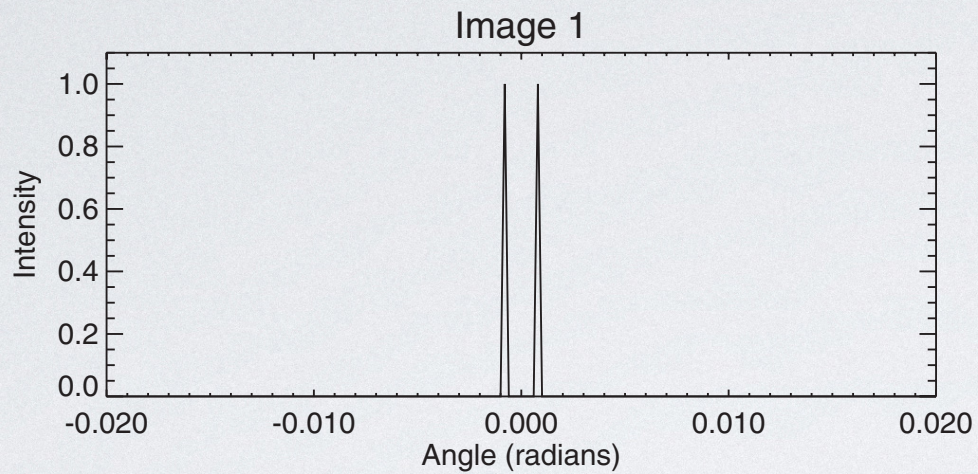


(+ phase)

each point corresponds to a  
baseline separation and orientation



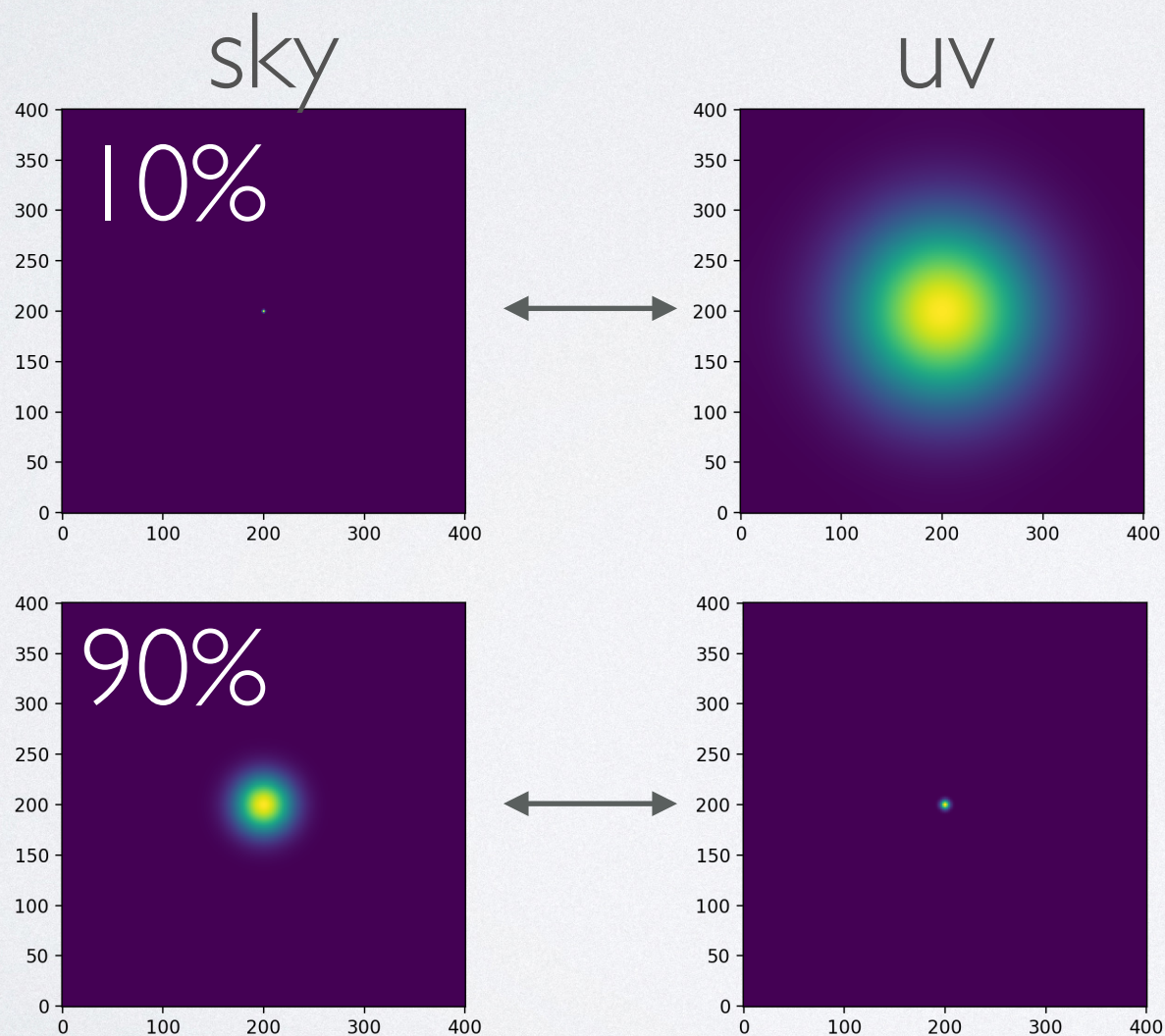
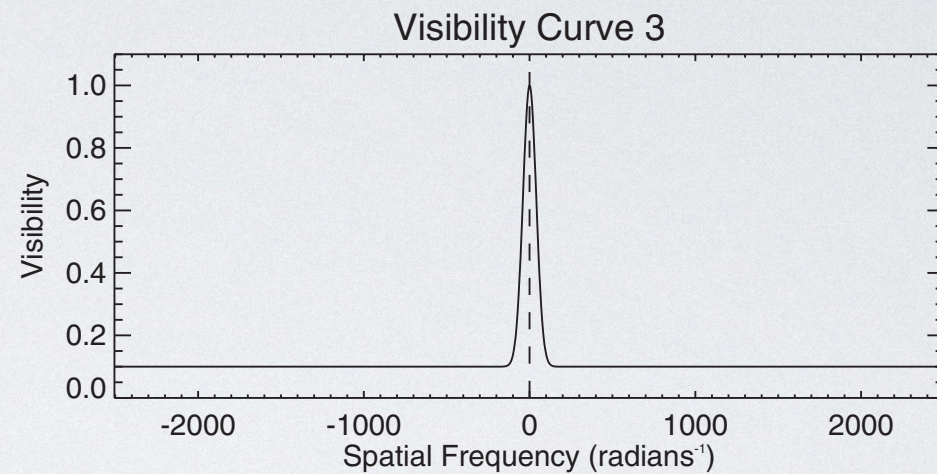
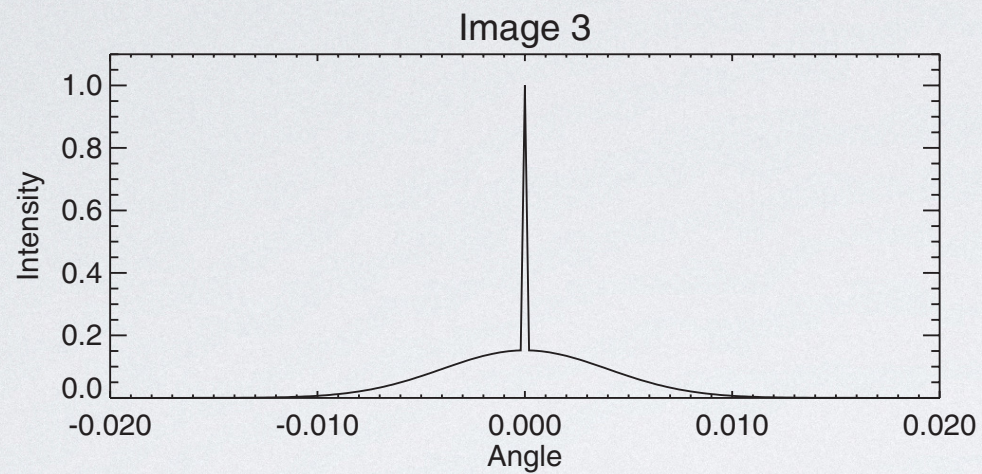
# Visibility curves



baseline ( $b/\lambda$ )

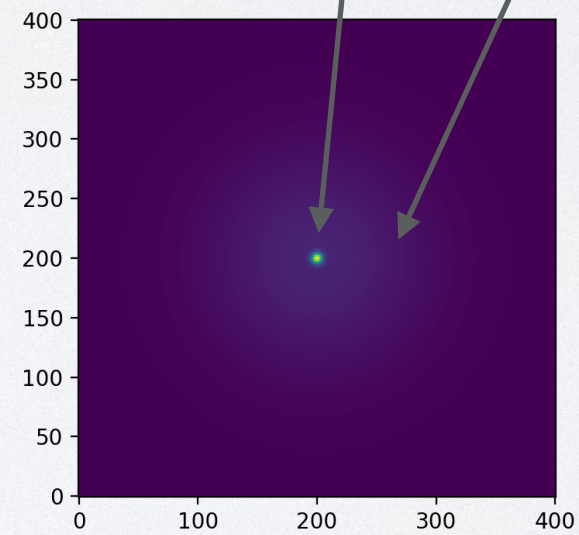


# Resolving out 'extended' flux



small b

large b



uv, both



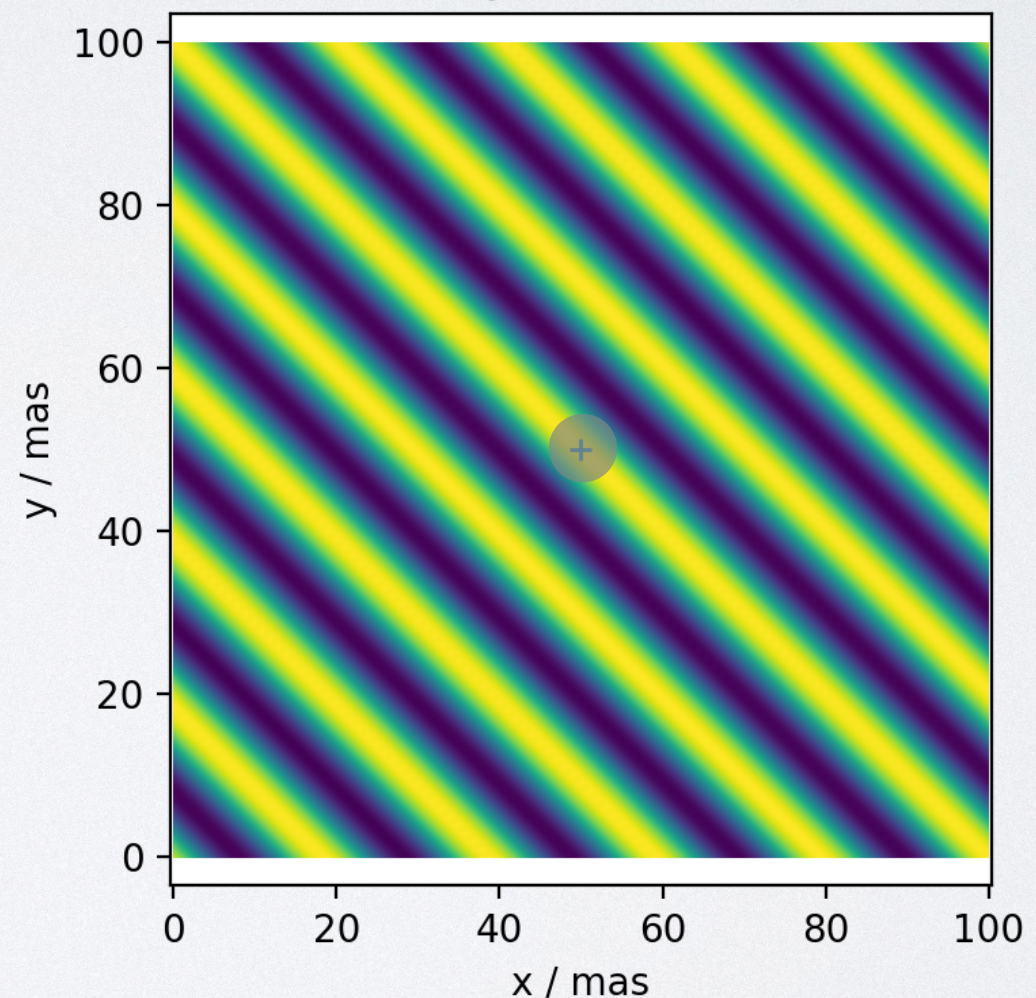
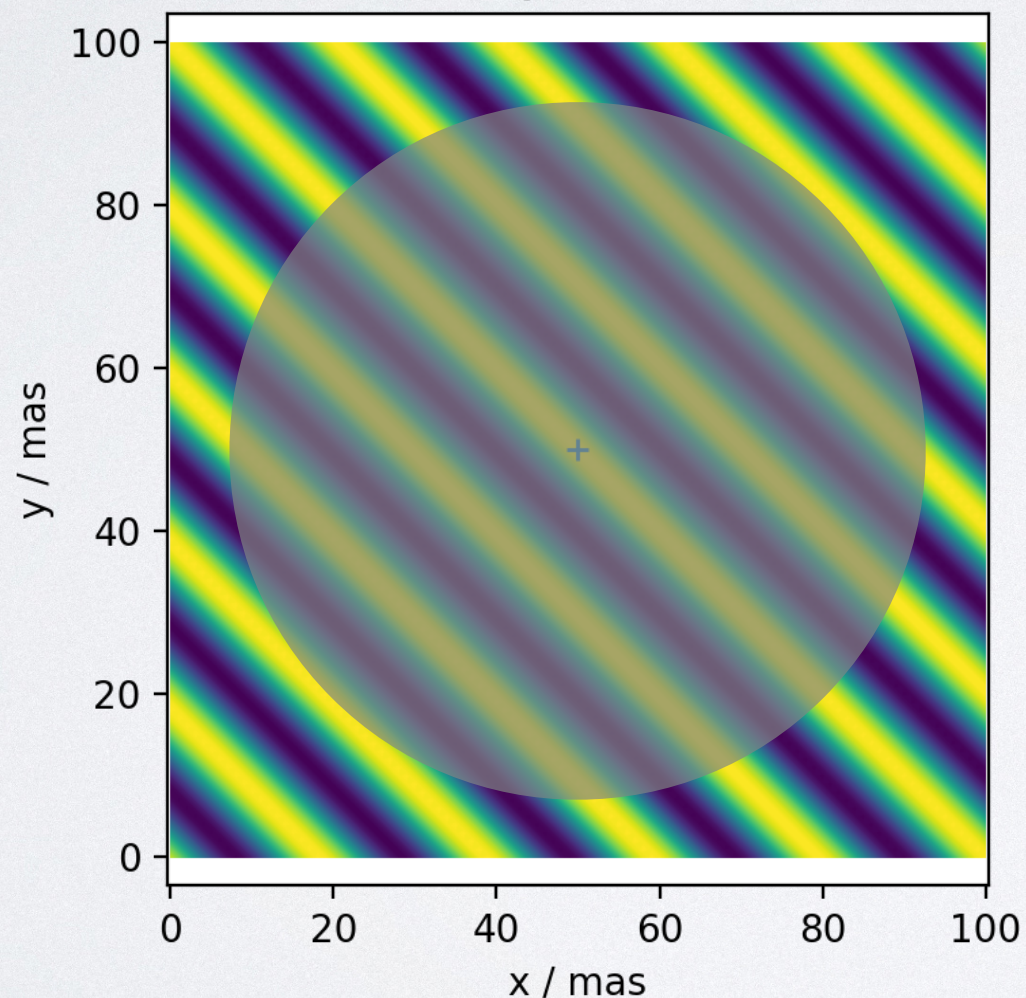
# Resolving out 'extended' flux

signal = sum of (sky image x fringe pattern on sky)

$$R_C = \int I(\mathbf{s}) \cos(2\pi \mathbf{b} \cdot \hat{\mathbf{s}} / \lambda) d\Omega \quad (\text{i.e. a number})$$

$$R_C \sim 0$$

$$R_C \sim 0.1$$



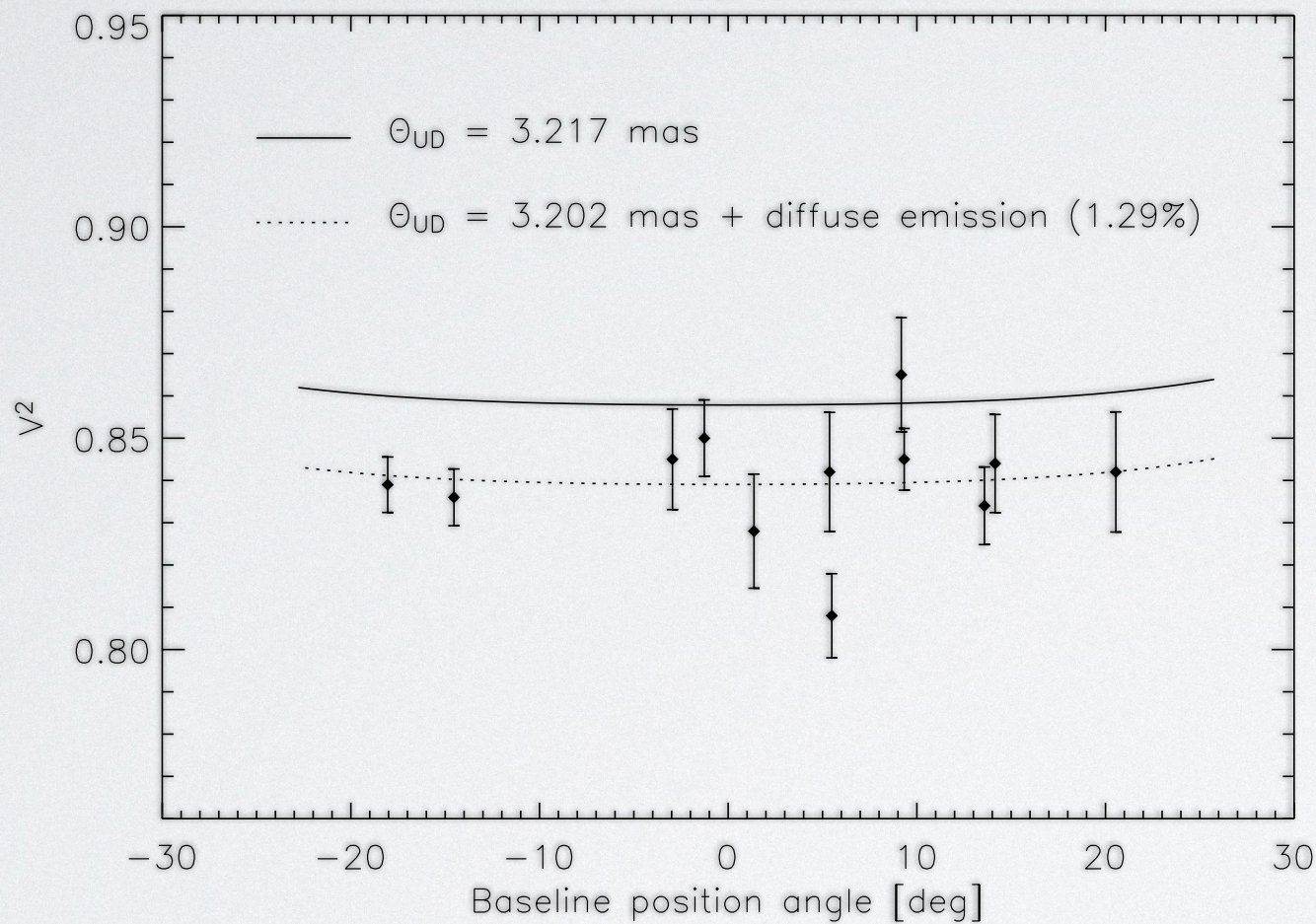
large source - averaging over many fringes



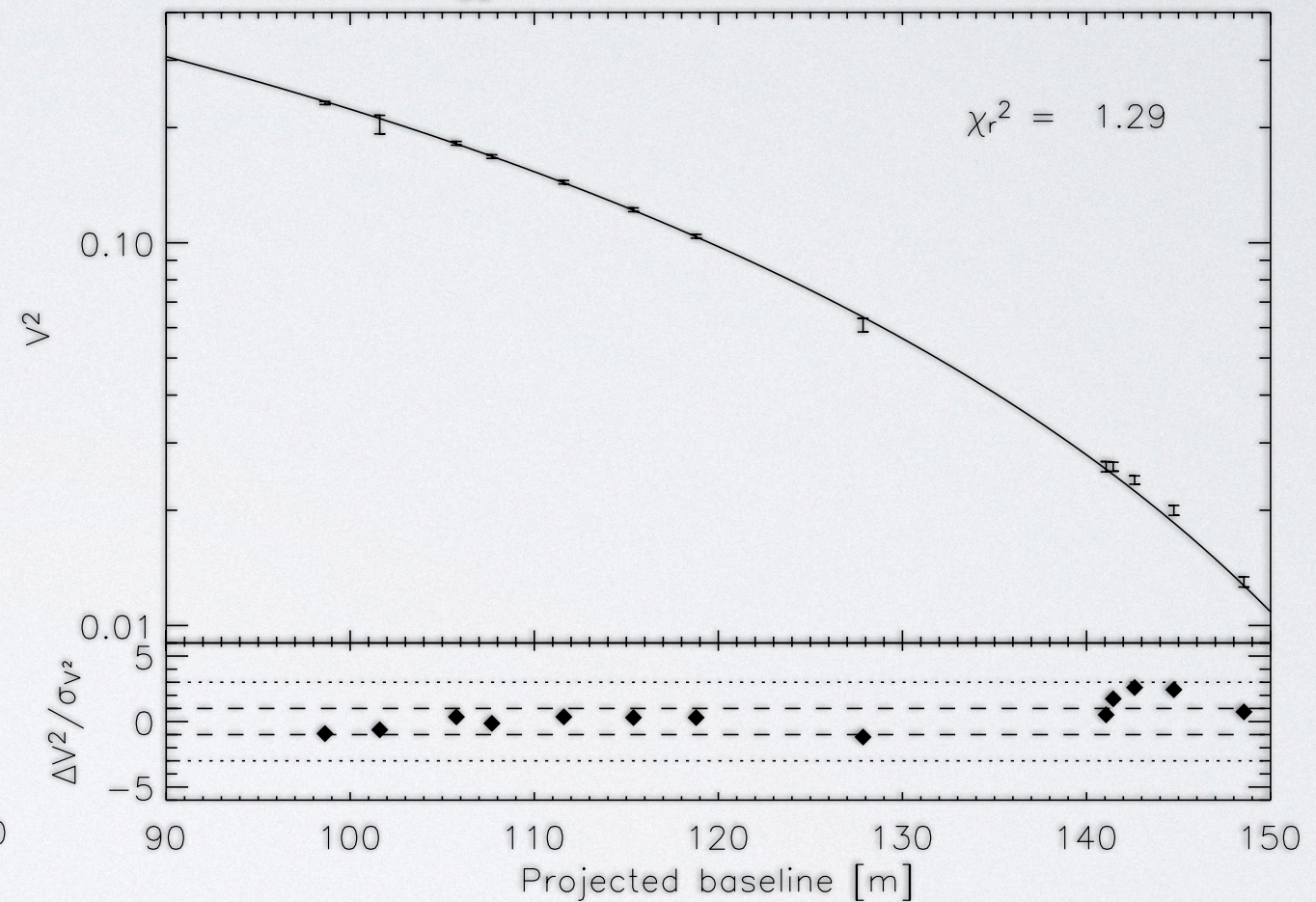
# Resolving out 'extended' flux

application to 'exo-Zodi' with CHARA

S1-S2 data



$\theta_{UD} = 3.218 \pm 0.005$  mas

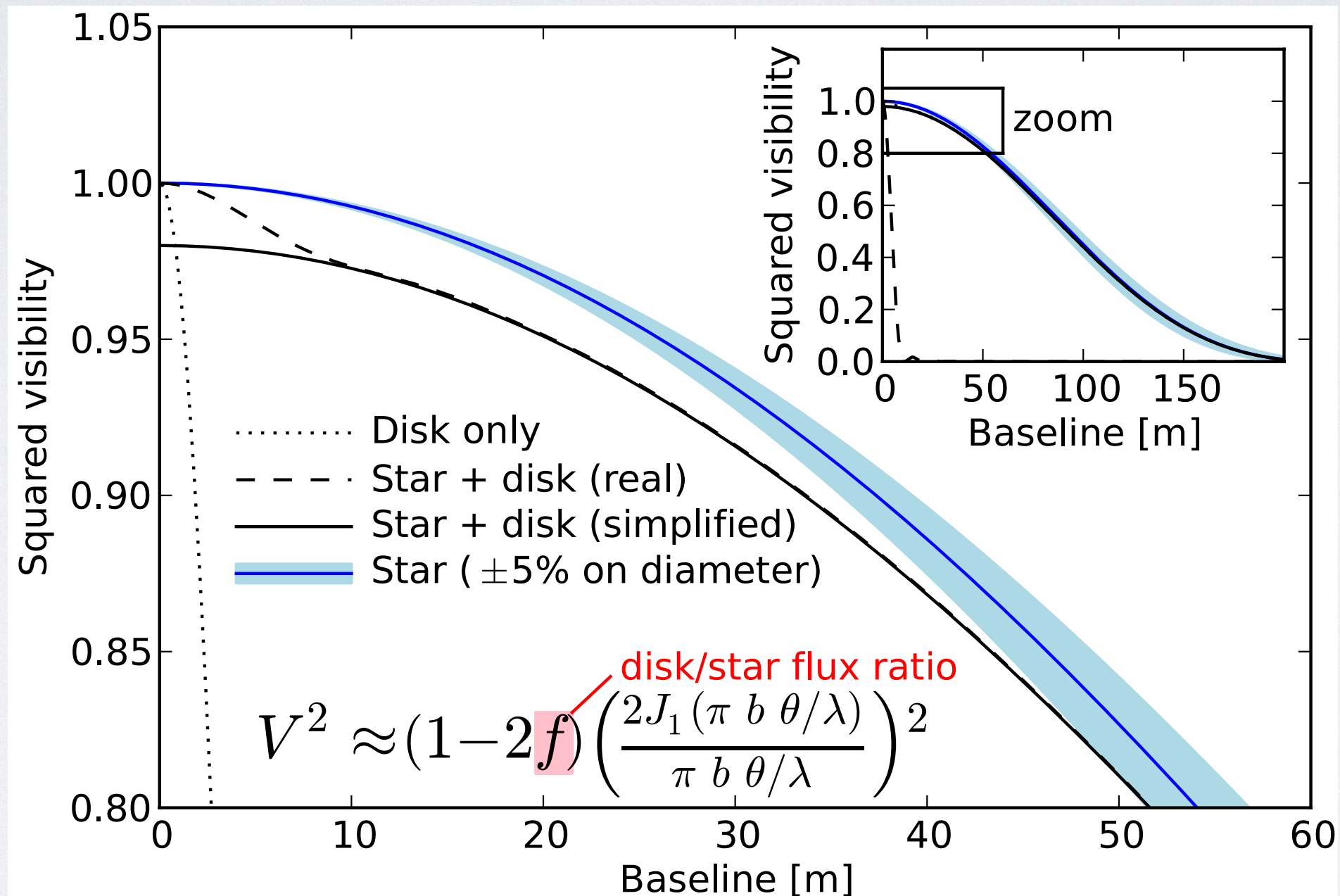


34m baseline



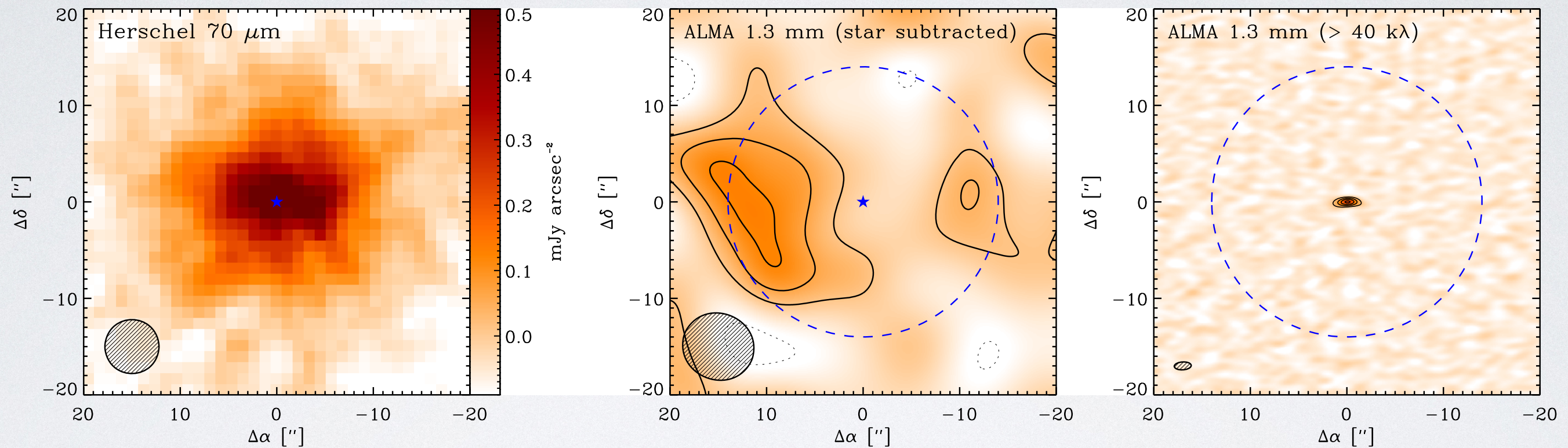
# Resolving out 'extended' flux

application to 'exo-Zodi' with CHARA



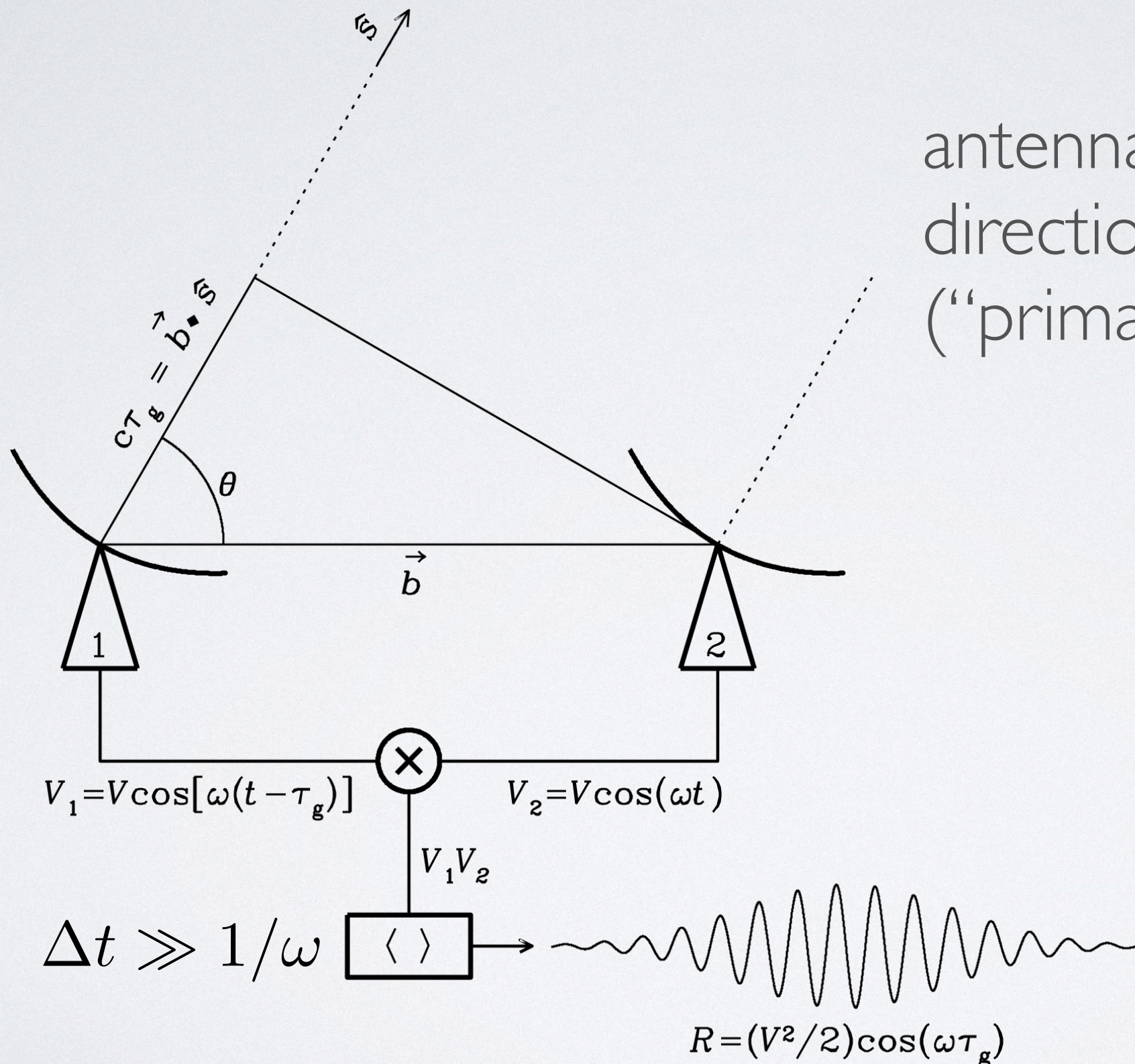


# Resolving out 'extended' flux





# Basic interferometer



antenna has directional response ("primary beam")

'fringe' for source moving past **S**



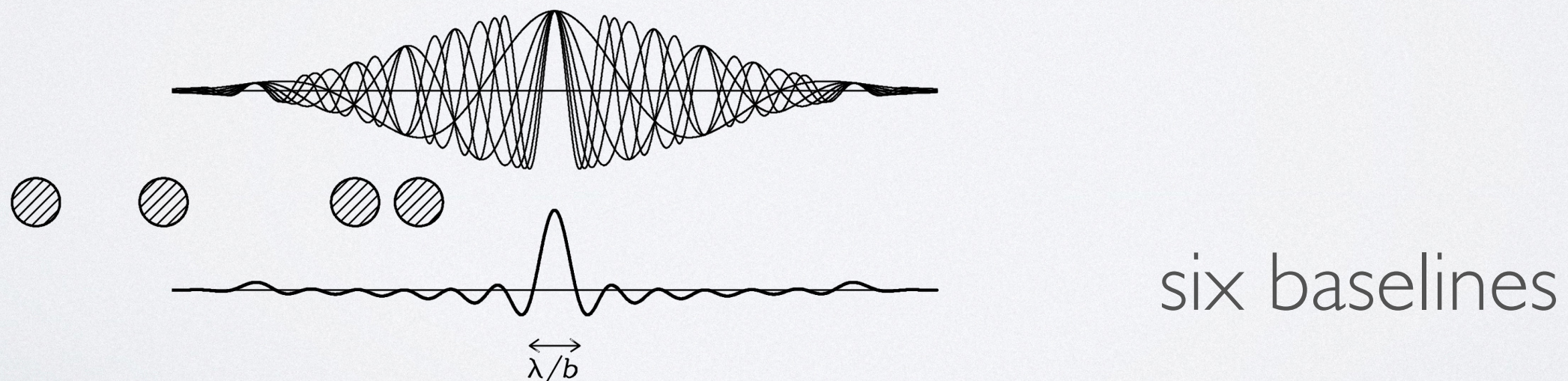
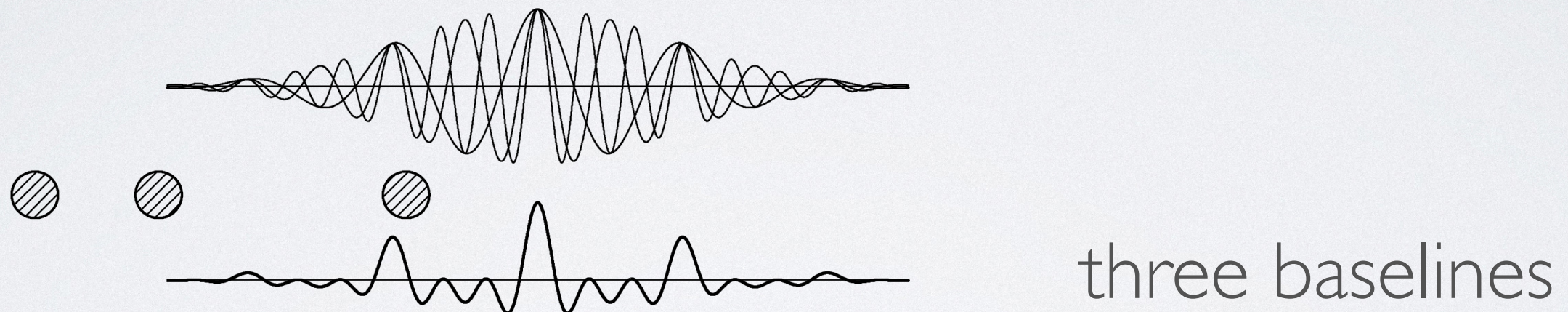
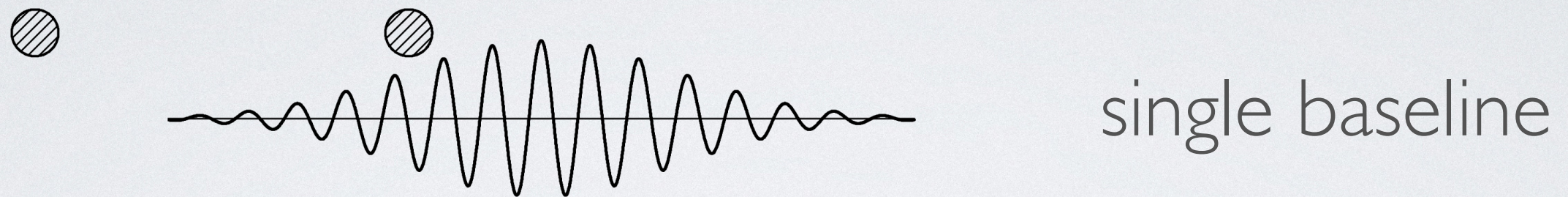
# Aperture synthesis

- Two element interferometer - imaging degenerate
- But,  $N$  antennas means  $N(N-1)/2$  unique baselines
- Goal: sample visibility at enough  $u,v$  points with many small antennas to “synthesise” an aperture of size  $u_{\max}, v_{\max}$
- Result: response to point source (“dirty beam”) is the average of the fringes for all baselines (more baselines, more Gaussian beam).



# Multiple baselines

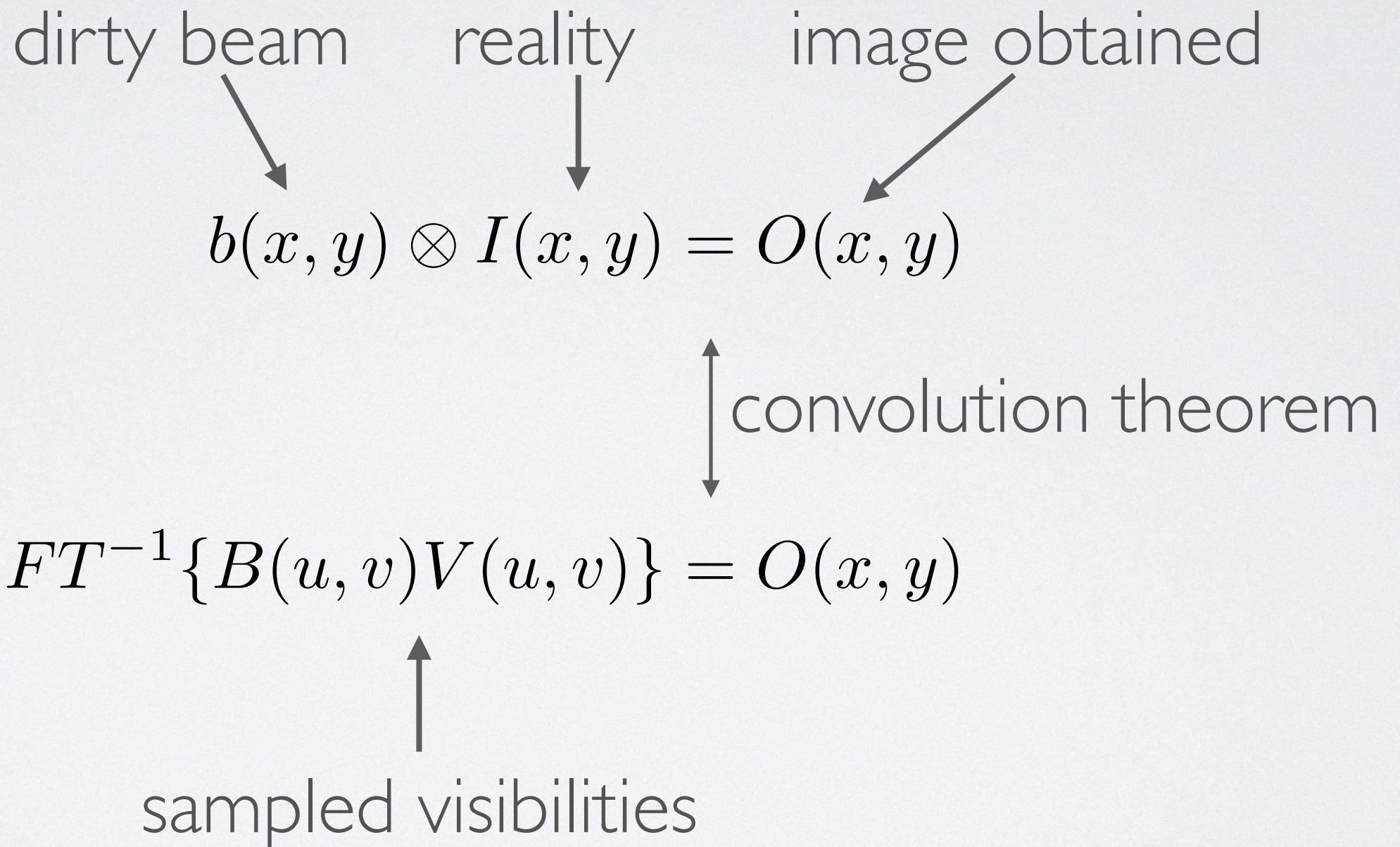
point-source response = synthesised (“dirty”) beam





# Multiple baselines

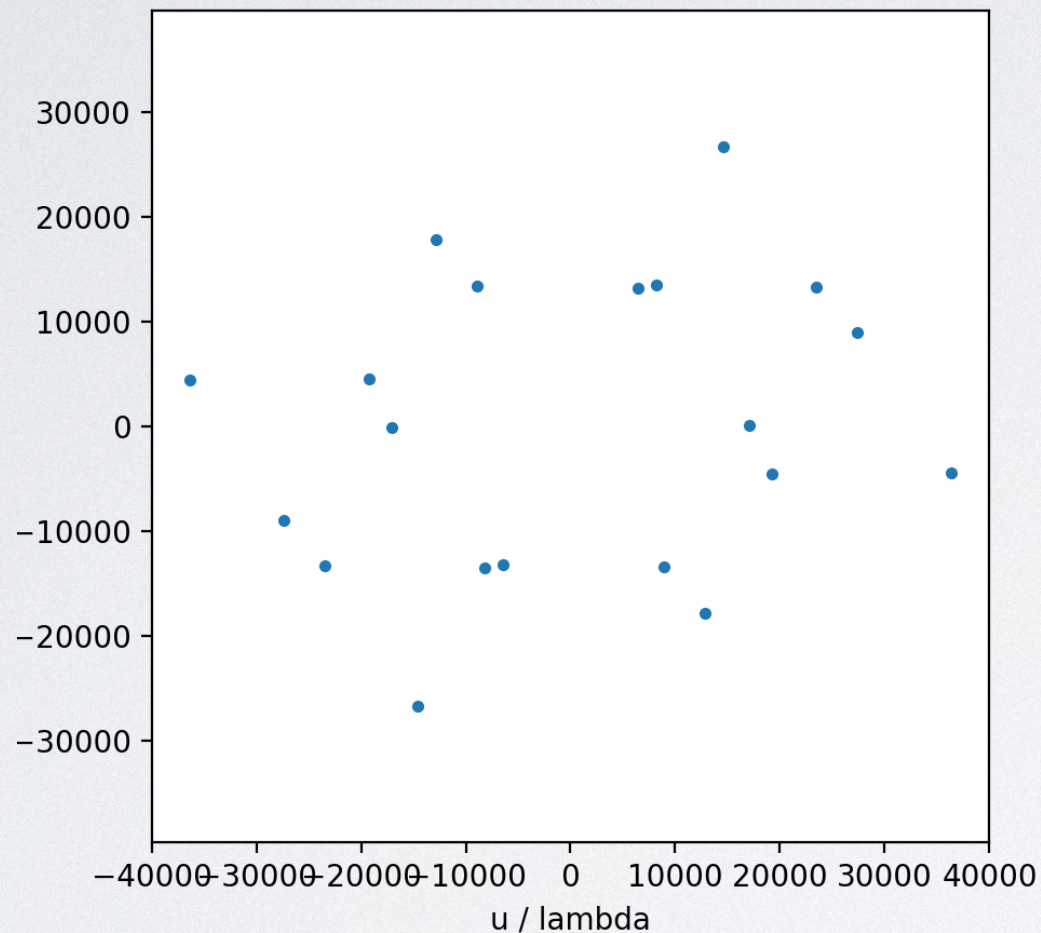
what is the dirty beam?



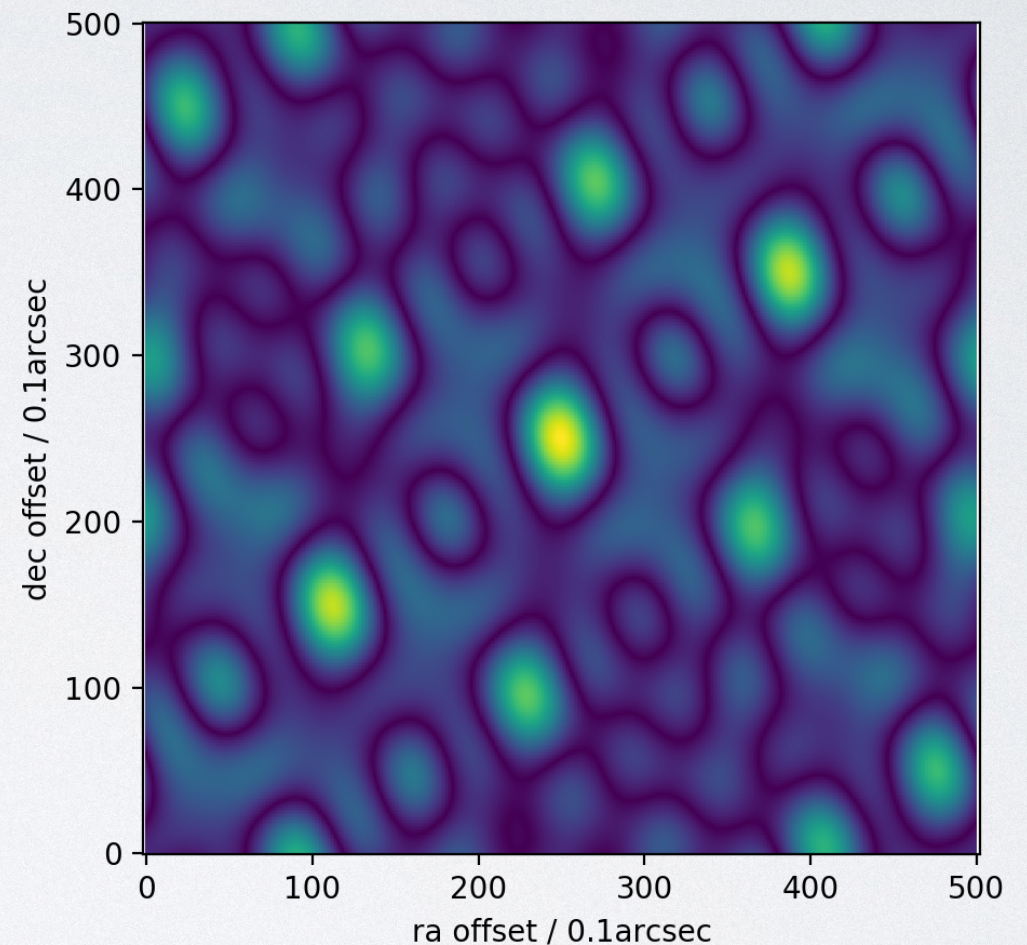


# Multiple baselines

$$B(u, v) = \sum_i (u_i, v_i)$$



$$FT^{-1}\{B(u, v)\} = b(x, y)$$



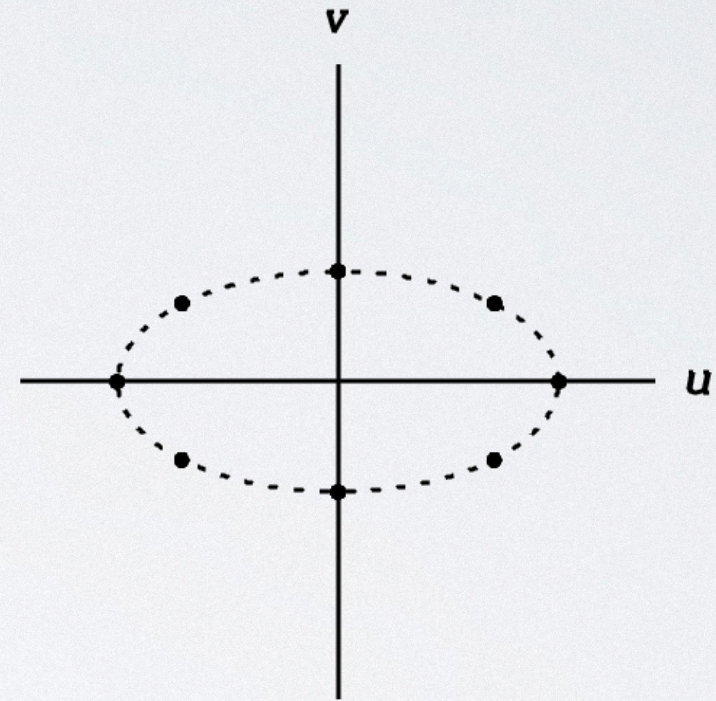
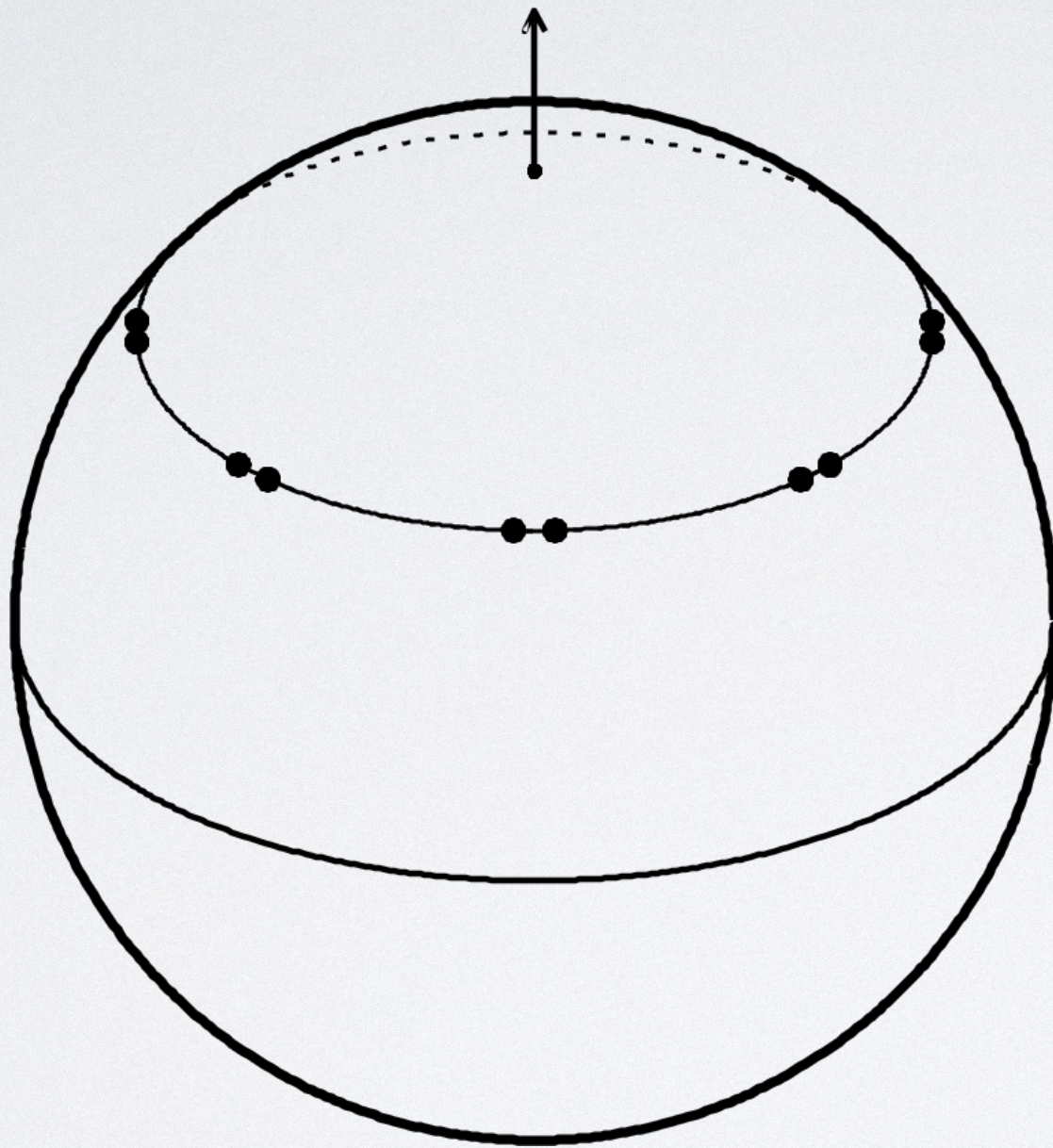
'dirty beam'

i.e. sample all spatial scales,  
and  $FT(\text{constant}) = \text{delta function}$



# Aperture synthesis

use Earth rotation to fill in uv plane

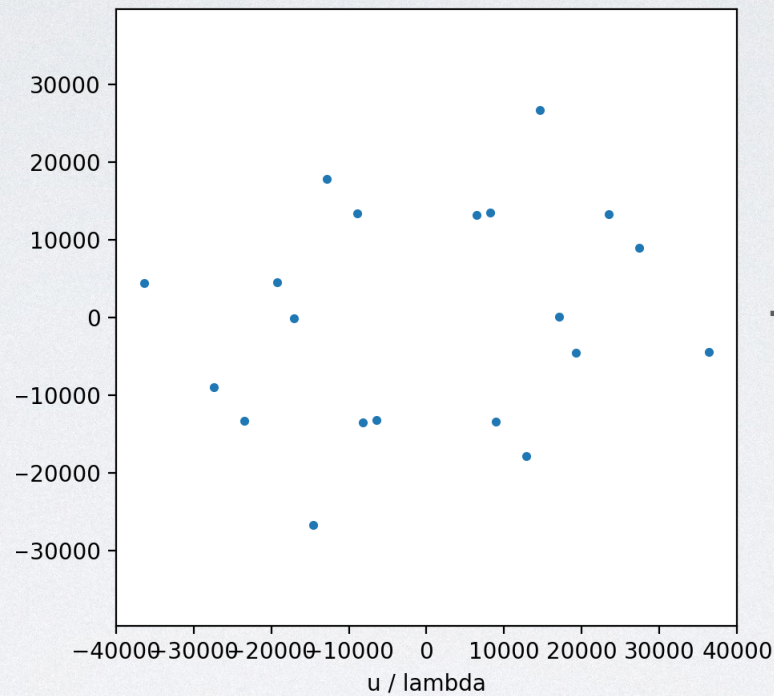
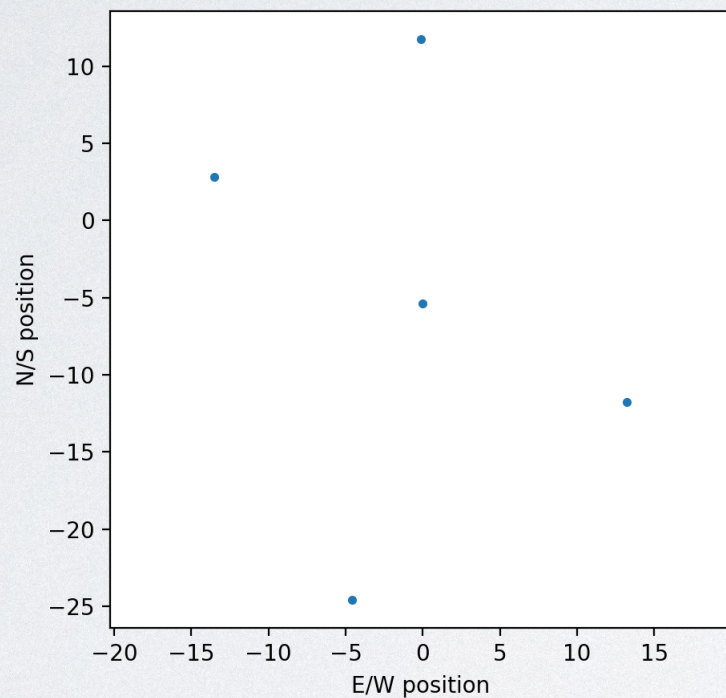




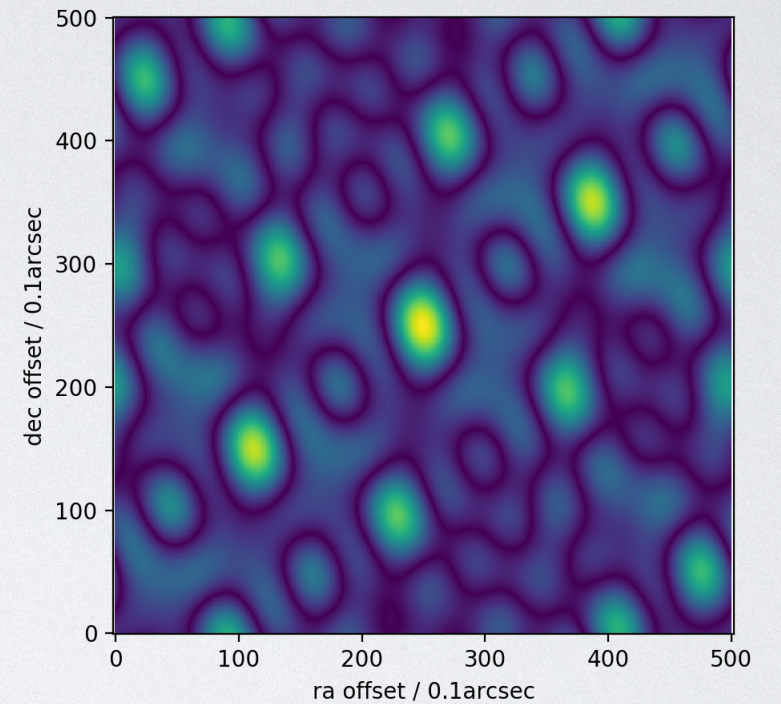
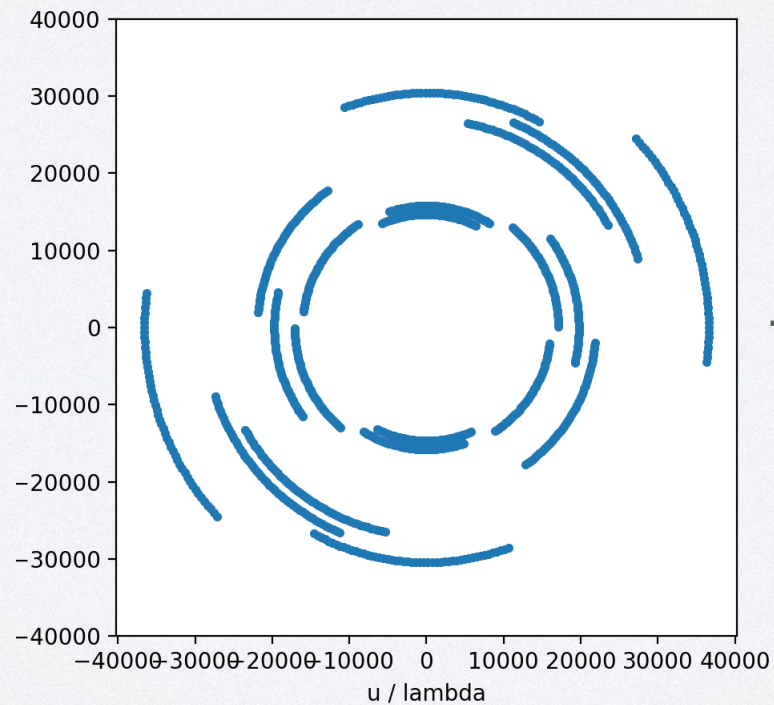
# Aperture synthesis

sky rotation makes all the difference

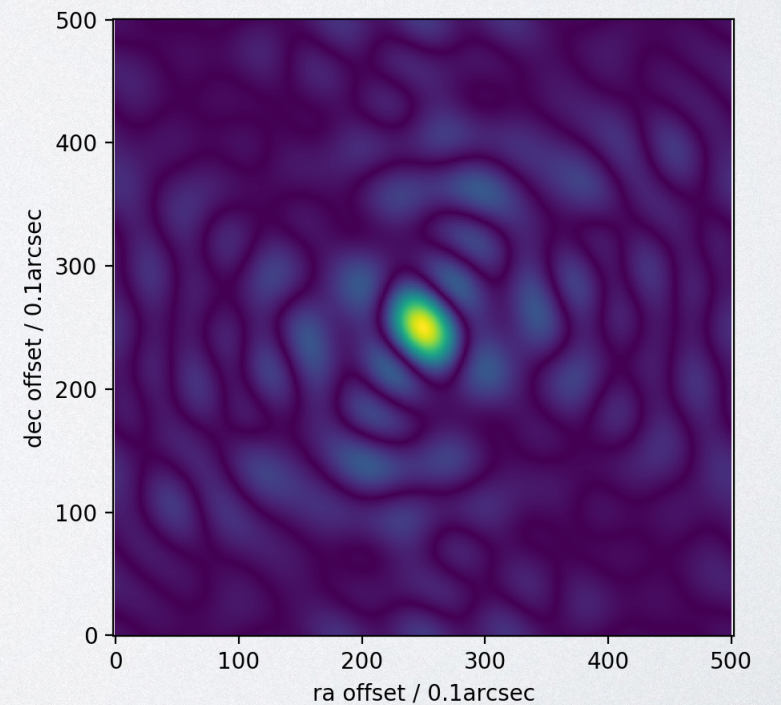
5 antennas



baselines



sum of fringes

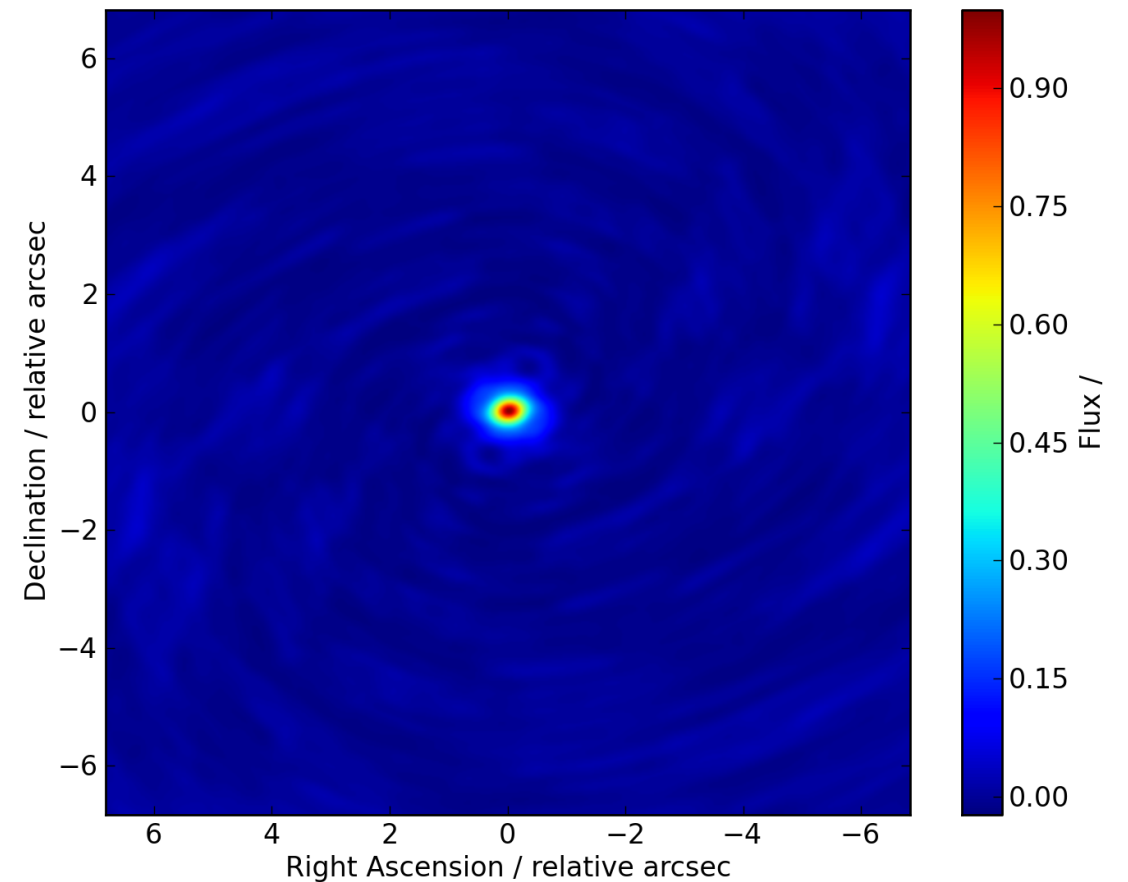
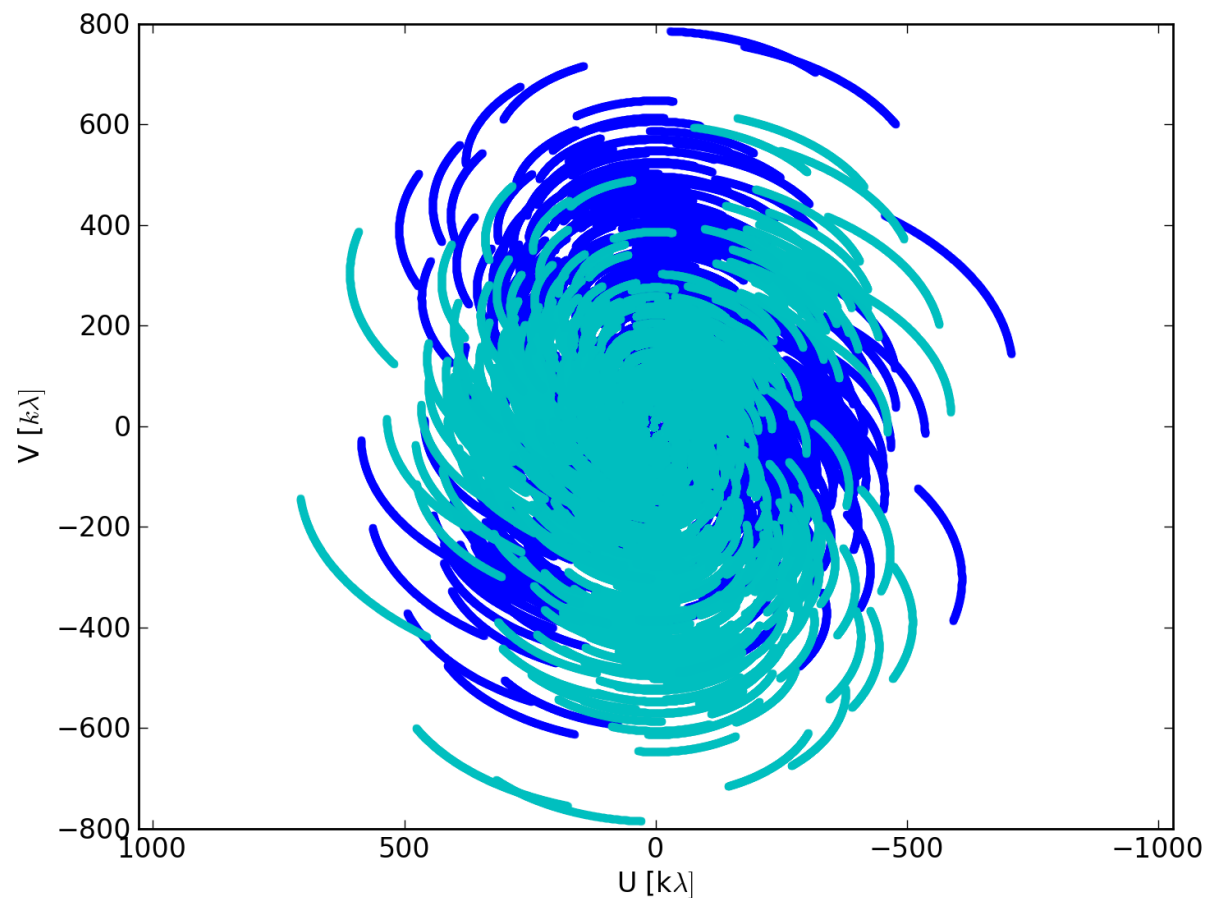




# Aperture synthesis

ALMA: 2.5km max baseline, 3h, 43 antennas: 861 baselines

(for ALMA integration time the main consideration)

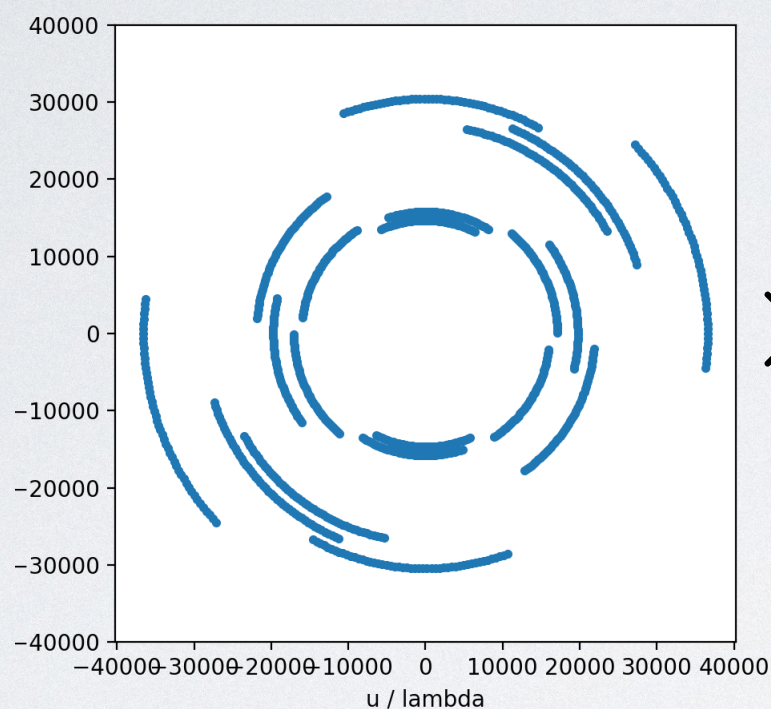


<http://almaost.jb.man.ac.uk/>

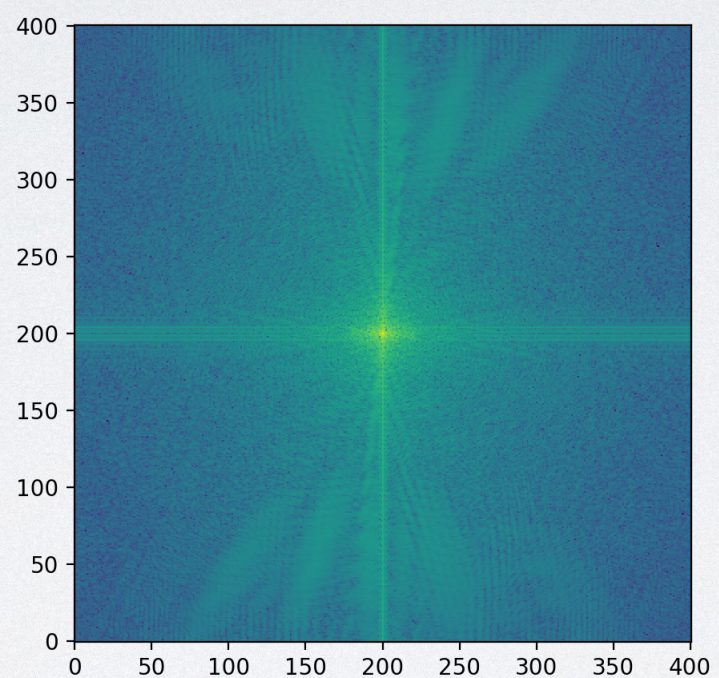


# Imaging visibilities

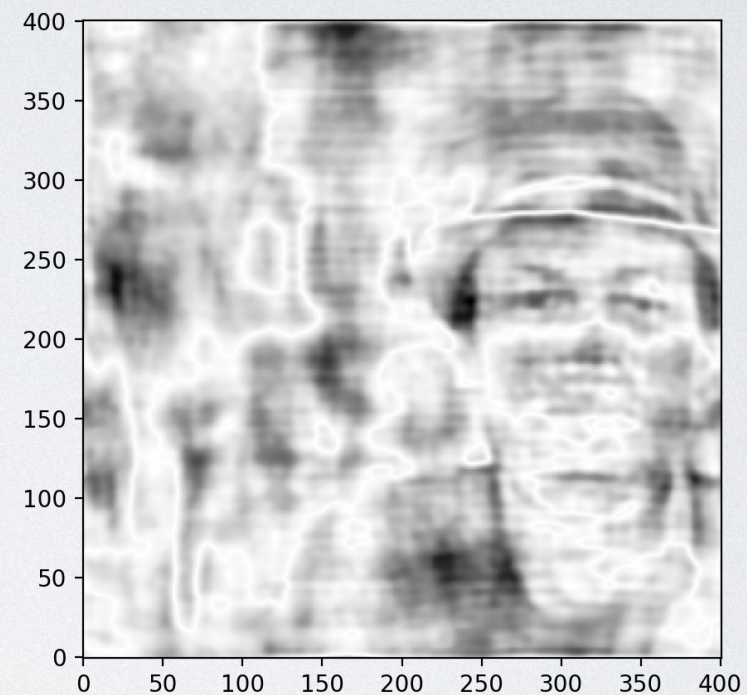
incomplete uv coverage results in spatial filtering



$\times$



$\xrightarrow{FT^{-1}}$



$FT\{me\}$  ↑





# CLEAN

turning visibility data into images

- Initialise residual image to dirty image
- Identify strongest source in residual image
  - subtract fraction of this peak from residual image
  - add it to clean component list
- Repeat until residual image maximum less than some threshold



# CLEAN

turning visibility data into images

- Make restored image:
  - make image with all clean components
  - convolve with Gaussian fit to main lobe of dirty beam
  - add residual map



# CLEAN

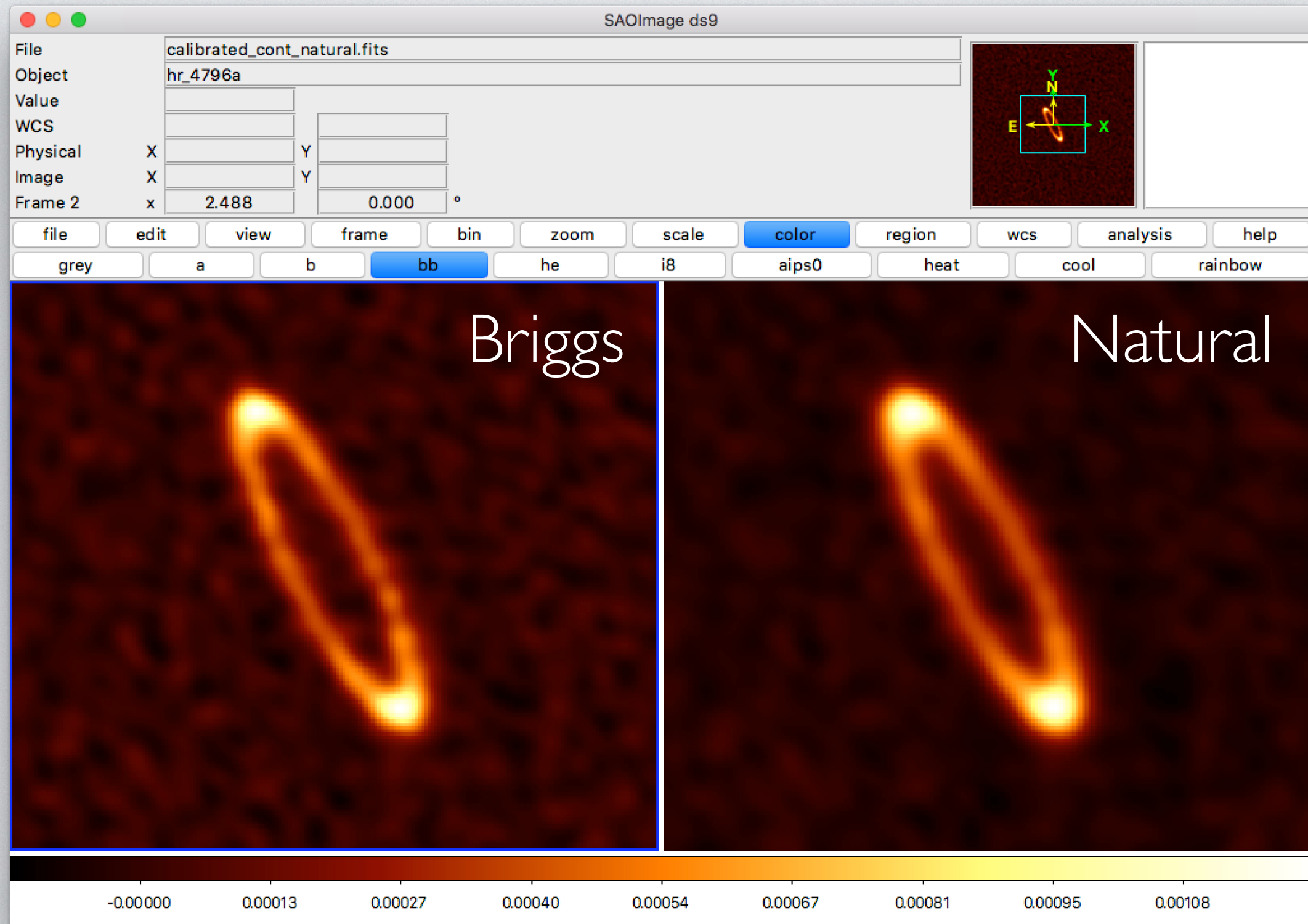
turning visibility data into images

- Main options:
  - Continuum vs. spectral cube
  - Choose how to weight baselines (e.g. 'natural')
  - Choose where clean components are ('mask')



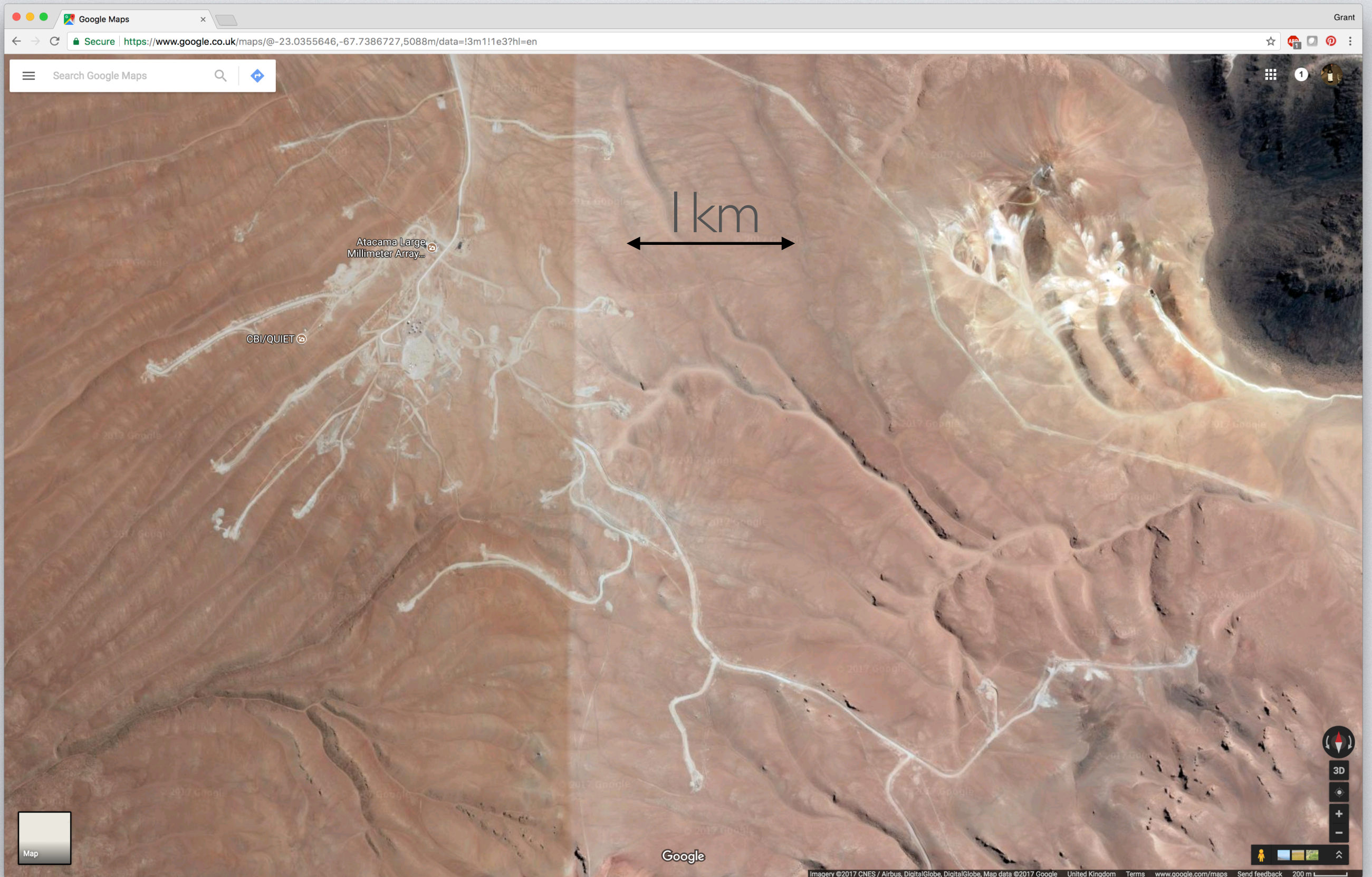
# CLEAN

turning visibility data into images





# ALMA





# ALMA





# ALMA

4 × 12m + 12 × 7m compact array, the 'ACA'  
acts as a 'single dish' to recover large scale structure





# Spectral line observations

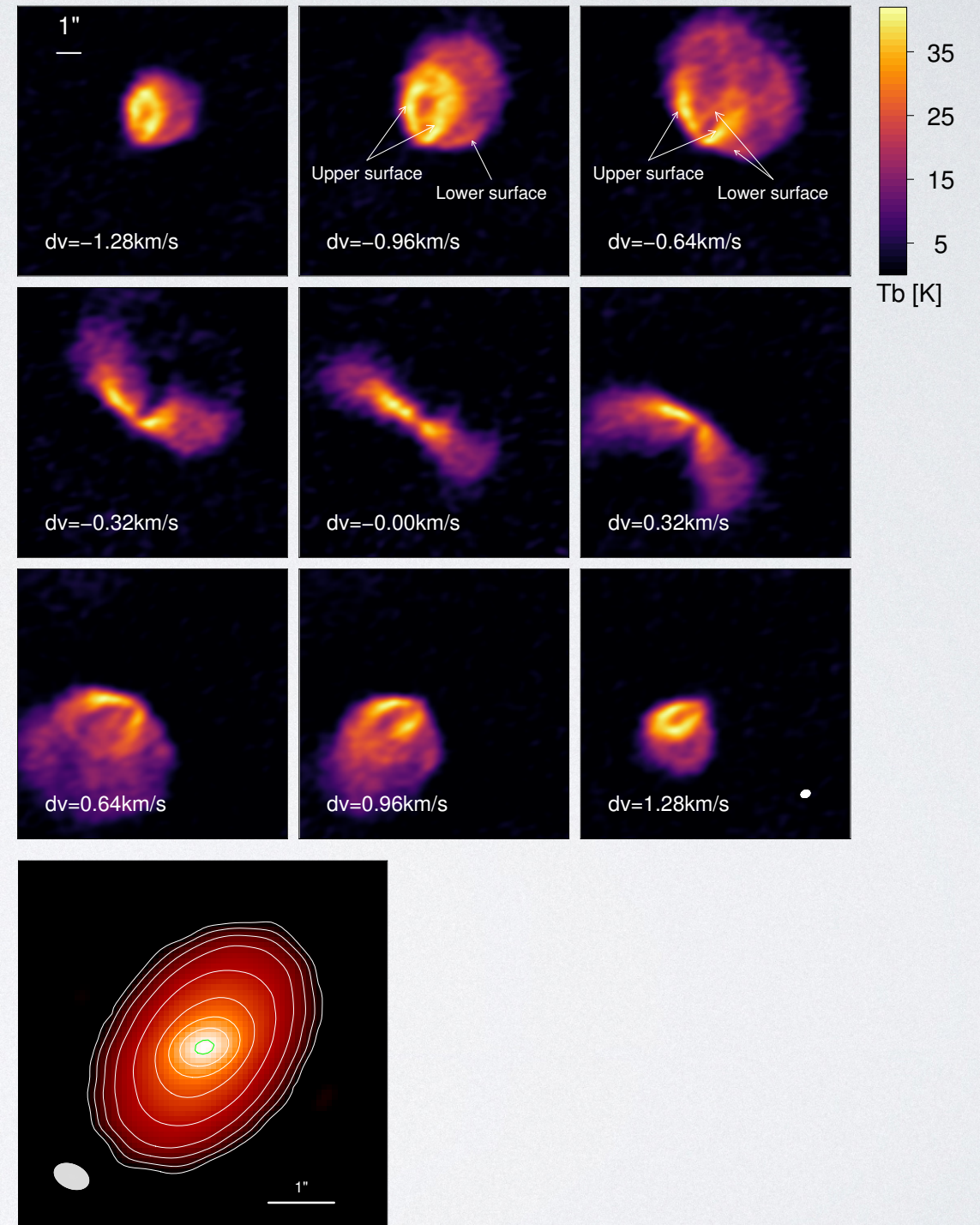
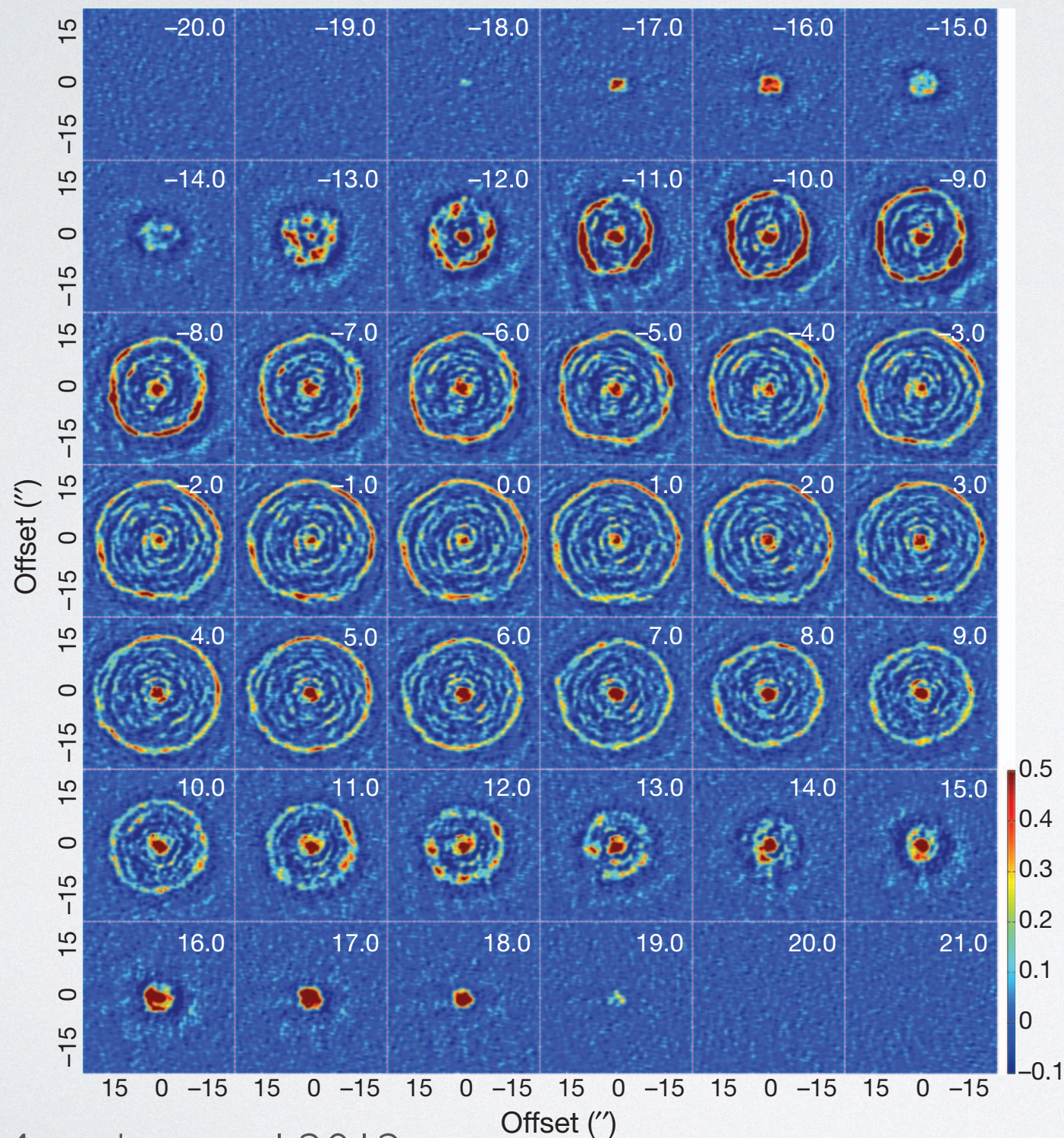


[www.eso.org](http://www.eso.org)



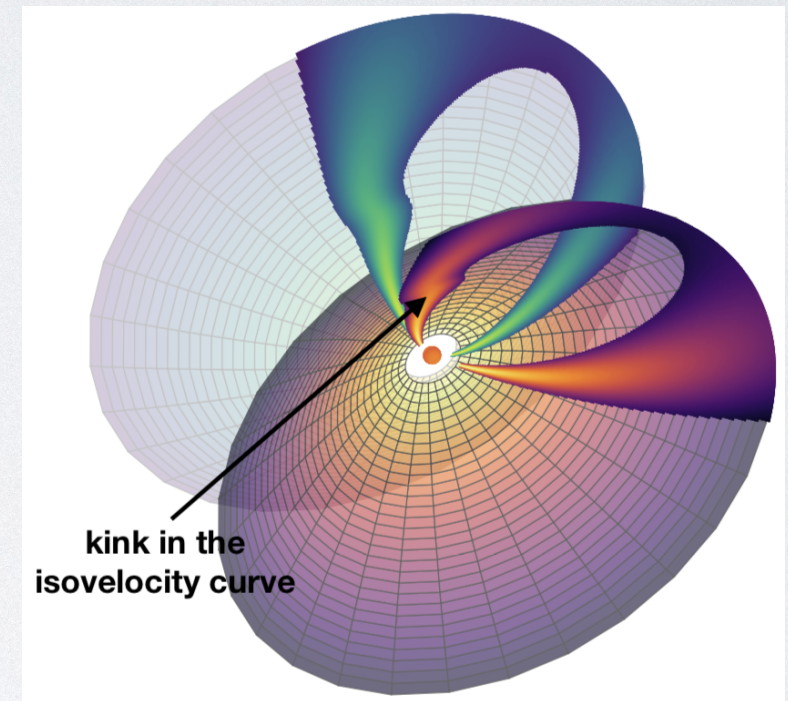
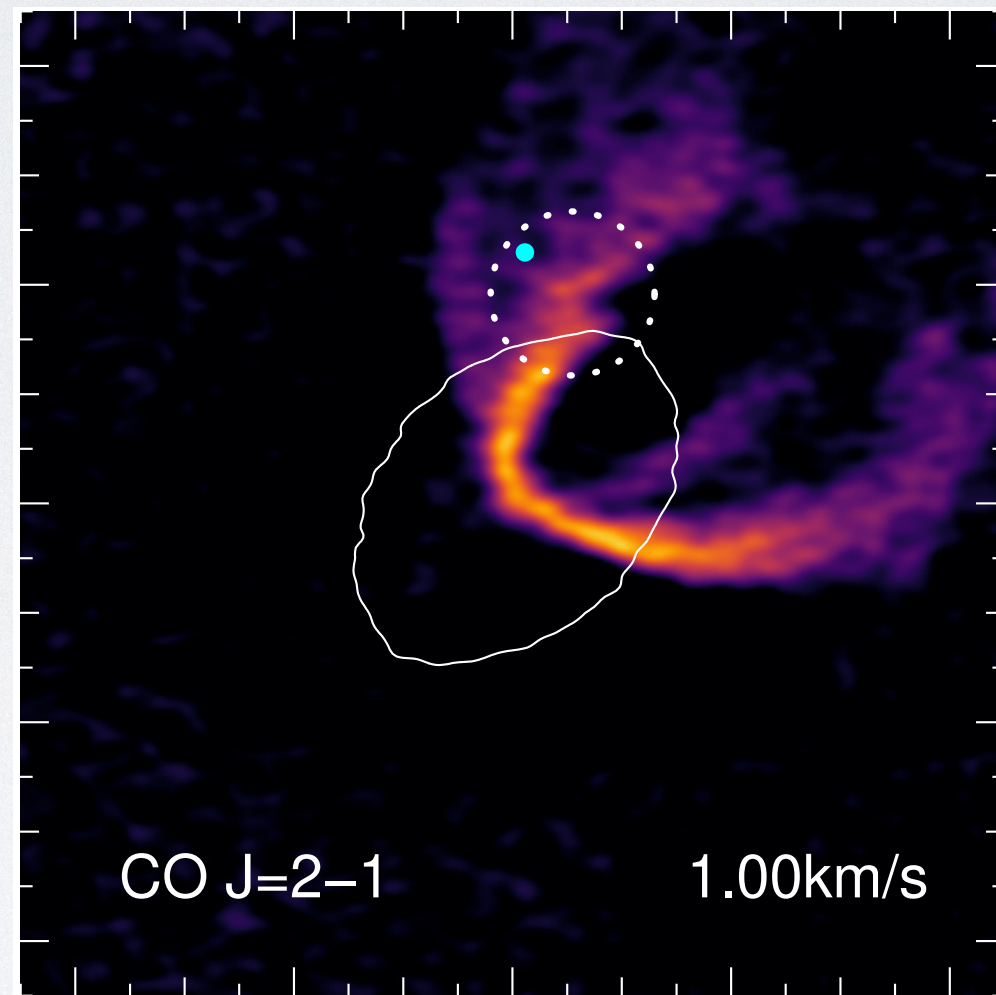
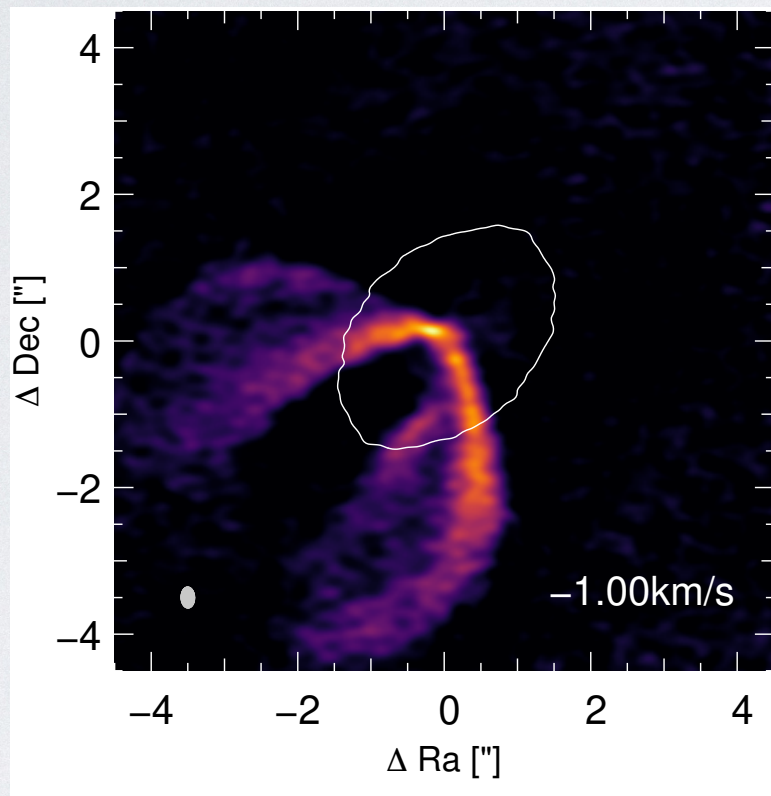
# Spectral line observations

different 'slices' through a data cube





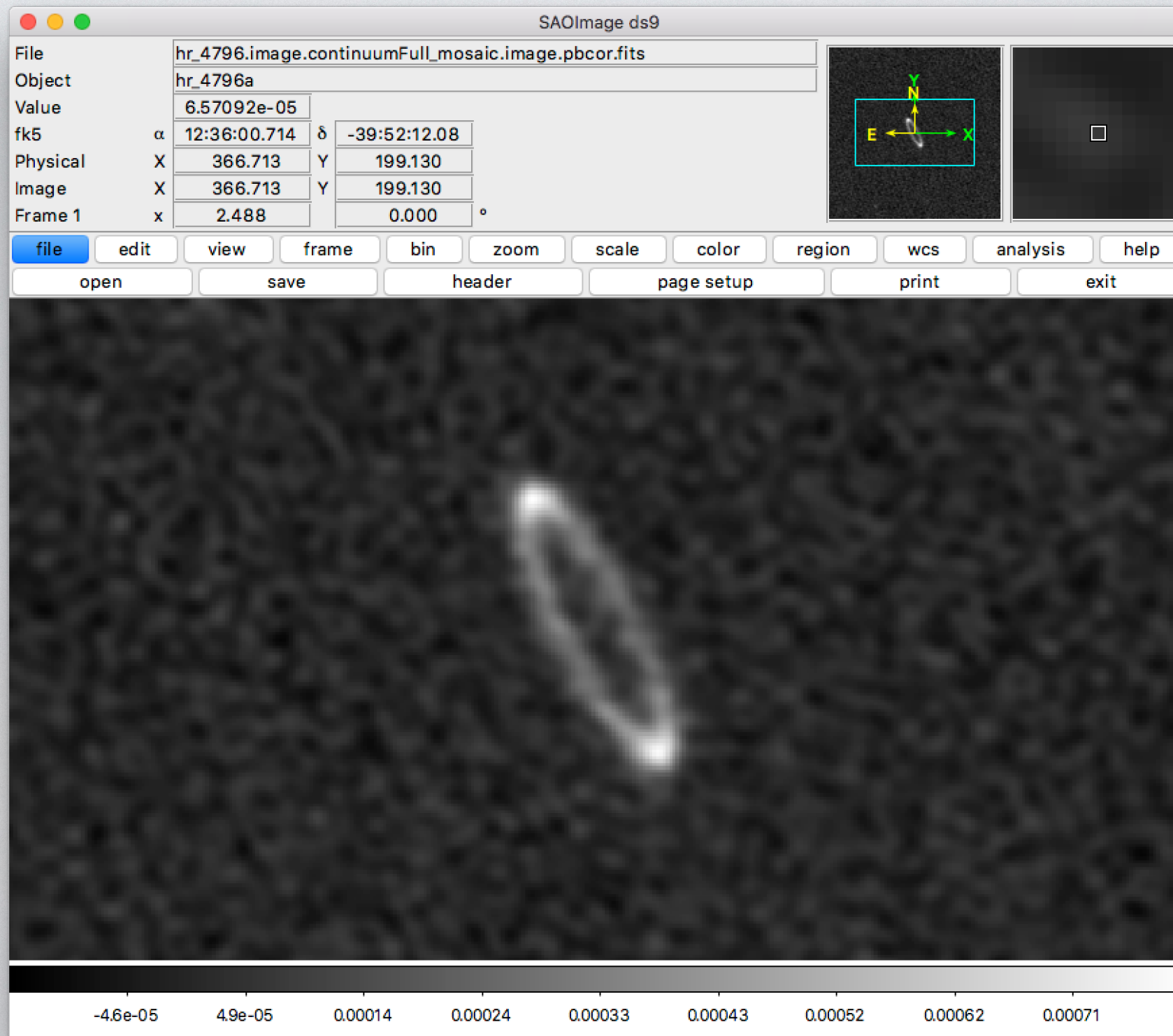
# Spectral line observations





# ALMA...

...will do a lot of the hard stuff for you





# ALMA

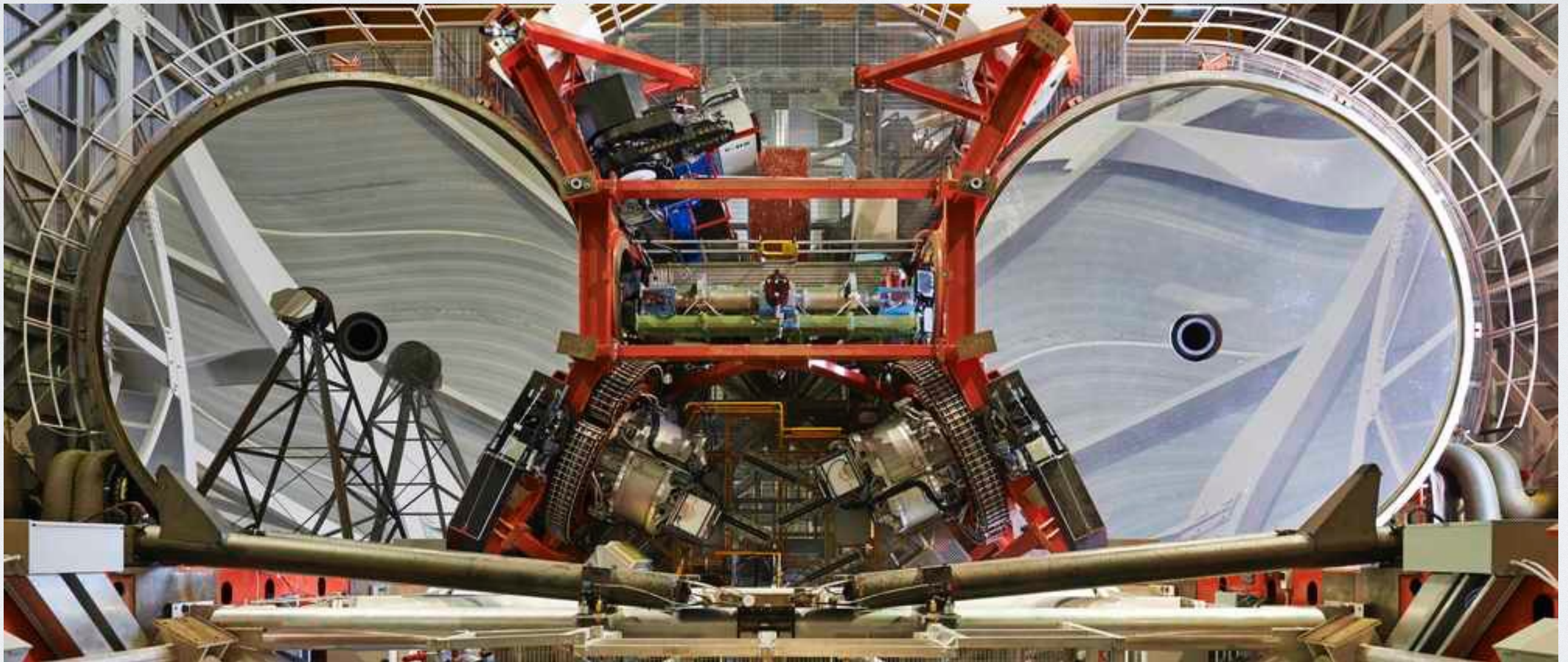
...and packages exist to deal with visibility modelling

- Modelling example:
- [https://github.com/drgmk/alma/blob/master/examples/vis\\_model.ipynb](https://github.com/drgmk/alma/blob/master/examples/vis_model.ipynb)



# Nulling interferometry

~as before, but 180deg phase shift and no correlator  
(i.e. photons on an IR detector)

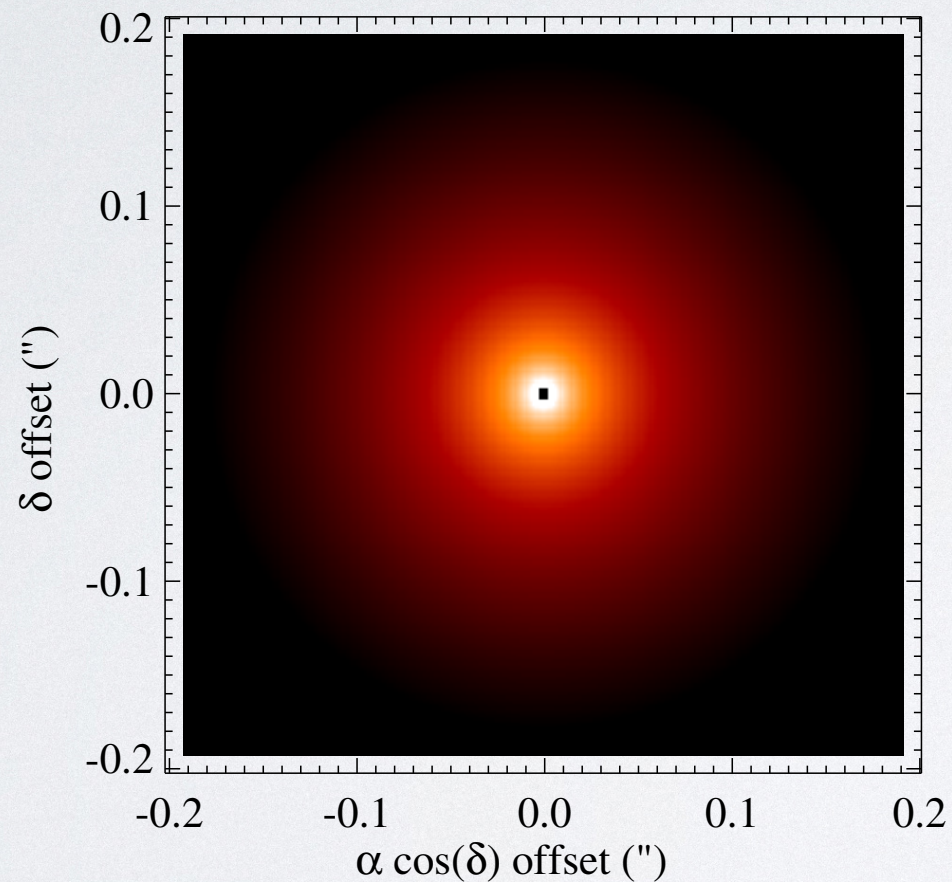




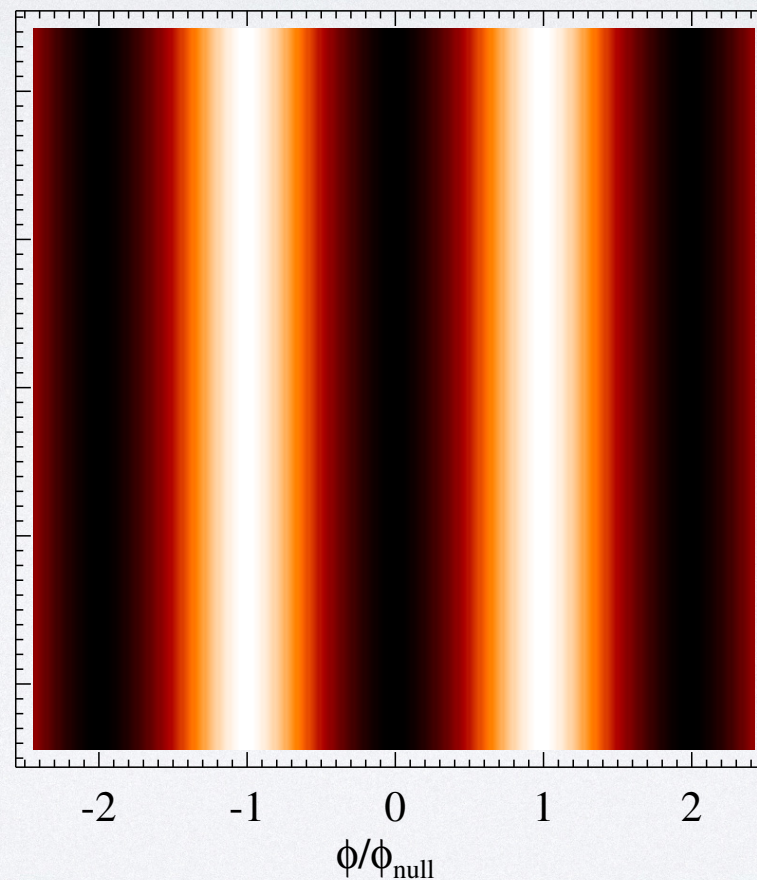
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(i.e. photons on an IR detector)

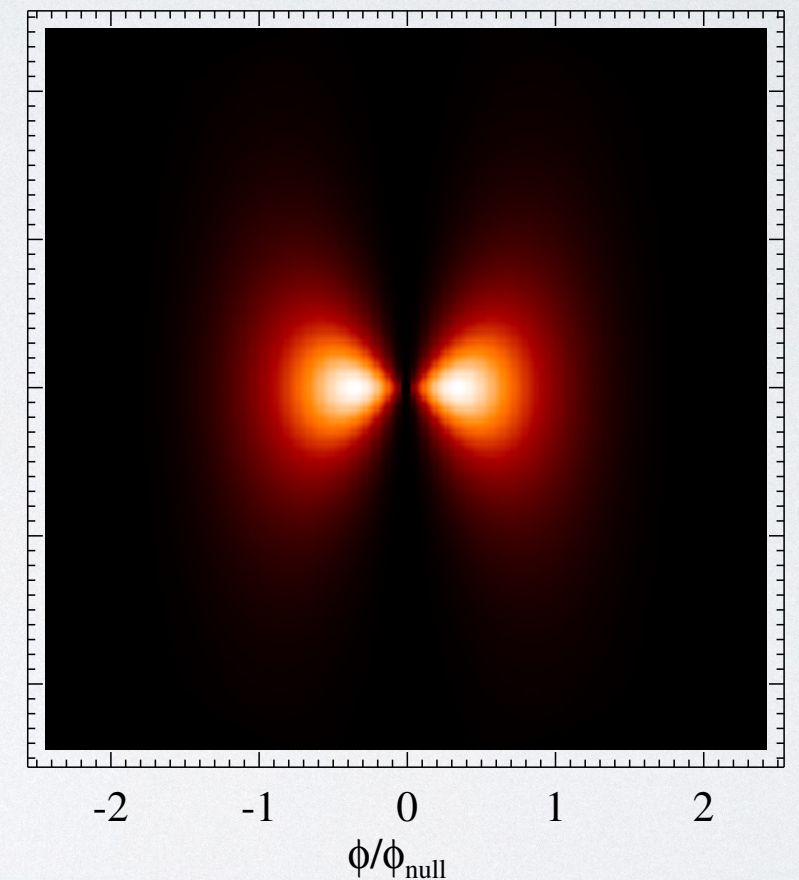
disk



transmission

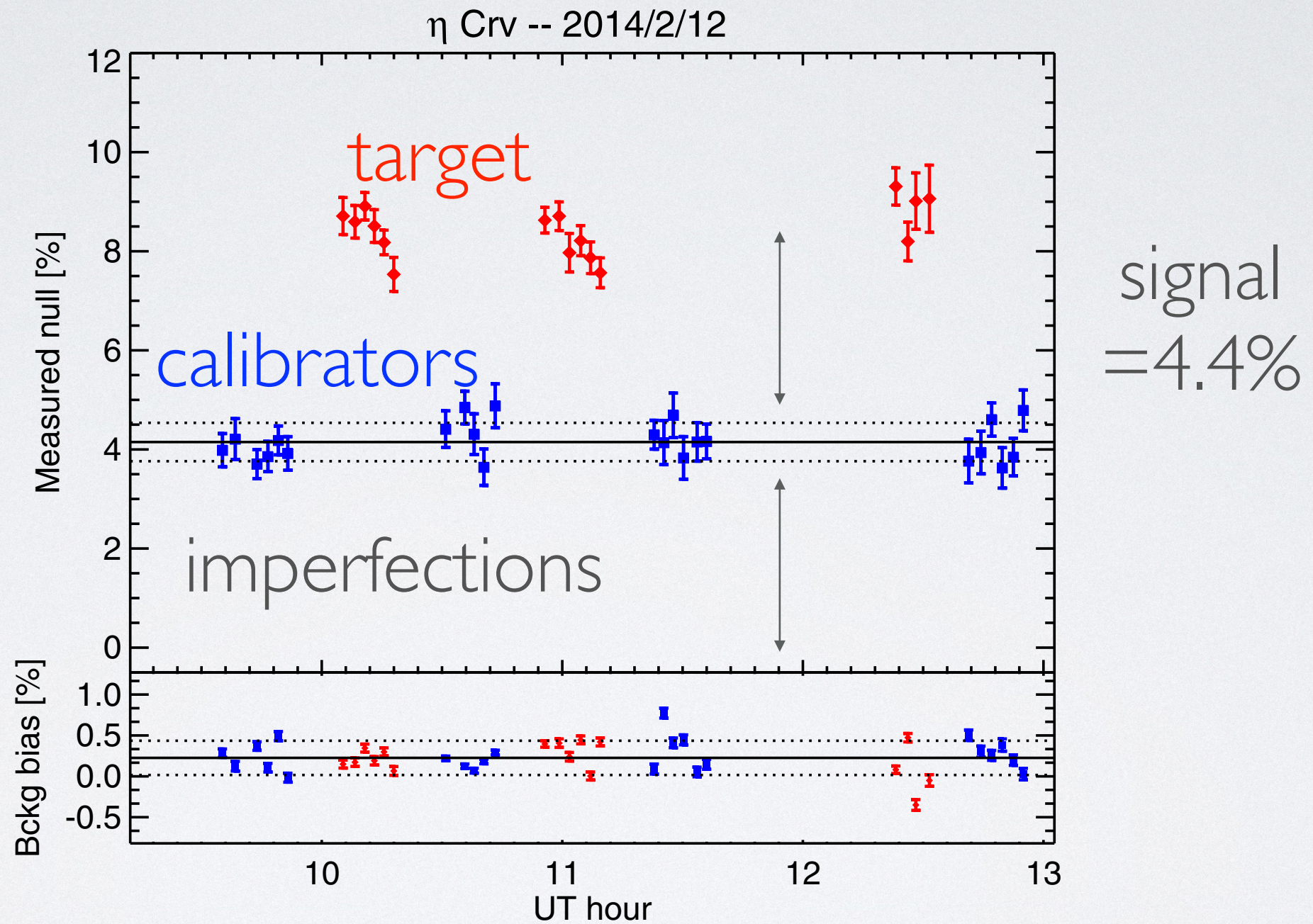


result





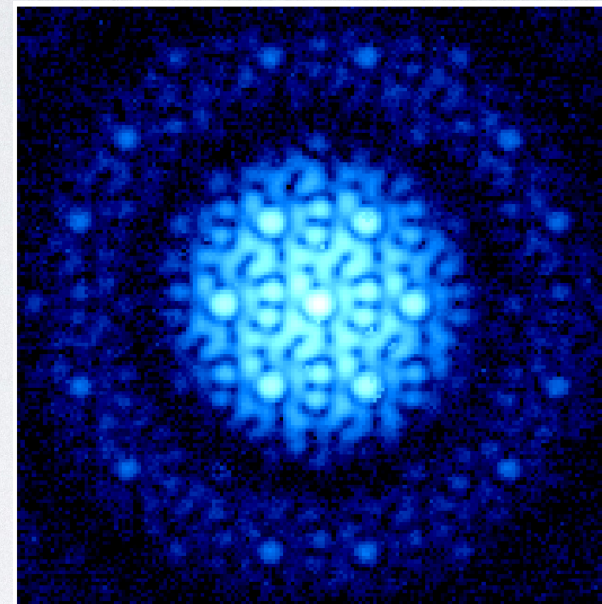
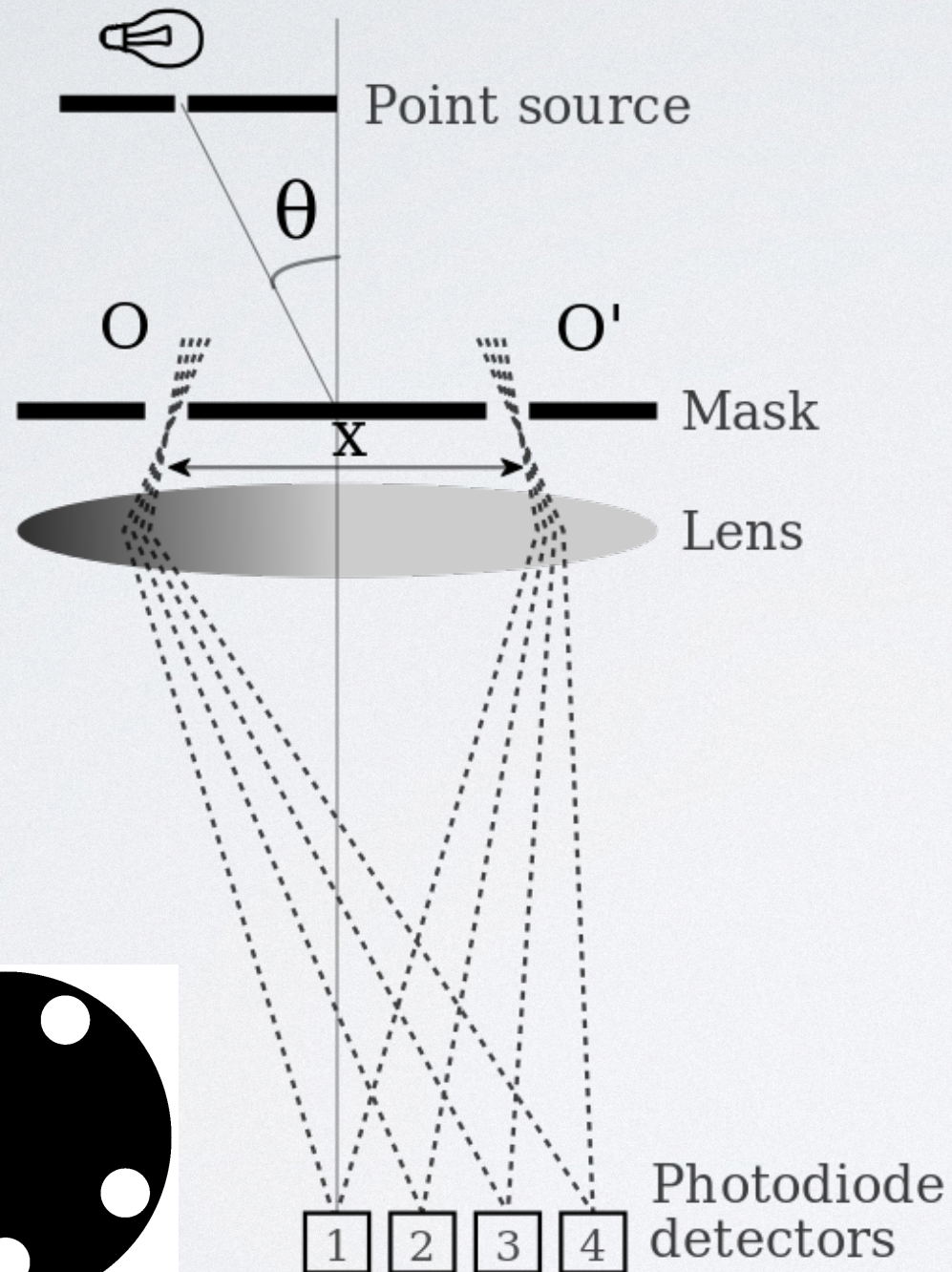
# LBTI - early results



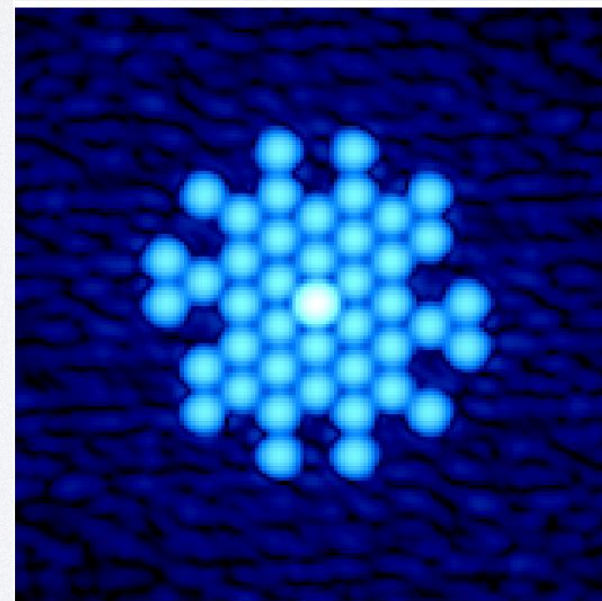
$$\text{signal} = \frac{\text{transmitted disk flux}}{\text{stellar flux}}$$



# Sparse Aperture Masking



image



Fourier transform  
(42 dots)

21 unique baselines - 'sparse'



# Resources

- <http://www.phys.unm.edu/~gbtaylor/astr423/s98book.pdf>
- <https://science.nrao.edu/opportunities/courses/era/>
- John D Monnier, 2003, Rep. Prog. Phys. 66 789
- <http://almaost.jb.man.ac.uk/> <https://github.com/crpurcell/friendlyVRI>
- <http://www.jb.man.ac.uk/pynterferometer/index.html>
- <https://launchpad.net/apsynsim>
- [https://github.com/griffinfoster/fundamentals\\_of\\_interferometry](https://github.com/griffinfoster/fundamentals_of_interferometry)



# Summary

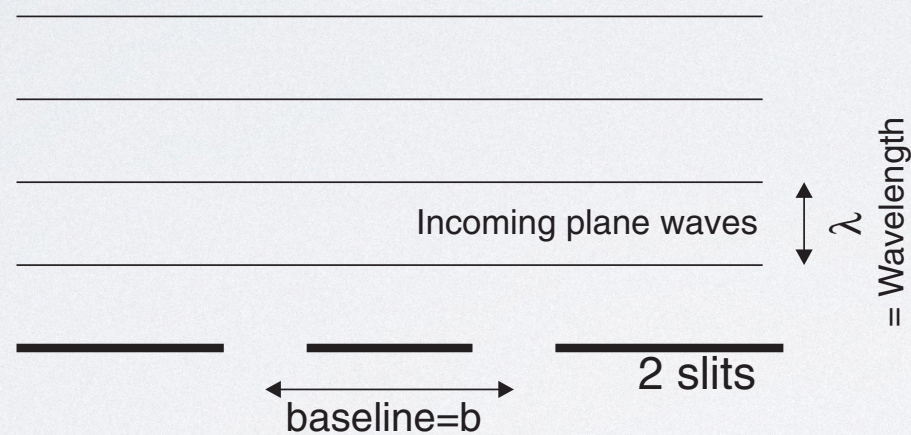
- Interferometry is a valuable and flexible tool
- Main concept: interferometer samples  $uv$  space
- With good  $uv$  coverage; well-defined beam, images



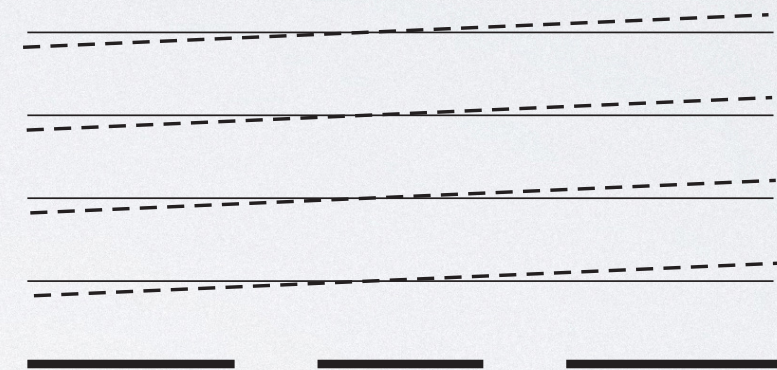


# When is a source resolved?

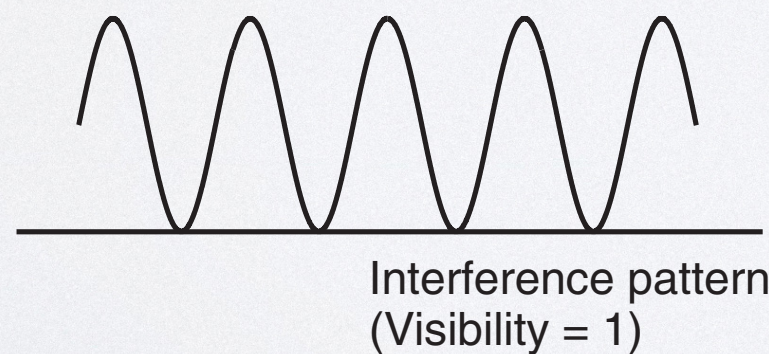
○ Point source at infinity



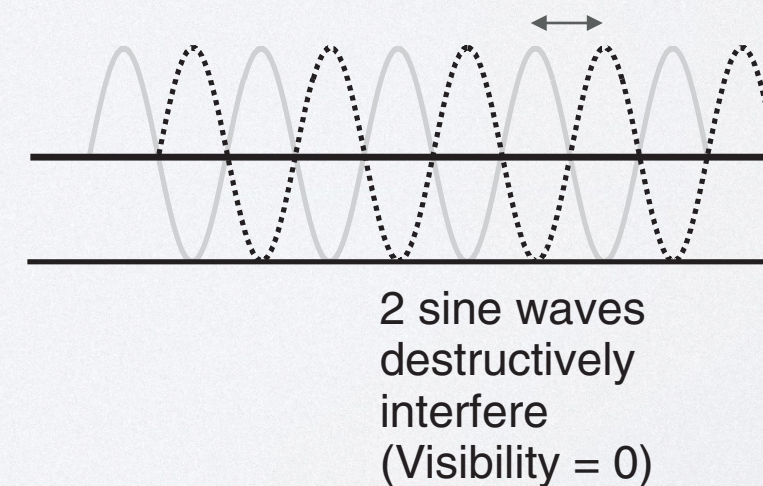
○ ○ Point sources at infinity separated by 1/2 the fringe spacing



$\Delta\theta$  = Fringe spacing  
 $\lambda/b$  radians



$$\Delta\theta = \lambda / (2b)$$



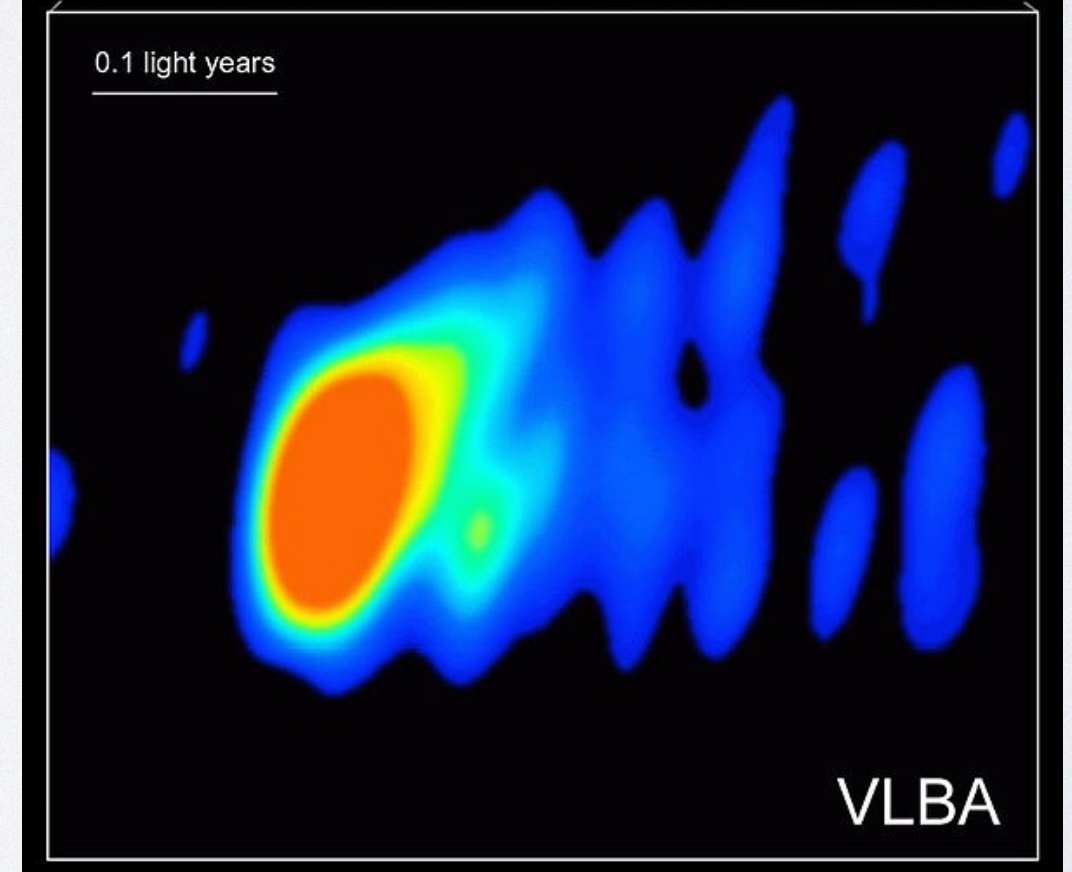
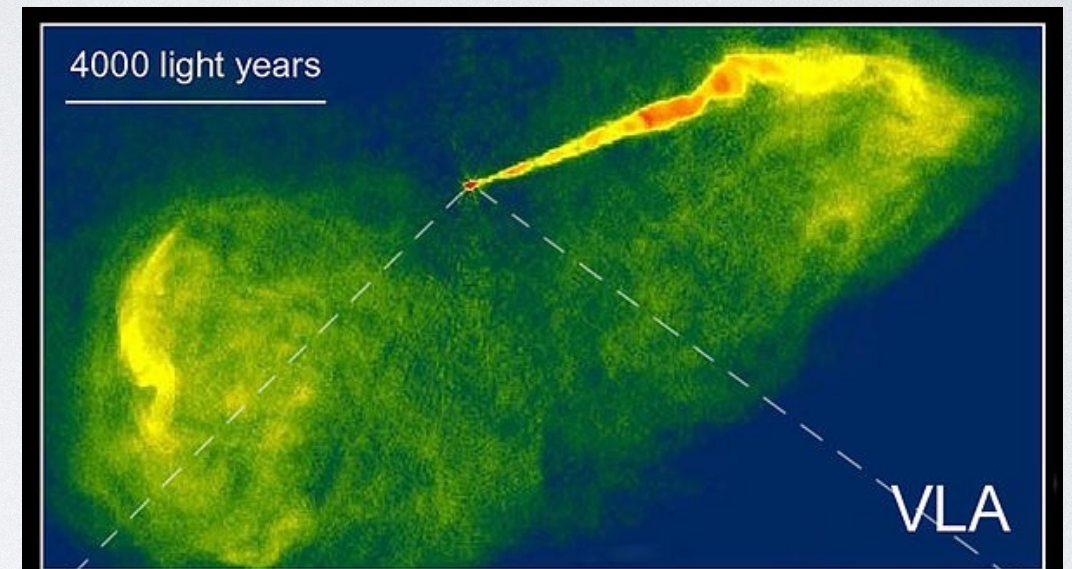


# Radio astronomy

M87



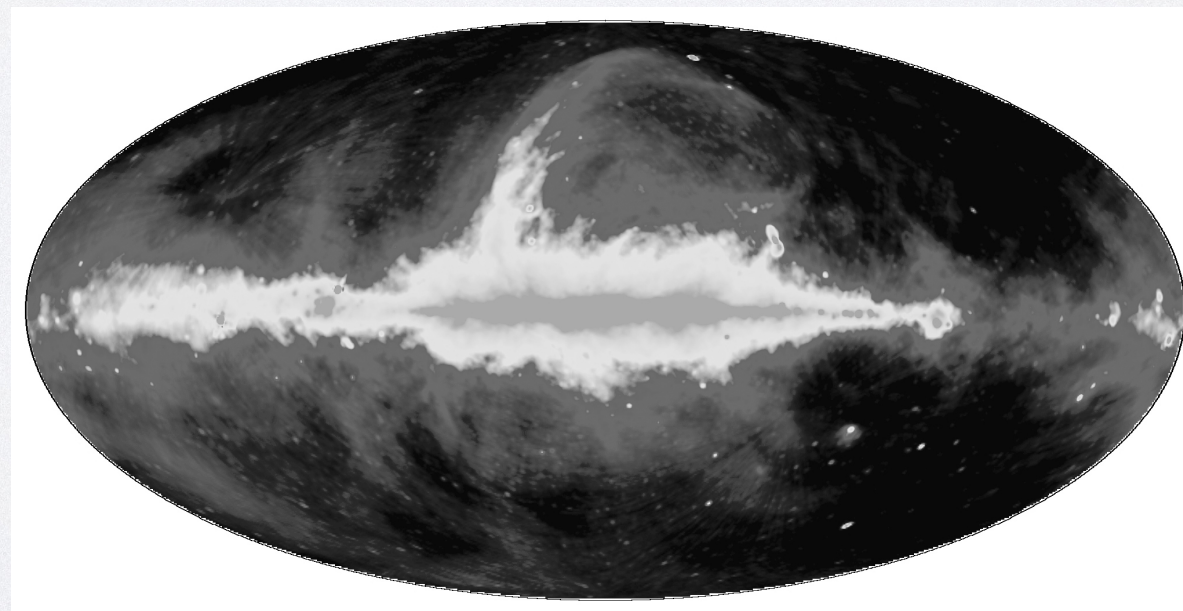
- Dust obscures optical light
- Not all emission is thermal





# Radio astronomy

- Interstellar dust smaller than wavelength - e.g. Sgr A\*
- Cold emission negligible in optical - e.g. CMB
- Free-free radiation - e.g. (ionised) HII regions
- Spectral lines - e.g. 21 cm HI line, CO rotational transitions
- Synchrotron emission -  $e^-$  accelerated in SN remnants



sky at 408MHz